

Compiler Construction

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Computer Systems Group
LIACS

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Why This Course

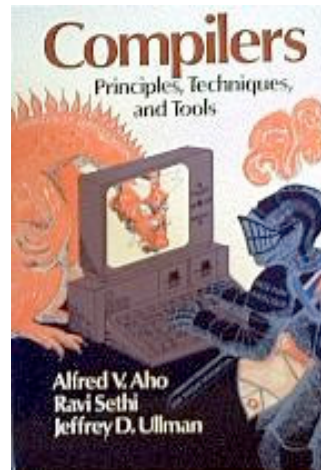
- ⌘ Know how to build a compiler for a (simplified) (programming) language
- ⌘ Know how to use compiler construction tools, such as generators for scanners and parsers
- ⌘ Be able to write LL(1), LR(1) grammars (for new languages)
- ⌘ Be familiar with compiler analysis and optimization techniques
- ⌘ ... learn how to work on a larger software project!

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Course Outline

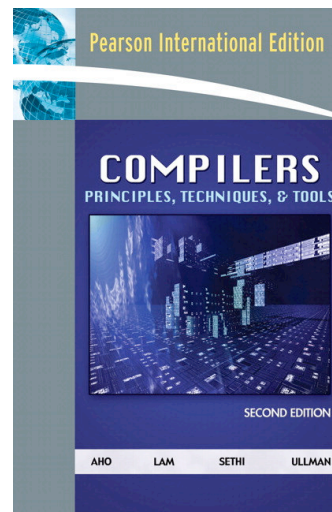
- ⌘ In class, we discuss the theory using the 'dragon' book by Aho et al.
- ⌘ In the practicum, the theory is applied when building a compiler that converts Pascal code to MIPS instructions.

A.V. Aho, R. Sethi, en J.D. Ullman, Compilers: Principles, Techniques, and Tools, Addison-Wesley, 1986, ISBN: 0-201-10088-6.



New edition

- ⌘ Dragon book has been revised in 2006
- ⌘ In Second edition good improvements are made
- ⌘ **Publisher:** Addison Wesley; 2 edition (August 31, 2006)
- ⌘ **Language:** English
- ⌘ **ISBN-10:** 0321486811



Course Outline

⌘ Contact hours

- ☒ Official communication medium is email
- ☒ Blackboard (<http://blackboard.leidenuniv.nl>)
- ☒ All material needed is available here

⌘ Practicum

- ☒ Different from previous years, we now offer 5 self contained assignments
- ☒ These assignments are done by groups of two persons
- ☒ Assignments are handed in into CVS

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Course Outline

⌘ Grading

- ☒ 2 ECTS Written Exam
- ☒ 5 ECTS Practicum

⌘ You need to pass all 5 assignments

⌘ No 'late' submissions will be accepted!

- ☒ If you miss these assignments, you have to wait until next year

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Course Outline (Tentative)

- ⌘ 04/09/08 Introduction
- ⌘ 11/09/08 Lexical and Syntax Analysis
- ⌘ 18/09/08 Syntax Analysis assignment 1
- ⌘ 25/09/08 NO CLASS
- ⌘ 02/10/08 Type Checking assignment 2
- ⌘ 09/10/08 Intermediate Code Generation 1
- ⌘ 16/10/08 NO CLASS
- ⌘ 23/10/08 Intermediate Code Generation 2 assignment 3
- ⌘ 30/10/08 Code Generation 1
- ⌘ 06/11/08 Code Generation 2 assignment 4
- ⌘ 13/11/08 Run-Time Organization
- ⌘ 20/11/08 Code Optimizations assignment 5
- ⌘ 27/11/08 ELECTIVE
- ⌘ 04/12/08 backup date

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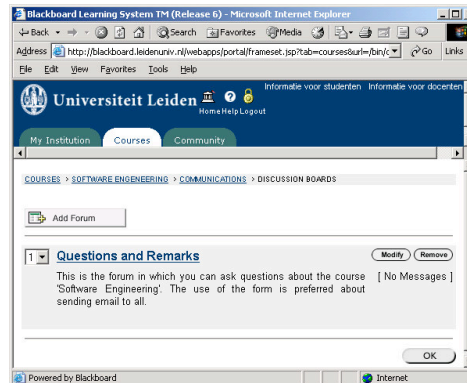
Practicum

- ⌘ 28/09-02/10 assignment 1, Calculator
 - ⌘ 02/10-23/10 assignment 2, Parsing & Syntax tree
 - ⌘ 23/10-06/11 assignment 3, Intermediate code
 - ⌘ 06/11-20/11 assignment 4, Assembly generation
 - ⌘ 20/11-04/12 assignment 5, Optimizations
- ⌘ All deadlines are at 17.00h (5 pm).
- ⌘ The deadlines are strict.
- ⌘ Submission takes place in CVS

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Blackboard Coco

- ⌘ Please enroll on-line to Coco in Blackboard
- ⌘ Communication about Coco is shared between everyone.
- ⌘ Use the 'Forum' option to ask me questions.
- ⌘ If you ask me directly, I will submit also to the forum.



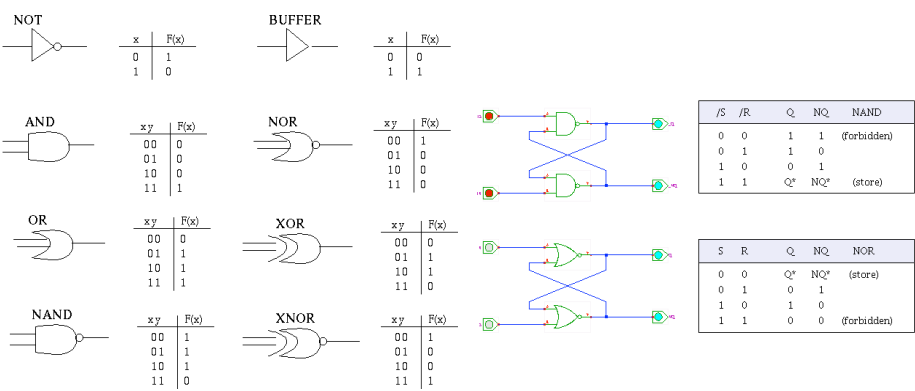
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Introduction

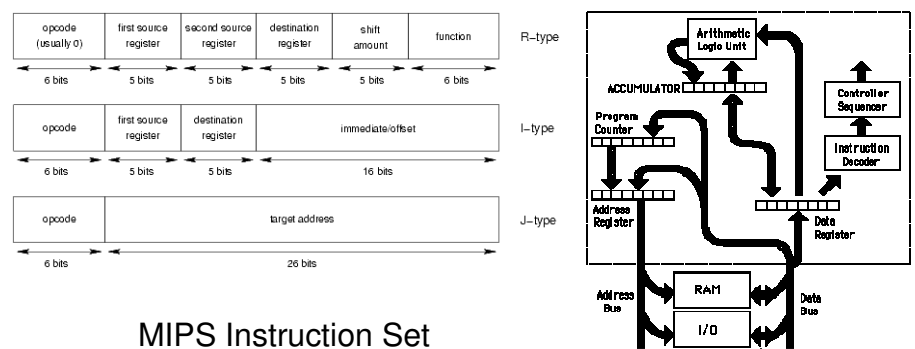
- ⌘ Compiler Construction
- ⌘ Missing Link between
 - ⊞ Digital Technique
 - ⊞ Boolean Logic
 - ⊞ Flip-Flops
 - ⊞ Computer Architectures
 - ⊞ Memory
 - ⊞ Instructions

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Digital Technique



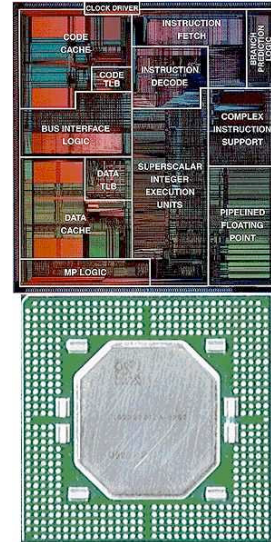
Computer Architecture



MIPS Instruction Set

opcode field opcode instruction format

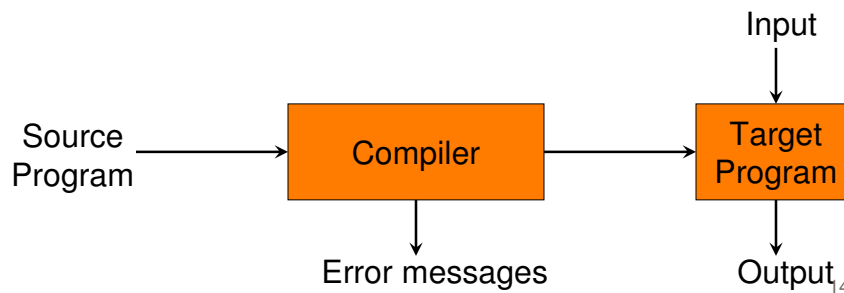
000010	j	J-type
000011	jal	J-type
000100	beq	I-type
000101	bne	I-type
001000	Addi	I-type
001001	Addiu	I-type
001010	Slti	I-type
001011	Sltiu	I-type
001100	Andi	I-type



Compilers and Interpreters

⌘ "Compilation"

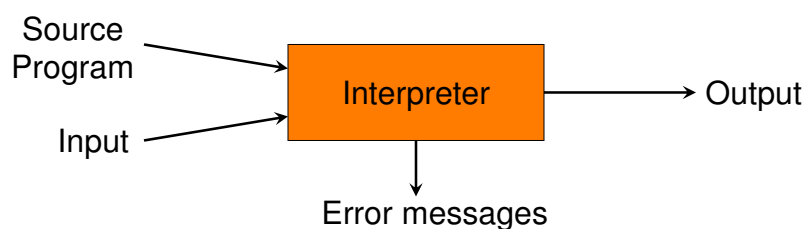
- ☒ Translation of a program written in a source language into a semantically equivalent program written in a target language



Compilers and Interpreters (cont'd)

⌘ "Interpretation"

- ☒ Performing the operations implied by the source program



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The Analysis-Synthesis Model of Compilation

⌘ There are two parts to compilation:

- ☒ *Analysis* determines the operations implied by the source program which are recorded in a tree structure
- ☒ *Synthesis* takes the tree structure and translates the operations therein into the target program

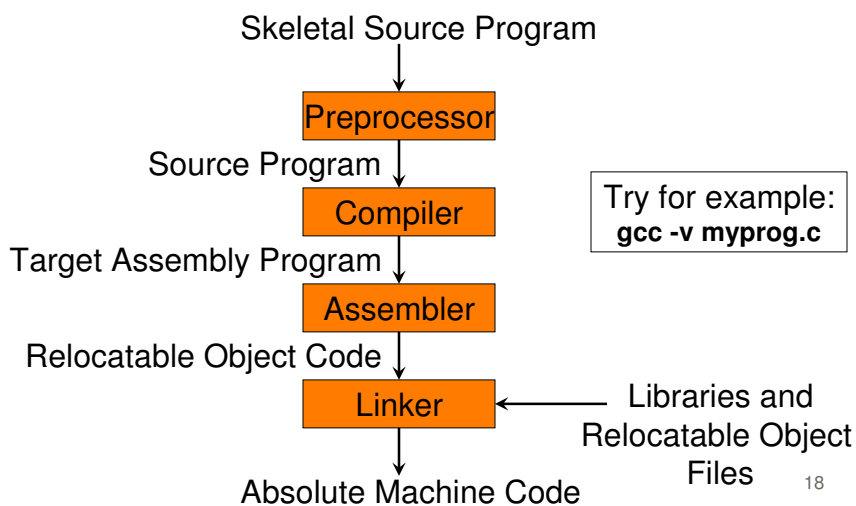
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Other Tools that Use the Analysis-Synthesis Model

- ⌘ *Editors* (syntax highlighting)
- ⌘ *Pretty printers* (e.g. doxygen)
- ⌘ *Static checkers* (e.g. lint and splint)
- ⌘ *Interpreters*
- ⌘ *Text formatters* (e.g. TeX and LaTeX)
- ⌘ *Silicon compilers* (e.g. VHDL)
- ⌘ *Query interpreters/compilers* (Databases)

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Preprocessors, Compilers, Assemblers, and Linkers



The Phases of a Compiler

Phase	Output	Sample
<i>Programmer</i>	Source string	<code>A=B+C;</code>
<i>Scanner</i> (performs <i>lexical analysis</i>)	Token string	<code>'A', '=', 'B', '+', 'C', '\n', '\n'</code> And <i>symbol table</i> for
<i>Parser</i> (performs <i>syntax analysis</i> based on the grammar of the programming language)	Parse tree or abstract syntax tree	identifiers <pre> = / \ A + / \ B C </pre>
<i>Semantic analyzer</i> (type checking, etc)	Parse tree or abstract syntax tree	
<i>Intermediate code generator</i>	Three-address code, quads, or RTL	<code>int2fp B t1</code> <code>+ t1 C t2</code> <code>:= t2 A</code>
<i>Optimizer</i>	Three-address code, quads, or RTL	<code>int2fp B t1</code> <code>+ t1 #2.3 A</code>
<i>Code generator</i>	Assembly code	<code>MOVF #2.3, r1</code> <code>ADDF2 r1, r2</code> <code>MOVF r2, A</code>
<i>Peephole optimizer</i>	Assembly code	<code>ADDF2 #2.3, r2</code> <code>MOVF r2, A</code> 19

The Grouping of Phases

⌘ Compiler front and back ends:

- ☒ Analysis (*machine independent* front end)
- ☒ Synthesis (*machine dependent* back end)

⌘ Passes

- ☒ A collection of phases may be repeated only once (*single pass*) or multiple times (*multi pass*)
- ☒ Single pass: usually requires everything to be defined before being used in source program
- ☒ Multi pass: compiler may have to keep entire program representation in memory

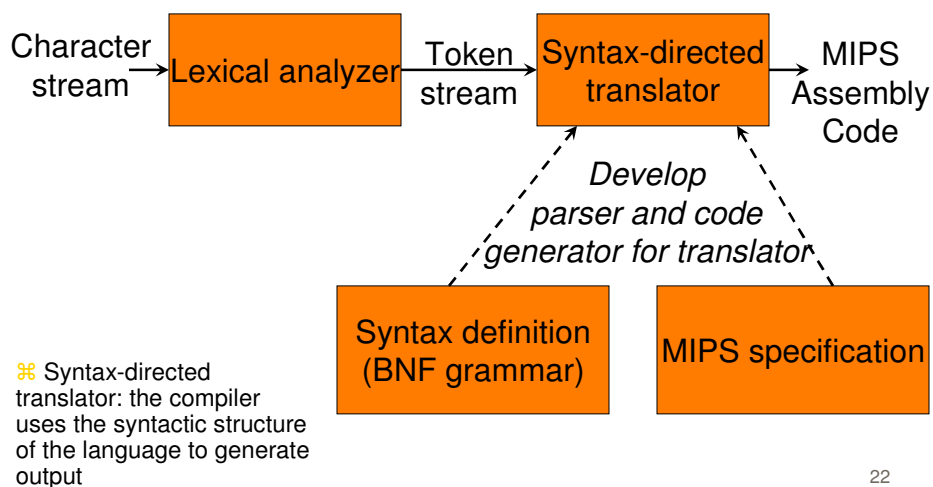
Compiler-Construction Tools

⌘ Software development tools are available to implement one or more compiler phases

- ☒ *Scanner generators*
- ☒ *Parser generators*
- ☒ *Syntax-directed translation engines*
- ☒ *Automatic code generators*
- ☒ *Data-flow engines*

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The Structure of our Compiler



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Syntax Definition

- ⌘ Context-free grammar is a 4-tuple with
 - ☒ A set of tokens (*terminal* symbols)
 - ☒ A set of *nonterminals*
 - ☒ A set of *productions*
 - ☒ A designated *start symbol*

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Example Grammar

Context-free grammar for simple expressions:

$$G = \langle \{list, digit\}, \{+, -, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}, P, list \rangle$$

with productions $P =$

$$list \rightarrow list + digit$$

$$list \rightarrow list - digit$$

$$list \rightarrow digit$$

$$digit \rightarrow 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9$$

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Derivation

⌘ Given a CF grammar we can determine the set of all *strings* (sequences of tokens) generated by the grammar using *derivation*

- ☒ We begin with the start symbol
- ☒ In each step, we replace one nonterminal in the current *sentential form* with one of the right-hand sides of a production for that nonterminal

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Derivation for the Example Grammar

$$\begin{aligned}
 & \textit{list} \\
 \Rightarrow & \underline{\textit{list}} + \textit{digit} \\
 \Rightarrow & \underline{\textit{list}} - \textit{digit} + \textit{digit} \\
 \Rightarrow & \underline{\textit{digit}} - \textit{digit} + \textit{digit} \\
 \Rightarrow & \mathbf{9} - \underline{\textit{digit}} + \textit{digit} \\
 \Rightarrow & \mathbf{9} - \mathbf{5} + \underline{\textit{digit}} \\
 \Rightarrow & \mathbf{9} - \mathbf{5} + \mathbf{2}
 \end{aligned}$$

This is an example *leftmost derivation*, because we replaced the leftmost nonterminal (underlined) in each step

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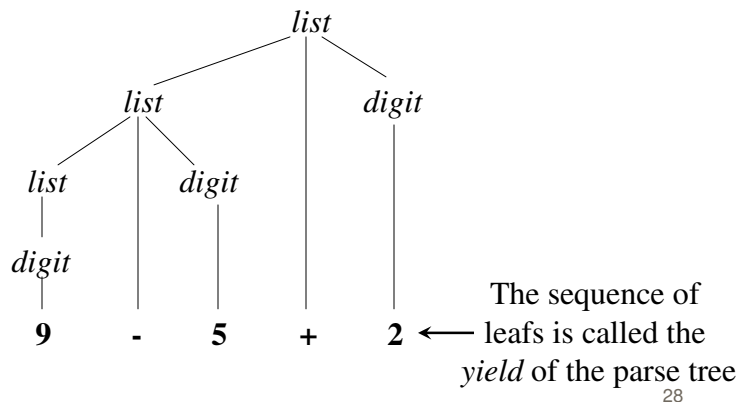
Parse Trees

- ⌘ The root of the tree is labeled by the start symbol
- ⌘ Each leaf of the tree is labeled by a terminal (=token) or ϵ (=empty)
- ⌘ Each interior node is labeled by a nonterminal
- ⌘ If $A \rightarrow X_1 X_2 \dots X_n$ is a production, then node A has children X_1, X_2, \dots, X_n where X_i is a (non)terminal or ϵ

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Parse Tree for the Example Grammar

Parse tree of the string **9-5+2** using grammar G



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Ambiguity

Consider the following context-free grammar:

$$G = \langle \{string\}, \{+,-,0,1,2,3,4,5,6,7,8,9\}, P, string \rangle$$

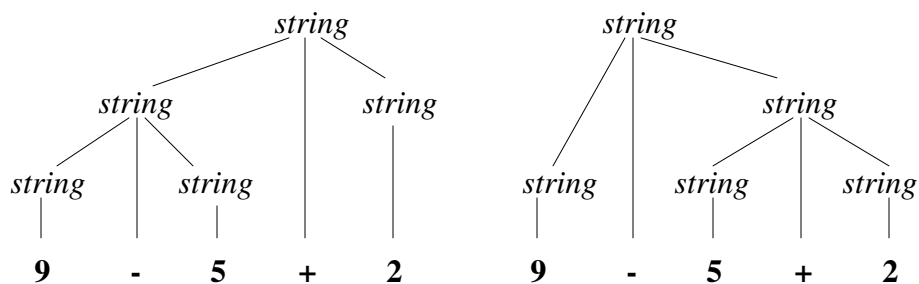
with production $P =$

$$string \rightarrow string + string \mid string - string \mid 0 \mid 1 \mid \dots \mid 9$$

This grammar is *ambiguous*, because more than one parse tree generates the string **9-5+2**

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Ambiguity (cont'd)



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Associativity of Operators

Left-associative operators have *left-recursive* productions

$$\textit{left} \rightarrow \textit{left} + \textit{term} \mid \textit{term}$$

String **a+b+c** has the same meaning as **(a+b)+c**

Right-associative operators have *right-recursive* productions

$$\textit{right} \rightarrow \textit{term} = \textit{right} \mid \textit{term}$$

String **a=b=c** has the same meaning as **a=(b=c)**

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Precedence of Operators

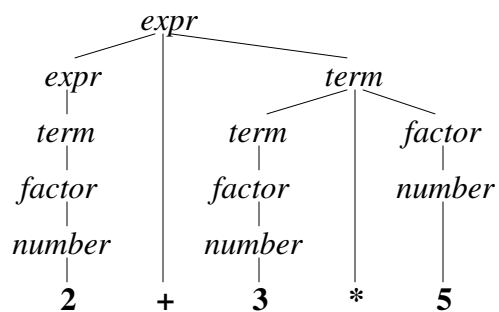
Operators with higher precedence “bind more tightly”

$$\textit{expr} \rightarrow \textit{expr} + \textit{term} \mid \textit{term}$$

$$\textit{term} \rightarrow \textit{term} * \textit{factor} \mid \textit{factor}$$

$$\textit{factor} \rightarrow \textit{number} \mid (\textit{expr})$$

String **2+3*5** has the same meaning as **2+(3*5)**



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Syntax of Statements

$$\begin{aligned}
 \text{stmt} &\rightarrow \text{id} := \text{expr} \\
 &\quad | \text{if } \text{expr} \text{ then } \text{stmt} \\
 &\quad | \text{if } \text{expr} \text{ then } \text{stmt} \text{ else } \text{stmt} \\
 &\quad | \text{while } \text{expr} \text{ do } \text{stmt} \\
 &\quad | \text{begin } \text{opt_stmts} \text{ end} \\
 \text{opt_stmts} &\rightarrow \text{stmt} ; \text{opt_stmts} \\
 &\quad | \varepsilon
 \end{aligned}$$

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Syntax-Directed Translation

- ⌘ Uses a CF grammar to specify the syntactic structure of the language
- ⌘ AND associates a set of *attributes* with (non)terminals
- ⌘ AND associates with each production a set of *semantic rules* for computing values for the attributes
- ⌘ The attributes contain the translated form of the input after the computations are completed

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Synthesized and Inherited Attributes

- ⌘ An attribute is said to be ...
 - ☒ *synthesized* if its value at a parse-tree node is determined from the attribute values at the children of the node
 - ☒ *inherited* if its value at a parse-tree node is determined by the parent (by enforcing the parent's semantic rules)

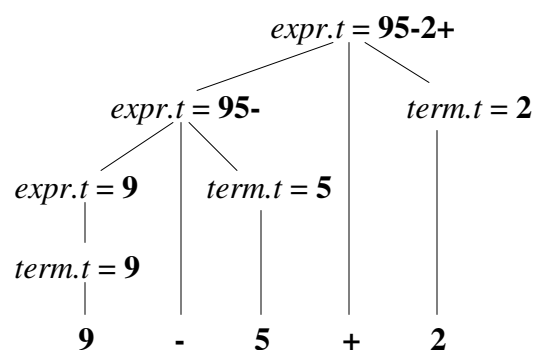
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Example Attribute Grammar

Production	Semantic Rule
$expr \rightarrow expr_1 + term$	$expr.t := expr_1.t \parallel term.t \parallel "+"$
$expr \rightarrow expr_1 - term$	$expr.t := expr_1.t \parallel term.t \parallel "-"$
$expr \rightarrow term$	$expr.t := term.t$
$term \rightarrow 0$	$term.t := "0"$
$term \rightarrow 1$	$term.t := "1"$
...	...
$term \rightarrow 9$	$term.t := "9"$

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Example Annotated Parse Tree



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Depth-First Traversals

```

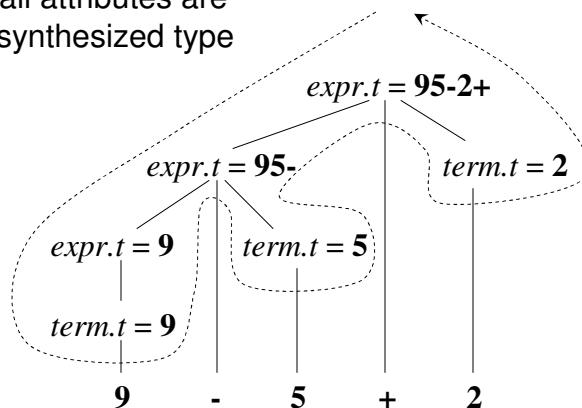
procedure visit(n : node);
begin
  for each child m of n, from left to right do
    visit(m);
  evaluate semantic rules at node n
end

```

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Depth-First Traversals (Example)

Note: all attributes are of the synthesized type



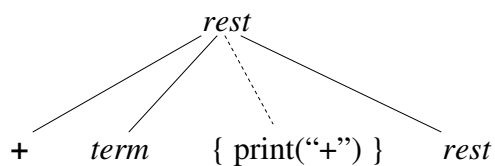
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Translation Schemes

⌘ A *translation scheme* is a CF grammar embedded with *semantic actions*

$$rest \rightarrow + term \{ \text{print}(\text{"+"}) \} rest$$

Embedded
semantic action



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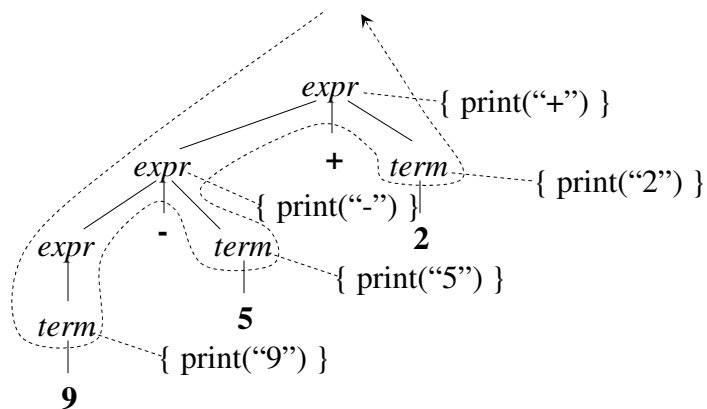
Example Translation Scheme

```

expr → expr + term  { print(“+”) }
expr → expr - term  { print(“-”) }
expr → term
term → 0              { print(“0”) }
term → 1              { print(“1”) }
...
term → 9              { print(“9”) }
    
```

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Example Translation Scheme (cont'd)



Translates 9-5+2 into postfix 95-2+₄₂

Parsing

- ⌘ Parsing = *process of determining if a string of tokens can be generated by a grammar*
- ⌘ For any CF grammar there is a parser that takes at most $O(n^3)$ time to parse a string of n tokens
- ⌘ Linear algorithms suffice for parsing programming language
- ⌘ *Top-down parsing* “constructs” parse tree from root to leaves
- ⌘ *Bottom-up parsing* “constructs” parse tree from leaves to root

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Predictive Parsing

- ⌘ *Recursive descent parsing* is a top-down parsing method
 - ☒ Every nonterminal has one (recursive) procedure responsible for parsing the nonterminal’s syntactic category of input tokens
 - ☒ When a nonterminal has multiple productions, each production is implemented in a branch of a selection statement based on input look-ahead information
- ⌘ *Predictive parsing* is a special form of recursive descent parsing where we use one lookahead token to unambiguously determine the parse operations

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Example Predictive Parser (Grammar)

```

type → simple
      | ^ id
      | array [ simple ] of type
simple → integer
      | char
      | num dotdot num
    
```

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Example Predictive Parser (Program Code)

```

procedure match(t : token);
begin
  if lookahead = t then
    lookahead := nexttoken()
  else error()
end;

procedure type();
begin
  if lookahead in { 'integer', 'char', 'num' } then
    simple()
  else if lookahead = '^' then
    match('^'); match(id)
  else if lookahead = 'array' then
    match('array'); match('['); simple();
    match(']'); match('of'); type()
  else error()
end;

procedure simple();
begin
  if lookahead = 'integer' then
    match('integer')
  else if lookahead = 'char' then
    match('char')
  else if lookahead = 'num' then
    match('num');
    match('dotdot');
    match('num')
  else error()
end;
    
```

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Example Predictive Parser (Execution Step 1)

Check *lookahead*
and call *match*

match('array')

type()

Input: array [num dotdot num] of integer

 ↑
 lookahead

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Example Predictive Parser (Execution Step 2)

match('array')

match('[')

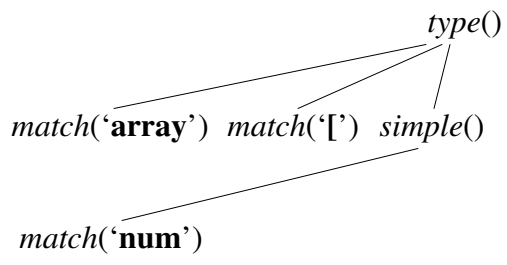
type()

Input: array [num dotdot num] of integer

 ↑
 lookahead

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Example Predictive Parser (Execution Step 3)

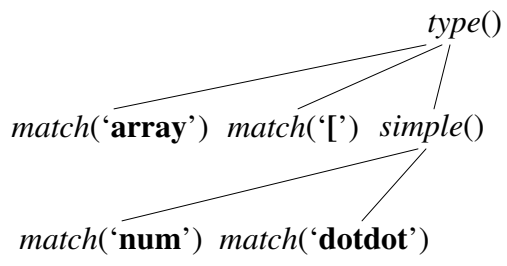


Input: array [num dotdot num] of integer

↑

lookahead

Example Predictive Parser (Execution Step 4)

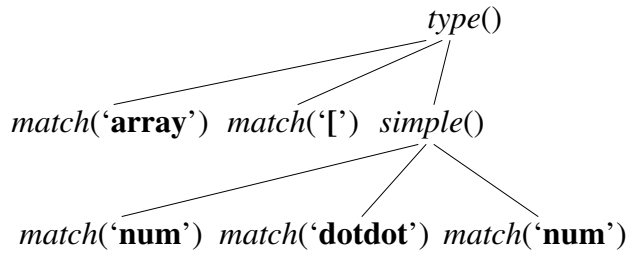


Input: array [num dotdot num] of integer

↑

lookahead

Example Predictive Parser (Execution Step 5)

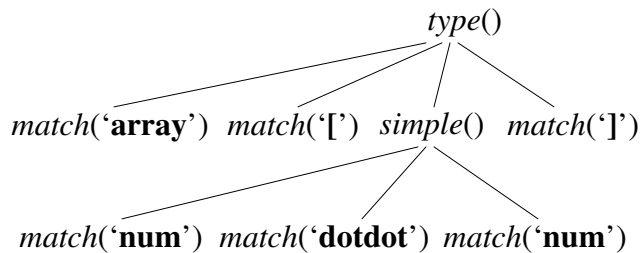


Input: array [num dotdot num] of integer

↑
lookahead

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Example Predictive Parser (Execution Step 6)

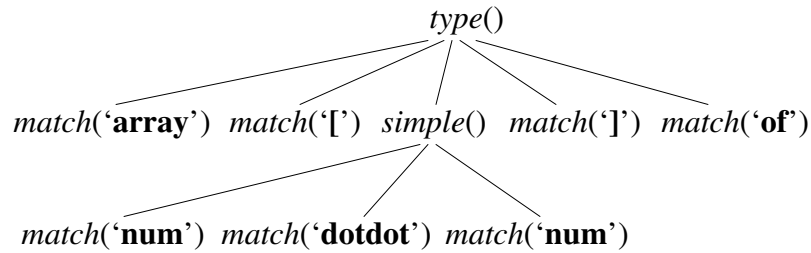


Input: array [num dotdot num] of integer

↑
lookahead

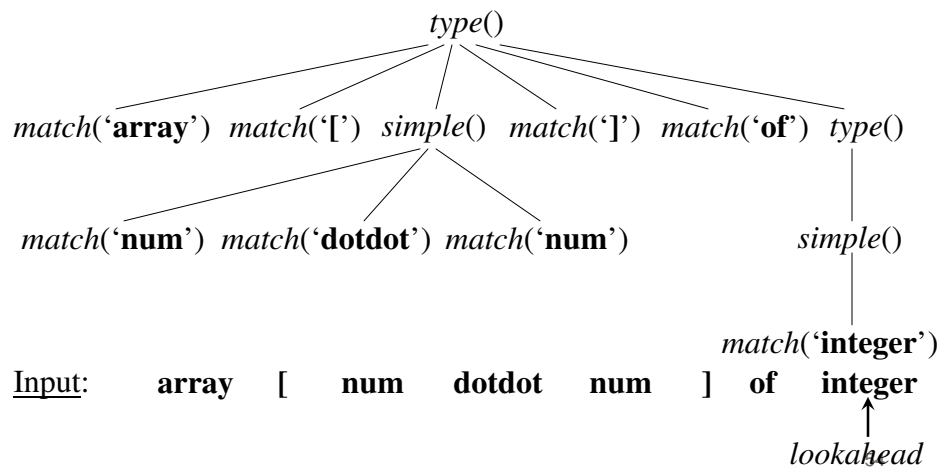
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Example Predictive Parser (Execution Step 7)



Input: **array** **[** **num** **dotdot** **num** **]** **of** **integer**
↑
lookahead 53

Example Predictive Parser (Execution Step 8)



Input: **array** **[** **num** **dotdot** **num** **]** **of** **integer**
↑
lookahead

FIRST

FIRST(α) is the set of terminals that appear as the first symbols of one or more strings generated from α

```

type → simple
      | ^ id
      | array [ simple ] of type
simple → integer
      | char
      | num dotdot num
    
```

```

FIRST(simple) = { integer, char, num }
FIRST(^ id) = { ^ }
FIRST(type) = { integer, char, num, ^, array }
    
```

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Using FIRST

We use FIRST to write a predictive parser as follows

```

expr → term rest
rest → + term rest
      | - term rest
      | ε
    
```

```

procedure rest();
begin
  if lookahead in FIRST(+ term rest) then
    match('+'); term(); rest()
  else if lookahead in FIRST(- term rest) then
    match('-'); term(); rest()
  else return
end;
    
```

When a nonterminal A has two (or more) productions as in

$$A \rightarrow \alpha$$

$$| \beta$$

Then FIRST(α) and FIRST(β) must be disjoint for predictive parsing to work

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Left Factoring

When more than one production for nonterminal A starts with the same symbols, the FIRST sets are not disjoint

$$\begin{aligned} stmt &\rightarrow \mathbf{if\ expr\ then\ stmt} \\ &\quad | \mathbf{if\ expr\ then\ stmt\ else\ stmt} \end{aligned}$$

We can use *left factoring* to fix the problem

$$\begin{aligned} stmt &\rightarrow \mathbf{if\ expr\ then\ stmt\ opt_else} \\ opt_else &\rightarrow \mathbf{else\ stmt} \\ &\quad | \epsilon \end{aligned}$$

Left factoring: if not clear what to choose, rewrite the production until we have seen enough to make a decision.

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Left Recursion

When a production for nonterminal A starts with a *self reference* then a predictive parser loops forever

$$\begin{aligned} A &\rightarrow A\ \alpha \\ &\quad | \beta \\ &\quad | \gamma \end{aligned}$$

We can eliminate *left recursive productions* by systematically rewriting the grammar using *right recursive productions*

$$\begin{aligned} A &\rightarrow \beta\ R \\ &\quad | \gamma\ R \\ R &\rightarrow \alpha\ R \\ &\quad | \epsilon \end{aligned}$$

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A Translator for Simple Expressions

```

expr → expr + term { print(“+”) }
expr → expr - term { print(“-”) }
expr → term
term → 0 { print(“0”) }
term → 1 { print(“1”) }
...
term → 9 { print(“9”) }
    
```

After left recursion elimination:

```

expr → term rest
rest → + term { print(“+”) } rest | - term { print(“-”) } rest | ε
term → 0 { print(“0”) }
term → 1 { print(“1”) }
...
term → 9 { print(“9”) }
    
```

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	<pre> main() { lookahead = getchar(); expr(); } expr() { term(); while (1) /* optimized by inlining rest() and removing recursive calls */ { if (lookahead == '+') { match('+'); term(); putchar('+'); } else if (lookahead == '-') { match('-'); term(); putchar('-'); } else break; } } term() { if (isdigit(lookahead)) { putchar(lookahead); match(lookahead); } else error(); } match(int t) { if (lookahead == t) { lookahead = getchar(); } else error(); } error() { printf("Syntax error\n"); exit(1); } </pre>
<i>expr</i> → <i>term rest</i>	}
<i>rest</i> → + <i>term</i> { print(“+”) } <i>rest</i> - <i>term</i> { print(“-”) } <i>rest</i> ε	
<i>term</i> → 0 { print(“0”) } <i>term</i> → 1 { print(“1”) } ... <i>term</i> → 9 { print(“9”) }	

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Lexical Analysis

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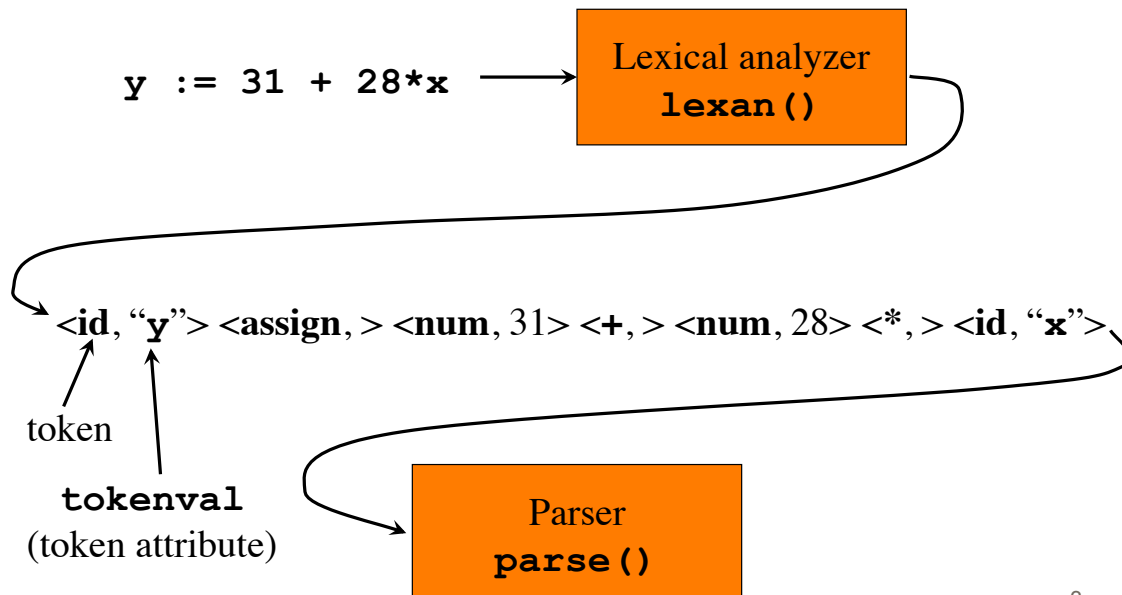
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Adding a Lexical Analyzer

- Typical tasks of the lexical analyzer:
 - Remove white space and comments
 - Encode constants as tokens
 - Recognize keywords
 - Recognize identifiers

2

The Lexical Analyzer



3

Token Attributes

```
factor → ( expr )  
        | num { print(num.value) }
```

```
#define NUM 256 /* token returned by lexan */
```

```
factor()  
{  
  if (lookahead == '(')  
  {  
    match('('); expr(); match(')');  
  }  
  else if (lookahead == NUM)  
  {  
    printf(" %d ", tokenval); match(NUM);  
  }  
  else error();  
}
```

4

Symbol Table

The symbol table is globally accessible (to all phases of the compiler)

Each entry in the symbol table contains a string and a token value:

```
struct entry
{   char *lexptr; /* lexeme (string) */
    int token;
};
struct entry symtable[];
```

`insert(s, t)`: returns array index to new entry for string **s** token **t**

`lookup(s)`: returns array index to entry for string **s** or 0

Possible implementations: - simple C code (see textbook) - hashtables

5

Identifiers

$$\textit{factor} \rightarrow (\textit{expr})$$

| **id** { print(**id**.string) }

```
#define ID 259 /* token returned by lexan() */

factor()
{   if (lookahead == '(')
    {   match('('); expr(); match(')');
    }
    else if (lookahead == ID)
    {   printf(" %s ", symtable[tokenval].lexptr);
        match(NUM);
    }
    else error();
}
```

6

Handling Reserved Keywords

We simply initialize the global symbol table with the set of keywords

```
/* global.h */
#define DIV 257 /* token */
#define MOD 258 /* token */
#define ID 259 /* token */

/* init.c */
insert("div", DIV);
insert("mod", MOD);

/* lexer.c */
int lexan()
{
    ...
    tokenval = lookup(lexbuf);
    if (tokenval == 0)
        tokenval = insert(lexbuf, ID);
    return symtable[p].token;
}
```

7

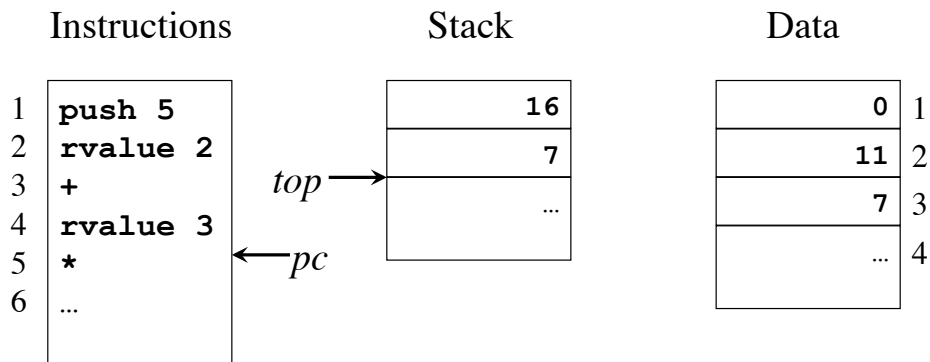
Handling Reserved Keywords (cont'd)

morefactors → **div** *factor* { print('DIV') } *morefactors*
| **mod** *factor* { print('MOD') } *morefactors*
| ...

```
/* parser.c */
morefactors()
{
    if (lookahead == DIV)
    {
        match(DIV); factor(); printf("DIV"); morefactors();
    }
    else if (lookahead == MOD)
    {
        match(MOD); factor(); printf("MOD"); morefactors();
    }
    else
        ...
}
```

8

Abstract Stack Machines



9

Generic Instructions for Stack Manipulation

<code>push v</code>	push constant value v onto the stack
<code>rvalue l</code>	push contents of data location l
<code>lvalue l</code>	push address of data location l
<code>pop</code>	discard value on top of the stack
<code>:=</code>	the r-value on top is placed in the l-value below it and both are popped
<code>copy</code>	push a copy of the top value on the stack
<code>+</code>	add value on top with value below it pop both and push result
<code>-</code>	subtract value on top from value below it pop both and push result
<code>*, /, ...</code>	ditto for other arithmetic operations
<code><, &, ...</code>	ditto for relational and logical operations

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Generic Control Flow Instructions

label l	label instruction with l
goto l	jump to instruction labeled l
gofalse l	pop the top value, if zero then jump to l
gotrue l	pop the top value, if nonzero then jump to l
halt	stop execution
jsr l	jump to subroutine labeled l , push return address
return	pop return address and return to caller

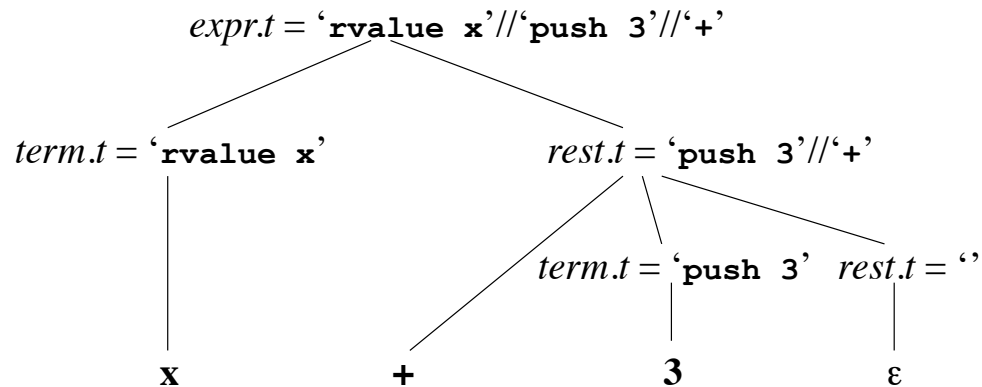
11

Syntax-Directed Translation of Expressions

$expr \rightarrow term\ rest \{ expr.t := term.t \parallel rest.t \}$
 $rest \rightarrow +\ term\ rest_1 \{ rest.t := term.t \parallel '+' \parallel rest_1.t \}$
 $rest \rightarrow -\ term\ rest_1 \{ rest.t := term.t \parallel '-' \parallel rest_1.t \}$
 $rest \rightarrow \epsilon \{ rest.t := '' \}$
 $term \rightarrow \mathbf{num} \{ term.t := 'push' \parallel \mathbf{num.value} \}$
 $term \rightarrow \mathbf{id} \{ term.t := 'rvalue' \parallel \mathbf{id.lexeme} \}$

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Syntax-Directed Translation of Expressions (cont'd)



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Translation Scheme to Generate Abstract Machine Code

```
expr → term moreterms
moreterms → + term { print( '+' ) } moreterms
moreterms → - term { print( '-' ) } moreterms
moreterms → ε
term → factor morefactors
morefactors → * factor { print( '*' ) } morefactors
morefactors → div factor { print( 'DIV' ) } morefactors
morefactors → mod factor { print( 'MOD' ) } morefactors
morefactors → ε
factor → ( expr )
factor → num { print( 'push ' // num.value ) }
factor → id { print( 'rvalue ' // id.lexeme ) }
```

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Translation Scheme to Generate Abstract Machine Code (cont'd)

$stmt \rightarrow id := \{ \text{print('lvalue ' // id.lexeme)} \} expr \{ \text{print(' :=')} \}$

<code>lvalue id.lexeme</code>
code for <i>expr</i>
<code>:=</code>

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Translation Scheme to Generate Abstract Machine Code (cont'd)

$stmt \rightarrow \text{if } expr \{ \text{out} := \text{newlabel}(); \text{print('gofalse ' // out)} \}$
 $\quad \text{then } stmt \{ \text{print('label ' // out)} \}$

code for <i>expr</i>
<code>gofalse out</code>
code for <i>stmt</i>
<code>label out</code>

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Translation Scheme to Generate Abstract Machine Code (cont'd)

```
stmt → while { test := newlabel(); print('label ' // test) }  
      expr { out := newlabel(); print('gofalse ' // out) }  
      do stmt { print('goto ' // test // 'label ' // out) }
```

label <i>test</i>
code for <i>expr</i>
gofalse <i>out</i>
code for <i>stmt</i>
goto <i>test</i>
label <i>out</i>

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Translation Scheme to Generate Abstract Machine Code (cont'd)

```
start → stmt { print('halt') }  
stmt → begin opt_stmts end  
opt_stmts → stmt ; opt_stmts | ε
```

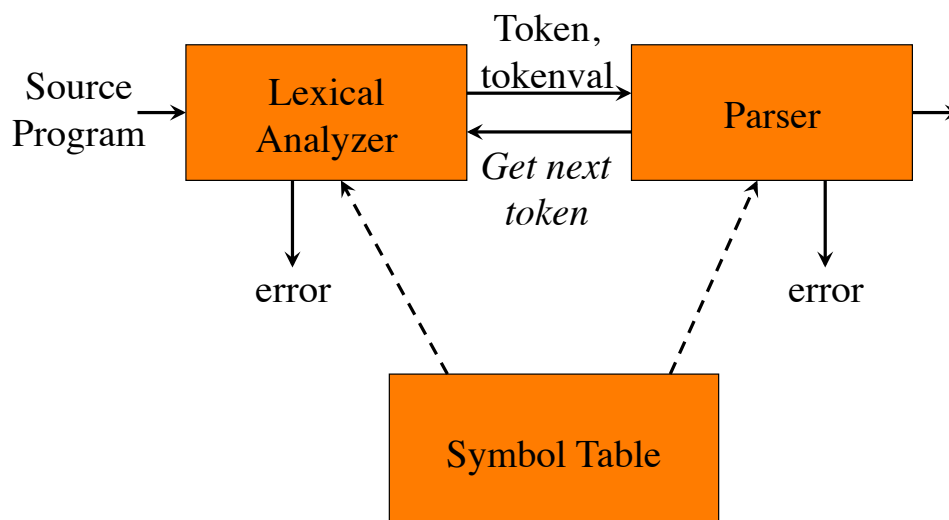
18

The Reason Why Lexical Analysis is a Separate Phase

- Simplifies the design of the compiler
- Provides efficient implementation
 - Systematic techniques to implement lexical analyzers by hand or automatically
 - Stream buffering methods to scan input
- Improves portability
 - Non-standard symbols and alternate character encodings can be more easily translated

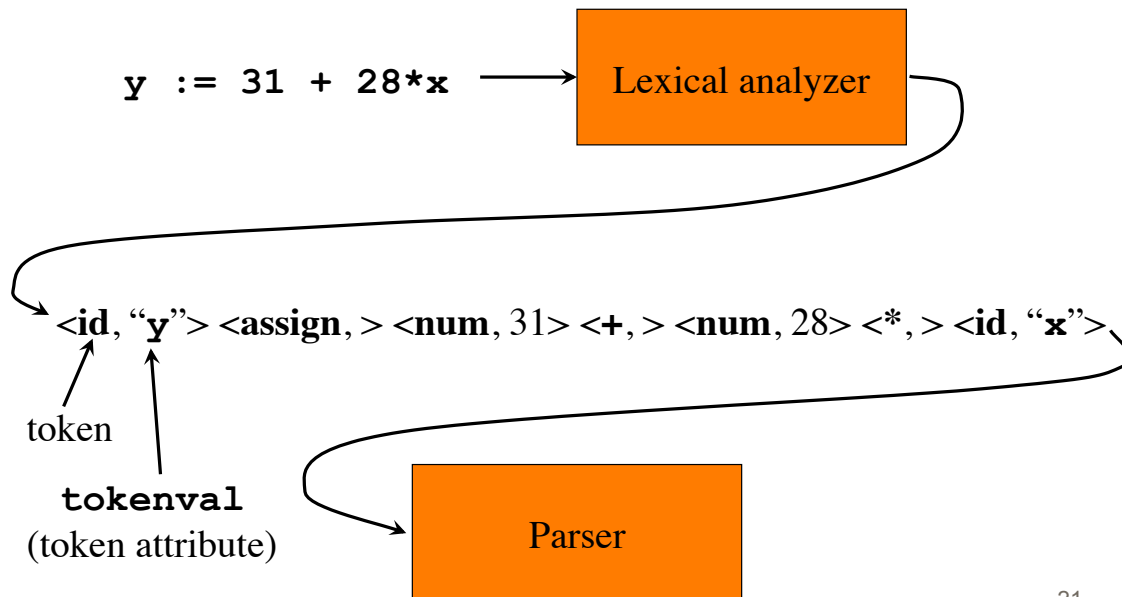
19

Interaction of the Lexical Analyzer with the Parser



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Attributes of Tokens



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Tokens, Patterns, and Lexemes

- A *token* is a classification of lexical units
 - For example: **id** and **num**
- *Lexemes* are the specific character strings that make up a token
 - For example: `abc` and `123`
- *Patterns* are rules describing the set of lexemes belonging to a token
 - For example: "*letter followed by letters and digits*" and "*non-empty sequence of digits*"

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Specification of Patterns for Tokens: Terminology

- An *alphabet* Σ is a finite set of symbols (characters)
- A *string* s is a finite sequence of symbols from Σ
 - $|s|$ denotes the length of string s
 - ε denotes the empty string, thus $|\varepsilon| = 0$
- A *language* is a specific set of strings over some fixed alphabet Σ

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Specification of Patterns for Tokens: String Operations

- The *concatenation* of two strings x and y is denoted by xy
- The *exponentiation* of a string s is defined by
$$s^0 = \varepsilon$$
$$s^i = s^{i-1}s \text{ for } i > 0$$
(note that $s\varepsilon = \varepsilon s = s$)

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Specification of Patterns for Tokens: Language Operations

- *Union*

$$L \cup M = \{s \mid s \in L \text{ or } s \in M\}$$

- *Concatenation*

$$LM = \{xy \mid x \in L \text{ and } y \in M\}$$

- *Exponentiation*

$$L^0 = \{\varepsilon\}; L^i = L^{i-1}L$$

- *Kleene closure*

$$L^* = \bigcup_{i=0, \dots, \infty} L^i$$

- *Positive closure*

$$L^+ = \bigcup_{i=1, \dots, \infty} L^i$$

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Specification of Patterns for Tokens: Regular Expressions

- *Basis symbols:*

- ε is a regular expression denoting language $\{\varepsilon\}$

- $a \in \Sigma$ is a regular expression denoting $\{a\}$

- If r and s are regular expressions denoting languages $L(r)$ and $M(s)$ respectively, then

- $r \mid s$ is a regular expression denoting $L(r) \cup M(s)$

- rs is a regular expression denoting $L(r)M(s)$

- r^* is a regular expression denoting $L(r)^*$

- (r) is a regular expression denoting $L(r)$

- A language defined by a regular expression is called a *regular set*

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Specification of Patterns for Tokens: Regular Definitions

- Naming convention for regular expressions:

$$d_1 \rightarrow r_1$$
$$d_2 \rightarrow r_2$$

...

$$d_n \rightarrow r_n$$

where r_i is a regular expression over

$$\Sigma \cup \{d_1, d_2, \dots, d_{i-1}\}$$

- Each d_j in r_i is textually substituted in r_i

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Specification of Patterns for Tokens: Regular Definitions

- Example:

letter \rightarrow **A** | **B** | ... | **Z** | **a** | **b** | ... | **z**

digit \rightarrow **0** | **1** | ... | **9**

id \rightarrow **letter** (**letter** | **digit**)*

- Cannot use recursion, this is illegal:

digits \rightarrow **digit digits** | **digit**

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Specification of Patterns for Tokens: Notational Shorthands

- We frequently use the following shorthands:

$$r^+ = rr^*$$

$$r? = r \mid \varepsilon$$

$$[a-z] = a \mid b \mid c \mid \dots \mid z$$

- For example:

digit \rightarrow $[0-9]$

num \rightarrow **digit**⁺ (**.** **digit**⁺)? (**E** (**+** | **-**)? **digit**⁺)?

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Regular Definitions and Grammars

Grammar

stmt \rightarrow **if** *expr* **then** *stmt*
| **if** *expr* **then** *stmt* **else** *stmt*
| ε

expr \rightarrow *term* **relop** *term*
| *term*

term \rightarrow **id**
| **num**

Regular definitions

if \rightarrow **if**

then \rightarrow **then**

else \rightarrow **else**

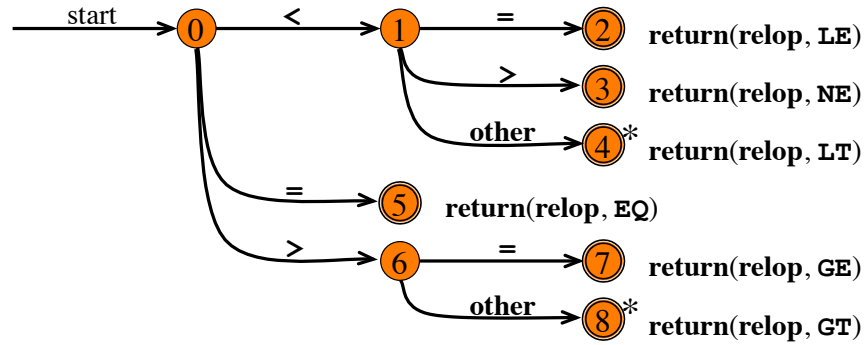
relop \rightarrow **<** | **<=** | **<>** | **>** | **>=** | **=**

id \rightarrow **letter** (**letter** | **digit**)*

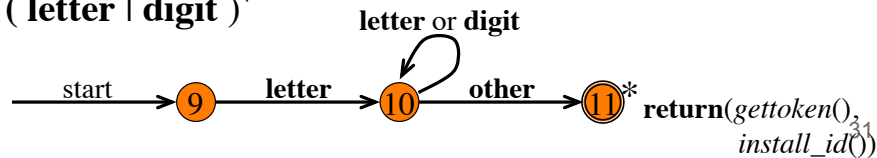
num \rightarrow **digit**⁺ (**.** **digit**⁺)? (**E** (**+** | **-**)? **digit**⁺)?

Implementing a Scanner Using Transition Diagrams

relop → < | <= | <> | > | >= | =



id → letter (letter | digit)*



Implementing a Scanner Using Transition Diagrams (Code)

```

token nexttoken()
{ while (1) {
  switch (state) {
    case 0: c = nextchar();
      if (c==blank || c==tab || c==newline) {
        state = 0;
        lexeme_beginning++;
      }
      else if (c=='<') state = 1;
      else if (c=='=') state = 5;
      else if (c=='>') state = 6;
      else state = fail();
      break;
    case 1:
      ...
    case 9: c = nextchar();
      if (isletter(c)) state = 10;
      else state = fail();
      break;
    case 10: c = nextchar();
      if (isletter(c)) state = 10;
      else if (isdigit(c)) state = 10;
      else state = 11;
      break;
  }
}
}

```

Decides what other start state is applicable



```

int fail()
{ forward = token_beginning;
  with (start) {
    case 0: start = 9; break;
    case 9: start = 12; break;
    case 12: start = 20; break;
    case 20: start = 25; break;
    case 25: recover(); break;
    default: /* error */
  }
  return start;
}

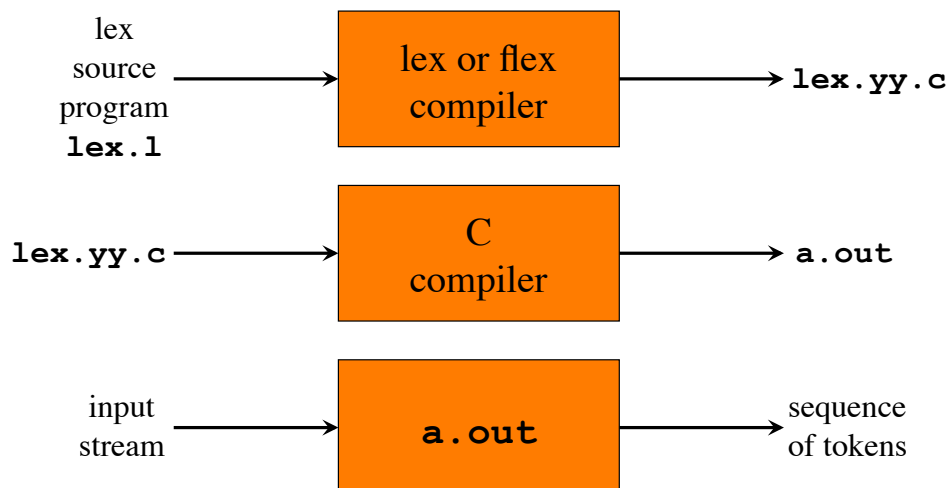
```

The Lex and Flex Scanner Generators

- *Lex* and its newer cousin *flex* are scanner generators
- Systematically translate regular definitions into C source code for efficient scanning
- Generated code is easy to integrate in C applications

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Creating a Lexical Analyzer with Lex and Flex



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Lex Specification

- A *lex specification* consists of three parts:
 - regular definitions, C declarations in* `% { % }`
`%%`
 - translation rules*
`%%`
 - user-defined auxiliary procedures*
- The *translation rules* are of the form:
 - $p_1 \{ \text{action}_1 \}$
 - $p_2 \{ \text{action}_2 \}$
 - ...
 - $p_n \{ \text{action}_n \}$

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Regular Expressions in Lex

x	match the character x
\.	match the character .
"string"	match contents of string of characters
.	match any character except newline
^	match beginning of a line
\$	match the end of a line
[xyz]	match one character x , y , or z (use \ to escape -)
[^xyz]	match any character except x , y , and z
[a-z]	match one of a to z
r*	closure (match zero or more occurrences)
r+	positive closure (match one or more occurrences)
r?	optional (match zero or one occurrence)
r₁r₂	match r₁ then r₂ (concatenation)
r₁ r₂	match r₁ or r₂ (union)
(r)	grouping
r₁\r₂	match r₁ when followed by r₂
{d}	match the regular expression defined by d

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Example Lex Specification 1

Translation rules

```
%{
#include <stdio.h>
}%
%%
[0-9]+ { printf("%s\n", yytext); }
.|\\n  { }
%%
main()
{ yylex();
}
```

Contains the matching lexeme

Invokes the lexical analyzer

```
lex spec.1
gcc lex.yy.c -ll
./a.out < spec.1
```

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Example Lex Specification 2

Translation rules

```
%{
#include <stdio.h>
int ch = 0, wd = 0, nl = 0;
}%
%%
delim    [ \t]+
%%
\\n      { ch++; wd++; nl++; }
^{delim} { ch+=yy leng; }
{delim}  { ch+=yy leng; wd++; }
.        { ch++; }
%%
main()
{ yylex();
  printf("%8d%8d%8d\n", nl, wd, ch);
}
```

Regular definition

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Example Lex Specification 3

```

%{
#include <stdio.h>
%}
digit      [0-9]
letter     [A-Za-z]
id         {letter}({letter}|{digit})*
%%
{digit}+  { printf("number: %s\n", yytext); }
{id}      { printf("ident: %s\n", yytext); }
.         { printf("other: %s\n", yytext); }
%%
main()
{ yylex();
}

```

Translation rules

Regular definitions

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Example Lex Specification 4

```

%{ /* definitions of manifest constants */
#define LT (256)
...
%}
delim     [ \t\n]
ws        {delim}+
letter    [A-Za-z]
digit     [0-9]
id        {letter}({letter}|{digit})*
number    {digit}+(\.{digit}+)?(E[+\-]?{digit}+)?
%%
{ws}      { }
if        {return IF;}
then      {return THEN;}
else      {return ELSE;}
{id}      {yylval = install_id(); return ID;}
{number}  {yylval = install_num(); return NUMBER;}
"<"      {yylval = LT; return RELOP;}
"<="     {yylval = LE; return RELOP;}
"="       {yylval = EQ; return RELOP;}
"<>"     {yylval = NE; return RELOP;}
">"      {yylval = GT; return RELOP;}
">="     {yylval = GE; return RELOP;}
%%
int install_id()
...

```

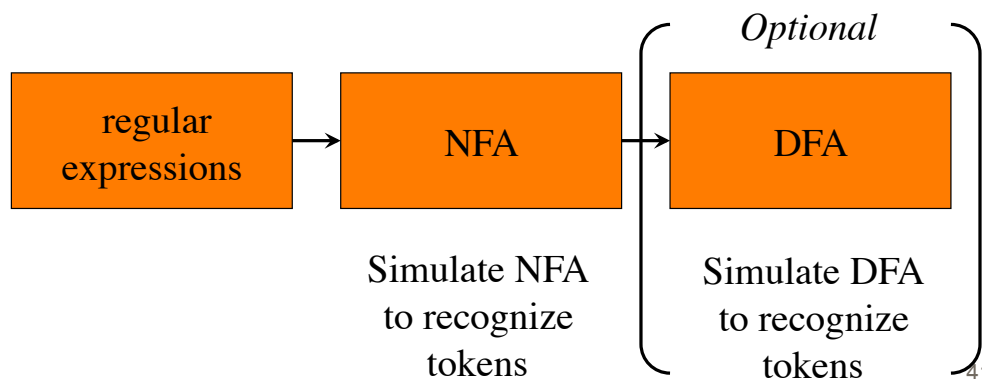
Return token to parser

Token attribute

Install **yytext** as identifier in symbol table

Design of a Lexical Analyzer Generator

- Translate regular expressions to NFA
- Translate NFA to an efficient DFA



Nondeterministic Finite Automata

- Definition: an NFA is a 5-tuple $(S, \Sigma, \delta, s_0, F)$ where

S is a finite set of *states*

Σ is a finite set of *input symbol alphabet*

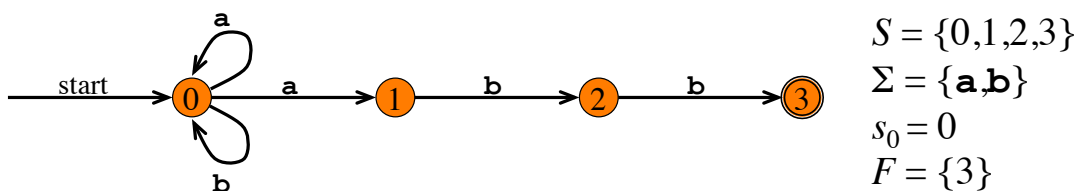
δ is a *mapping* from $S \times \Sigma$ to a set of states

$s_0 \in S$ is the *start state*

$F \subseteq S$ is the set of *accepting (or final) states*

Transition Graph

- An NFA can be diagrammatically represented by a labeled directed graph called a *transition graph*



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Transition Table

- The mapping δ of an NFA can be represented in a *transition table*

$\delta(0,a) = \{0,1\}$
 $\delta(0,b) = \{0\}$
 $\delta(1,b) = \{2\}$
 $\delta(2,b) = \{3\}$

State	Input a	Input b
0	{0, 1}	{0}
1		{2}
2		{3}

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The Language Defined by an NFA

- An NFA *accepts* an input string x **iff** there is some path with edges labeled with symbols from x in sequence from the start state to some accepting state in the transition graph
- A state transition from one state to another on the path is called a *move*
- The *language defined* by an NFA is the set of input strings it accepts, such as $(a|b)^*abb$ for the example NFA

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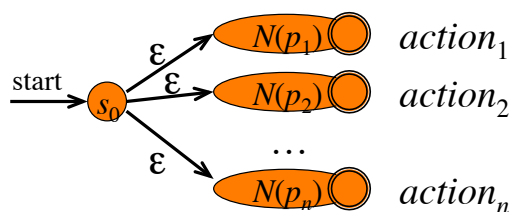
Design of a Lexical Analyzer Generator: RE to NFA to DFA

Lex specification with regular expressions

p_1 $\{ action_1 \}$
 p_2 $\{ action_2 \}$
...
 p_n $\{ action_n \}$



NFA

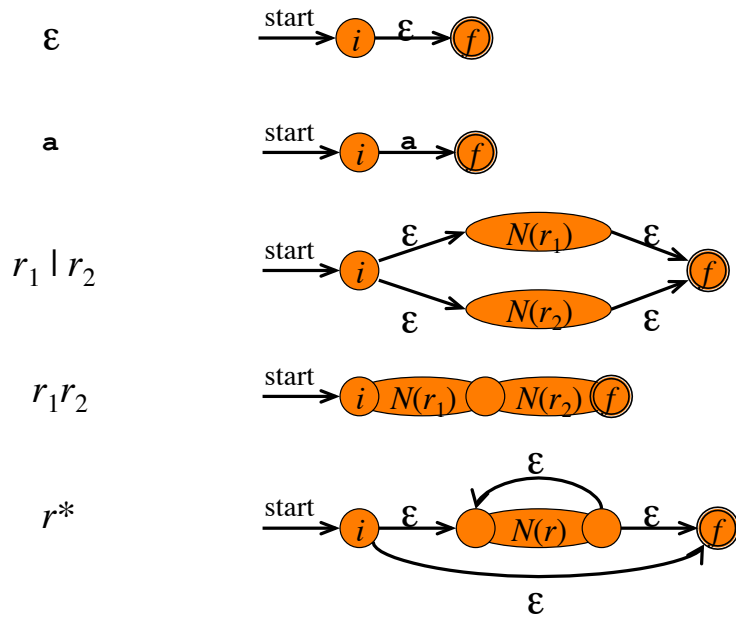


↓ Subset construction (optional)

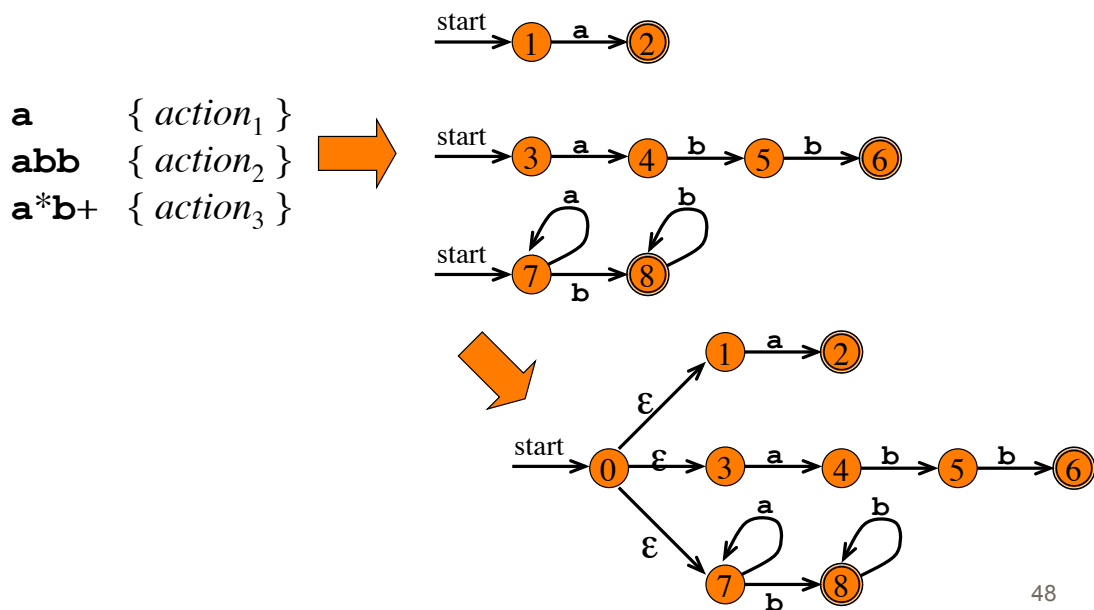
DFA

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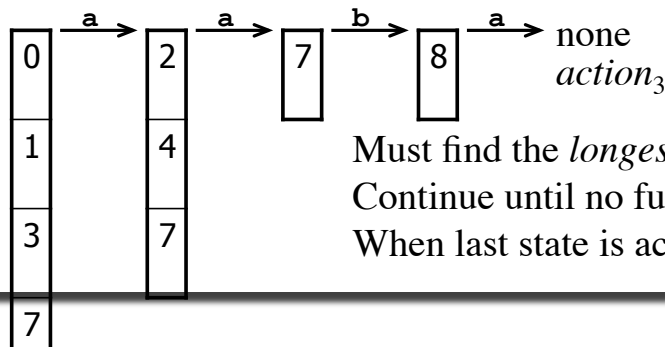
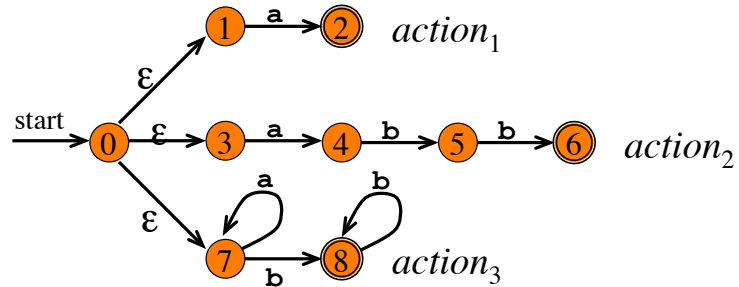
From Regular Expression to NFA (Thompson's Construction)



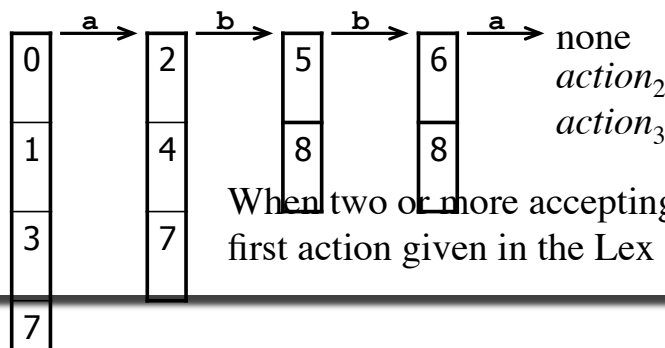
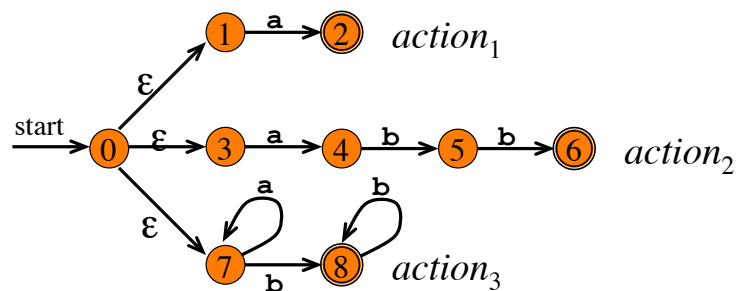
Combining the NFAs of a Set of Regular Expressions



Simulating the Combined NFA Example 1



Simulating the Combined NFA Example 2



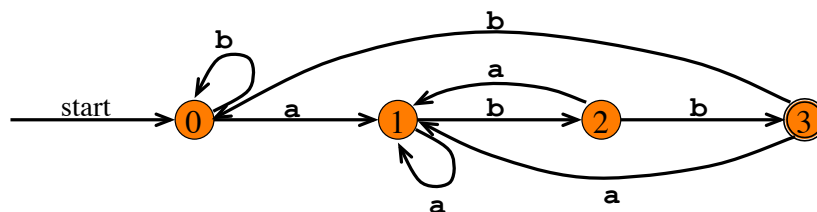
Deterministic Finite Automata

- A *deterministic finite automaton* is a special case of an NFA
 - No state has an ϵ -transition
 - For each state s and input symbol a there is at most one edge labeled a leaving s
- Each entry in the transition table is a single state
 - At most one path exists to accept a string
 - Simulation algorithm is simple

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Example DFA

A DFA that accepts $(ab)^*abb$



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Conversion of an NFA into a DFA

- The *subset construction algorithm* converts an NFA into a DFA using:

$$\varepsilon\text{-closure}(s) = \{s\} \cup \{t \mid s \xrightarrow{\varepsilon} \dots \xrightarrow{\varepsilon} t\}$$

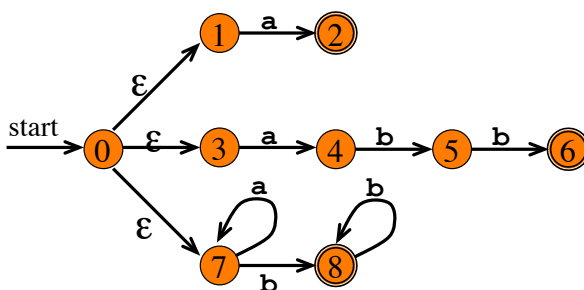
$$\varepsilon\text{-closure}(T) = \bigcup_{s \in T} \varepsilon\text{-closure}(s)$$

$$\text{move}(T, a) = \{t \mid s \xrightarrow{a} t \text{ and } s \in T\}$$

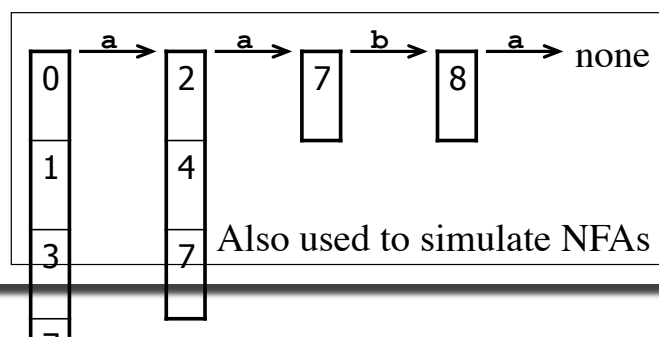
- The algorithm produces:
 - $Dstates$ is the set of states of the new DFA consisting of sets of states of the NFA
 - $Dtran$ is the transition table of the new DFA

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ε -closure and move Examples



$\varepsilon\text{-closure}(\{0\}) = \{0,1,3,7\}$
 $\text{move}(\{0,1,3,7\}, \mathbf{a}) = \{2,4,7\}$
 $\varepsilon\text{-closure}(\{2,4,7\}) = \{2,4,7\}$
 $\text{move}(\{2,4,7\}, \mathbf{a}) = \{7\}$
 $\varepsilon\text{-closure}(\{7\}) = \{7\}$
 $\text{move}(\{7\}, \mathbf{b}) = \{8\}$
 $\varepsilon\text{-closure}(\{8\}) = \{8\}$
 $\text{move}(\{8\}, \mathbf{a}) = \emptyset$



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Simulating an NFA using ϵ -closure and *move*

```
 $S := \epsilon\text{-closure}(\{s_0\})$   
 $S_{prev} := \emptyset$   
 $a := \text{nextchar}()$   
while  $S \neq \emptyset$  do  
     $S_{prev} := S$   
     $S := \epsilon\text{-closure}(\text{move}(S,a))$   
     $a := \text{nextchar}()$   
end do  
if  $S_{prev} \cap F \neq \emptyset$  then  
    execute action in  $S_{prev}$   
    return “yes”  
else    return “no”
```

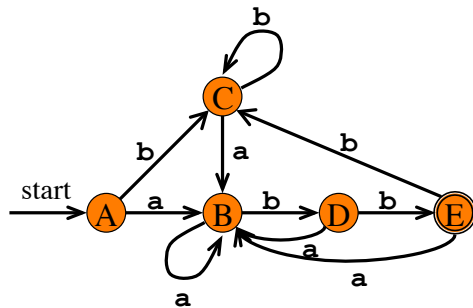
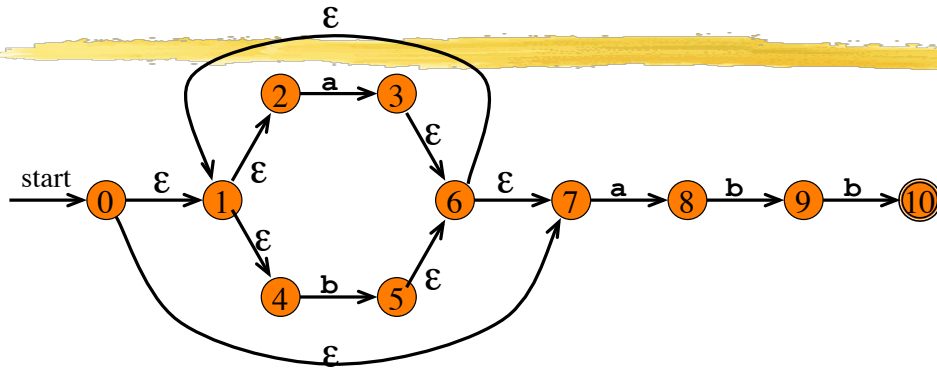
55

The Subset Construction Algorithm

Initially, $\epsilon\text{-closure}(s_0)$ is the only state in $Dstates$ and it is unmarked
while there is an unmarked state T in $Dstates$ **do**
 mark T
 for each input symbol $a \in \Sigma$ **do**
 $U := \epsilon\text{-closure}(\text{move}(T,a))$
 if U is not in $Dstates$ **then**
 add U as an unmarked state to $Dstates$
 end if
 $Dtran[T,a] := U$
 end do
end do

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Subset Construction Example 1



Dstates

A = {0,1,2,4,7}

B = {1,2,3,4,6,7,8}

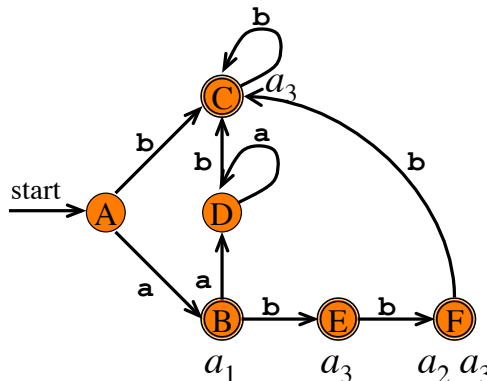
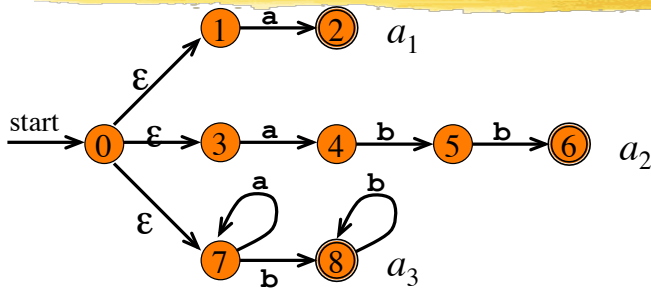
C = {1,2,4,5,6,7}

D = {1,2,4,5,6,7,9}

E = {1,2,4,5,6,7,10}

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Subset Construction Example 2



Dstates

A = {0,1,3,7}

B = {2,4,7}

C = {8}

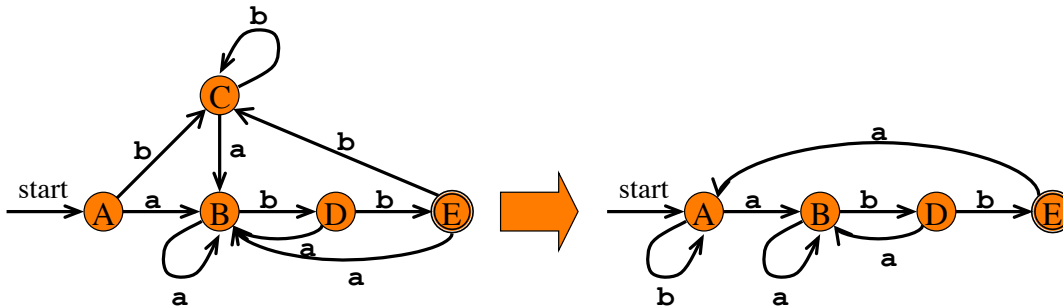
D = {7}

E = {5,8}

F = {6,8}

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Minimizing the Number of States of a DFA



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From Regular Expression to DFA Directly

- The *important states* of an NFA are those without an ϵ -transition, that is if $move(\{s\}, a) \neq \emptyset$ for some a then s is an important state
- The subset construction algorithm uses only the important states when it determines ϵ -closure($move(T, a)$)

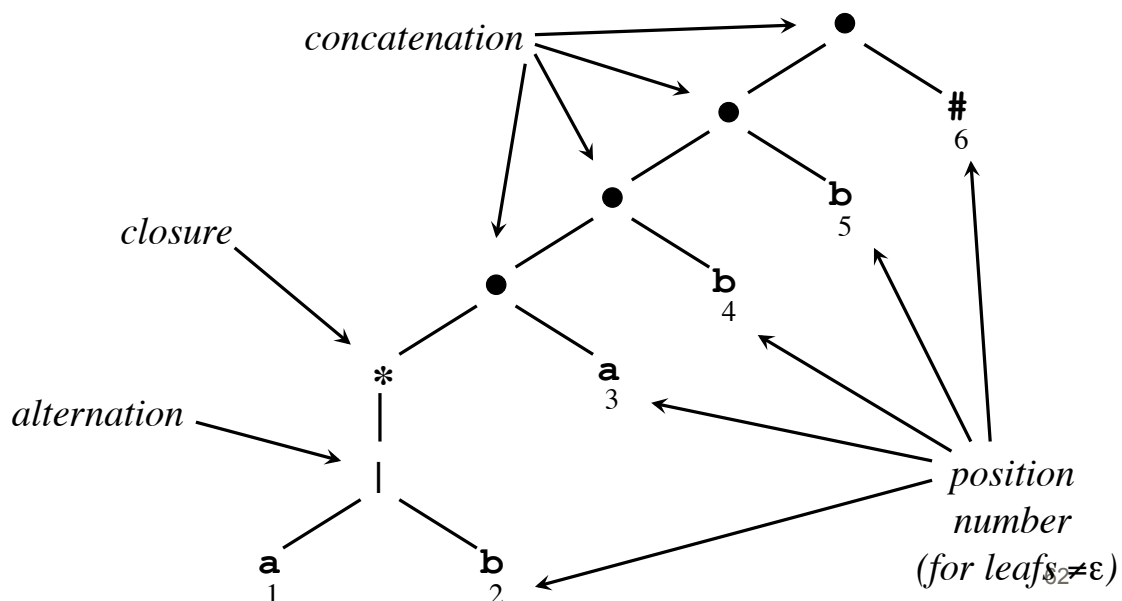
60

From Regular Expression to DFA Directly (Algorithm)

- Augment the regular expression r with a special end symbol $\#$ to make accepting states important: the new expression is $r\#$
- Construct a syntax tree for $r\#$
- Traverse the tree to construct functions *nullable*, *firstpos*, *lastpos*, and *followpos*

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From Regular Expression to DFA Directly: Syntax Tree of $(a|b)^*abb\#$



From Regular Expression to DFA Directly: Annotating the Tree

- $nullable(n)$: the subtree at node n generates languages including the empty string
- $firstpos(n)$: set of positions that can match the first symbol of a string generated by the subtree at node n
- $lastpos(n)$: the set of positions that can match the last symbol of a string generated by the subtree at node n
- $followpos(i)$: the set of positions that can follow position i in the tree

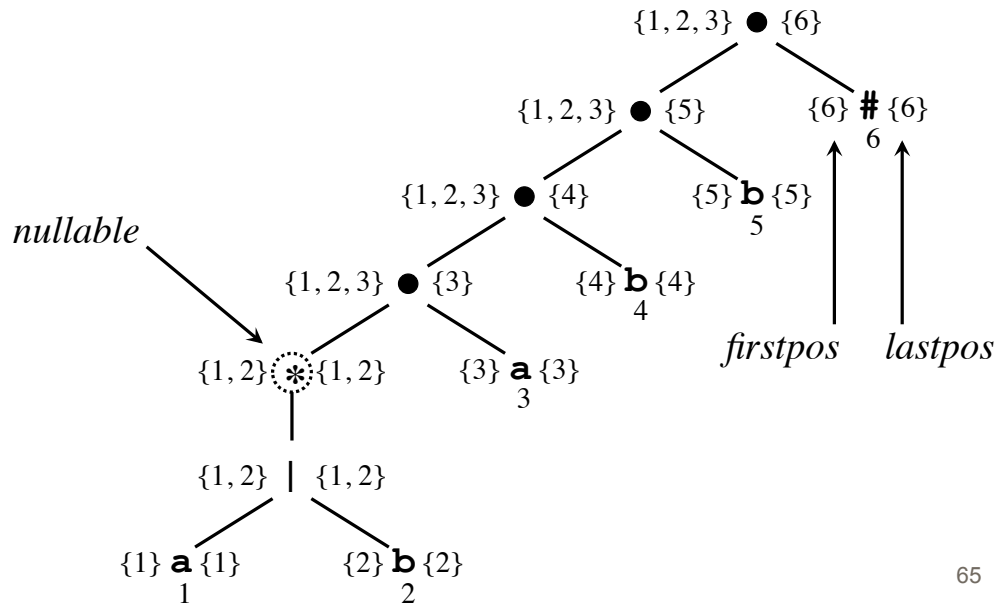
63

From Regular Expression to DFA Directly: Annotating the Tree

Node n	$nullable(n)$	$firstpos(n)$	$lastpos(n)$
Leaf ϵ	true	\emptyset	\emptyset
Leaf i	false	$\{i\}$	$\{i\}$
$\begin{array}{c} \\ / \quad \backslash \\ c_1 \quad c_2 \end{array}$	$nullable(c_1)$ or $nullable(c_2)$	$firstpos(c_1)$ \cup $firstpos(c_2)$	$lastpos(c_1)$ \cup $lastpos(c_2)$
$\begin{array}{c} \bullet \\ / \quad \backslash \\ c_1 \quad c_2 \end{array}$	$nullable(c_1)$ and $nullable(c_2)$	if $nullable(c_1)$ then $firstpos(c_1)$ \cup $firstpos(c_2)$ else $firstpos(c_1)$	if $nullable(c_2)$ then $lastpos(c_1)$ \cup $lastpos(c_2)$ else $lastpos(c_2)$
$\begin{array}{c} * \\ \\ c_1 \end{array}$	true	$firstpos(c_1)$	$lastpos(c_1)$

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From Regular Expression to DFA Directly: Syntax Tree of $(a|b)^*abb\#$



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From Regular Expression to DFA Directly: *followpos*

```

for each node  $n$  in the tree do
  if  $n$  is a cat-node with left child  $c_1$  and right child  $c_2$  then
    for each  $i$  in  $lastpos(c_1)$  do
       $followpos(i) := followpos(i) \cup firstpos(c_2)$ 
    end do
  else if  $n$  is a star-node
    for each  $i$  in  $lastpos(n)$  do
       $followpos(i) := followpos(i) \cup firstpos(n)$ 
    end do
  end if
end do

```

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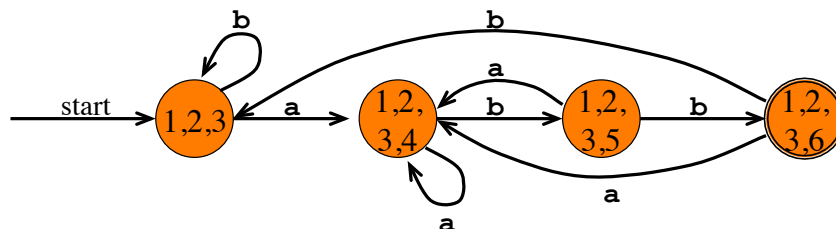
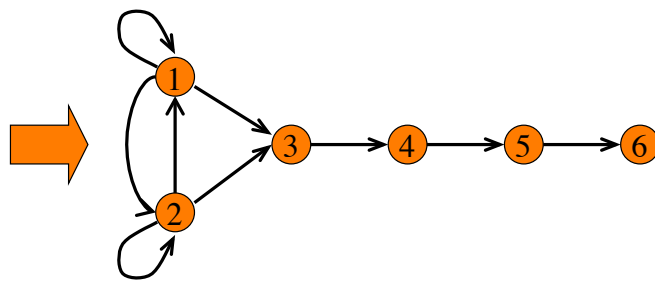
From Regular Expression to DFA Directly: Algorithm

$s_0 := \text{firstpos}(\text{root})$ where root is the root of the syntax tree
 $Dstates := \{s_0\}$ and is unmarked
while there is an unmarked state T in $Dstates$ **do**
 mark T
 for each input symbol $a \in \Sigma$ **do**
 let U be the set of positions that are in $\text{followpos}(p)$
 for some position p in T ,
 such that the symbol at position p is a
 if U is not empty and not in $Dstates$ **then**
 add U as an unmarked state to $Dstates$
 end if
 $Dtran[T,a] := U$
 end do
end do

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From Regular Expression to DFA Directly: Example

Node	<i>followpos</i>
1	{1, 2, 3}
2	{1, 2, 3}
3	{4}
4	{5}
5	{6}
6	-



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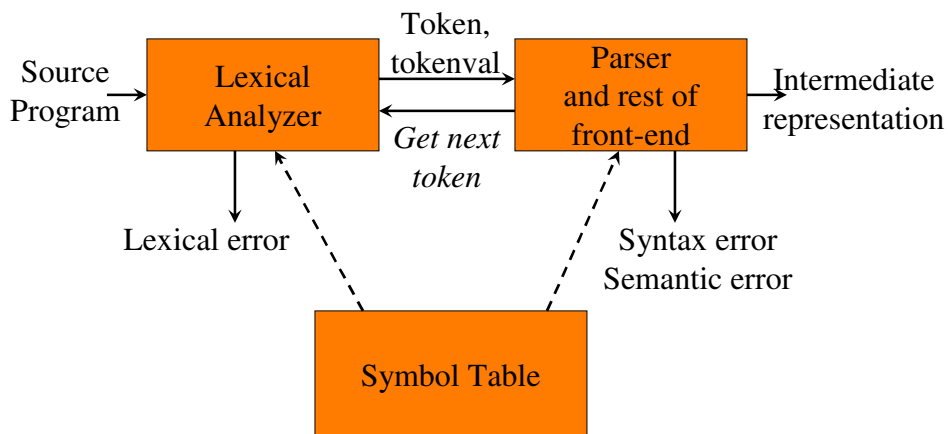
Time-Space Tradeoffs

<i>Automaton</i>	<i>Space (worst case)</i>	<i>Time (worst case)</i>
NFA	$O(r)$	$O(r \times x)$
DFA	$O(2^{ r })$	$O(x)$

Syntax Analysis (1)

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Computer Systems Group
LIACS

Position of a Parser in the Compiler Model



The Parser

- ⌘ The task of the parser is to check syntax
- ⌘ The syntax-directed translation stage in the compiler's front-end checks static semantics and produces an intermediate representation (IR) of the source program
 - ☒ Abstract syntax trees (ASTs)
 - ☒ Control-flow graphs (CFGs) with triples, three-address code, or register transfer lists
 - ☒ WHIRL (SGI Pro64 compiler) has 5 IR levels!

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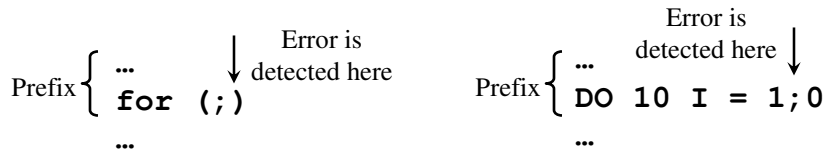
Error Handling

- ⌘ A good compiler should assist in identifying and locating errors
 - ☒ *Lexical errors*: important, compiler can easily recover and continue
 - ☒ *Syntax errors*: most important for compiler, can almost always recover
 - ☒ *Static semantic errors*: important, can sometimes recover
 - ☒ *Dynamic semantic errors*: hard or impossible to detect at compile time, runtime checks are required
 - ☒ *Logical errors*: hard or impossible to detect

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Viability-Prefix Property

- ⌘ The *viability-prefix property* of LL/LR parsers allows early detection of syntax errors
 - ☒ Goal: detection of an error as soon as possible without consuming unnecessary input
 - ☒ How: detect an error as soon as the prefix of the input does not match a prefix of any string in the language



Error Recovery Strategies

- ⌘ *Panic mode*
 - ☒ Discard input until a token in a set of designated synchronizing tokens is found
- ⌘ *Phrase-level recovery*
 - ☒ Perform local correction on the input to repair the error
- ⌘ *Error productions*
 - ☒ Augment grammar with productions for erroneous constructs
- ⌘ *Global correction*
 - ☒ Choose a minimal sequence of changes to obtain a global least-cost correction

Grammars (Recap)

- ⌘ Context-free grammar is a 4-tuple $G=(N, T, P, S)$ where
 - ⊠ T is a finite set of tokens (*terminal* symbols)
 - ⊠ N is a finite set of *nonterminals*
 - ⊠ P is a finite set of *productions* of the form $\alpha \rightarrow \beta$
 where $\alpha \in (N \cup T)^* N (N \cup T)^*$
 and $\beta \in (N \cup T)^*$
 - ⊠ S is a designated *start symbol* $S \in N$

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Notational Conventions Used

- ⌘ Terminals
 $a, b, c, \dots \in T$
 specific terminals: **0, 1, id, +**
- ⌘ Nonterminals
 $A, B, C, \dots \in N$
 specific nonterminals: *expr, term, stmt*
- ⌘ Grammar symbols
 $X, Y, Z \in (N \cup T)$
- ⌘ Strings of terminals
 $u, v, w, x, y, z \in T^*$
- ⌘ Strings of grammar symbols
 $\alpha, \beta, \gamma \in (N \cup T)^*$

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Derivations (Recap)

- ⌘ The *one-step derivation* is defined by

$$\alpha A \beta \Rightarrow \alpha \gamma \beta$$
 where $A \rightarrow \gamma$ is a production in the grammar
- ⌘ In addition, we define
 - ☒ \Rightarrow is *leftmost* \Rightarrow_{lm} if α does not contain a nonterminal
 - ☒ \Rightarrow is *rightmost* \Rightarrow_{rm} if β does not contain a nonterminal
 - ☒ Transitive closure \Rightarrow^* (zero or more steps)
 - ☒ Positive closure \Rightarrow^+ (one or more steps)
- ⌘ The *language generated by G* is defined by

$$L(G) = \{w \mid S \Rightarrow^+ w\}$$

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Derivation (Example)

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow - E$$

$$E \rightarrow \mathbf{id}$$

$$E \Rightarrow - E \Rightarrow - \mathbf{id}$$

$$E \Rightarrow_{rm} E + E \Rightarrow_{rm} E + \mathbf{id} \Rightarrow_{rm} \mathbf{id} + \mathbf{id}$$

$$E \Rightarrow^* E$$

$$E \Rightarrow^+ \mathbf{id} * \mathbf{id} + \mathbf{id}$$

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Chomsky Hierarchy: Language Classification

- ⌘ A grammar G is said to be
 - ☒ *Regular* if it is *right linear* where each production is of the form

$$A \rightarrow wB \quad \text{or} \quad A \rightarrow w$$
 or *left linear* where each production is of the form

$$A \rightarrow Bw \quad \text{or} \quad A \rightarrow w$$
 - ☒ *Context free* if each production is of the form

$$A \rightarrow \alpha$$
 where $A \in N$ and $\alpha \in (N \cup T)^*$
 - ☒ *Context sensitive* if each production is of the form

$$\alpha A \beta \rightarrow \alpha \gamma \beta$$
 where $A \in N$, $\alpha, \gamma, \beta \in (N \cup T)^*$, $|\gamma| > 0$
 - ☒ *Unrestricted*

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Chomsky Hierarchy

$L(\text{regular}) \subseteq L(\text{context free}) \subseteq L(\text{context sensitive}) \subseteq L(\text{unrestricted})$

Where $L(T) = \{ L(G) \mid G \text{ is of type } T \}$

That is, the set of all languages
generated by grammars G of type T

Examples:

Every *finite language* is regular

$L_1 = \{ \mathbf{a}^n \mathbf{b}^n \mid n \geq 1 \}$ is context free

$L_2 = \{ \mathbf{a}^n \mathbf{b}^n \mathbf{c}^n \mid n \geq 1 \}$ is context sensitive

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Parsing

- ⌘ *Universal* (any C-F grammar)
 - ☒ Cocke-Younger-Kasimi
 - ☒ Earley
- ⌘ *Top-down* (C-F grammar with restrictions)
 - ☒ Recursive descent (predictive parsing)
 - ☒ LL (Left-to-right, Leftmost derivation) methods
- ⌘ *Bottom-up* (C-F grammar with restrictions)
 - ☒ Operator precedence parsing
 - ☒ LR (Left-to-right, Rightmost derivation) methods
 - ☒ SLR, canonical LR, LALR

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Top-Down Parsing

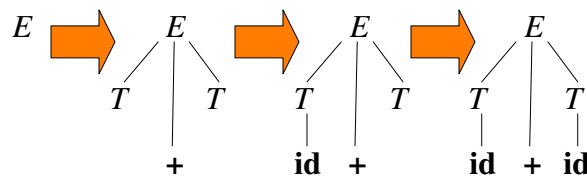
- ⌘ LL methods (Left-to-right, Leftmost derivation) and recursive-descent parsing

Grammar:

$E \rightarrow T + T$
 $T \rightarrow (E)$
 $T \rightarrow - E$
 $T \rightarrow \text{id}$

Leftmost derivation:

$E \Rightarrow_{lm} T + T$
 $\Rightarrow_{lm} \text{id} + T$
 $\Rightarrow_{lm} \text{id} + \text{id}$



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Left Recursion (Recap)

⌘ Productions of the form

$$A \rightarrow A \alpha$$

$$/ \beta$$

$$| \gamma$$

are left recursive

⌘ When one of the productions in a grammar is left recursive then a predictive parser may loop forever

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General Left Recursion Elimination

Arrange the nonterminals in some order A_1, A_2, \dots, A_n

for $i = 1, \dots, n$ **do**

for $j = 1, \dots, i-1$ **do**

 replace each

$$A_i \rightarrow A_j \gamma$$

 with

$$A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$$

 where

$$A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$$

enddo

 eliminate the immediate left recursion in A_i

enddo

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Immediate Left-Recursion Elimination

Rewrite every left-recursive production

$$\begin{aligned}
 A &\rightarrow A \alpha \\
 &| \beta \\
 &| \gamma \\
 &| A \delta
 \end{aligned}$$

into a right-recursive production:

$$\begin{aligned}
 A &\rightarrow \beta A_R \\
 &| \gamma A_R \\
 A_R &\rightarrow \alpha A_R \\
 &| \delta A_R \\
 &| \epsilon
 \end{aligned}$$

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Example Left Rec. Elimination

$$\left. \begin{aligned}
 A &\rightarrow BC | a \\
 B &\rightarrow CA | A b \\
 C &\rightarrow AB | CC | a
 \end{aligned} \right\} \text{Choose arrangement: } A, B, C$$

$i = 1$: nothing to do

$$\begin{aligned}
 i = 2, j = 1: & B \rightarrow CA | \underline{A} b \\
 \Rightarrow & B \rightarrow CA | \underline{BC} b | \underline{a} b \\
 \Rightarrow_{(\text{imm})} & B \rightarrow CA B_R | \underline{a} b B_R \\
 & B_R \rightarrow C \underline{b} B_R | \epsilon
 \end{aligned}$$

$$\begin{aligned}
 i = 3, j = 1: & C \rightarrow \underline{A} B | CC | a \\
 \Rightarrow & C \rightarrow \underline{BC} B | \underline{a} B | CC | a
 \end{aligned}$$

$$\begin{aligned}
 i = 3, j = 2: & C \rightarrow \underline{B} C B | \underline{a} B | CC | a \\
 \Rightarrow & C \rightarrow \underline{CA B_R} C B | \underline{a b B_R} C B | \underline{a} B | CC | a \\
 \Rightarrow_{(\text{imm})} & C \rightarrow \underline{a b B_R} C B C_R | \underline{a} B C_R | \underline{a} C_R \\
 & C_R \rightarrow A B_R C B C_R | C C_R | \epsilon
 \end{aligned}$$

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Left Factoring

⌘ When a nonterminal has two or more productions whose right-hand sides start with the same grammar symbols, the grammar is not LL(1) and cannot be used for predictive parsing

⌘ Replace productions

$$A \rightarrow \alpha \beta_1 / \alpha \beta_2 / \dots / \alpha \beta_n / \gamma$$

with

$$A \rightarrow \alpha A_R / \gamma$$

$$A_R \rightarrow \beta_1 / \beta_2 / \dots / \beta_n$$

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Predictive Parsing

⌘ Eliminate left recursion from grammar

⌘ Left factor the grammar

⌘ Compute FIRST and FOLLOW

⌘ Two variants:

☒ Recursive (recursive calls)

☒ Non-recursive (table-driven)

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FIRST (Use Defs from Book)

⌘ FIRST(α) = the set of terminals that begin all strings derived from α

$$\begin{aligned} \text{FIRST}(a) &= \{a\} && \text{if } a \in T \\ \text{FIRST}(\varepsilon) &= \{\varepsilon\} \\ \text{FIRST}(A) &= \bigcup_{A \rightarrow \alpha \in P} \text{FIRST}(\alpha) && \text{for } A \rightarrow \alpha \in P \\ \text{FIRST}(X_1 X_2 \dots X_k) &= && \\ & \quad \text{if for all } j = 1, \dots, k-1 : \varepsilon \in \text{FIRST}(X_j) \text{ then} && \\ & \quad \quad \text{add non-}\varepsilon \text{ in } \text{FIRST}(X_k) \text{ to} && \\ & \quad \text{FIRST}(X_1 X_2 \dots X_k) && \\ & \quad \text{if for all } j = 1, \dots, k : \varepsilon \in \text{FIRST}(X_j) \text{ then} && \\ & \quad \quad \text{add } \varepsilon \text{ to } \text{FIRST}(X_1 X_2 \dots X_k) && \end{aligned}$$

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FOLLOW (Use defs Book)

⌘ FOLLOW(A) = the set of terminals that can immediately follow nonterminal A

$$\begin{aligned} \text{FOLLOW}(A) &= \\ & \quad \text{for all } (B \rightarrow \alpha A \beta) \in P \text{ do} && \\ & \quad \quad \text{add } \text{FIRST}(\beta) \setminus \{\varepsilon\} \text{ to } \text{FOLLOW}(A) && \\ & \quad \text{for all } (B \rightarrow \alpha A \beta) \in P \text{ and } \varepsilon \in \text{FIRST}(\beta) \text{ do} && \\ & \quad \quad \text{add } \text{FOLLOW}(B) \text{ to } \text{FOLLOW}(A) && \\ & \quad \text{for all } (B \rightarrow \alpha A) \in P \text{ do} && \\ & \quad \quad \text{add } \text{FOLLOW}(B) \text{ to } \text{FOLLOW}(A) && \\ & \quad \text{if } A \text{ is the start symbol } S \text{ then} && \\ & \quad \quad \text{add } \$ \text{ to } \text{FOLLOW}(A) && \end{aligned}$$

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EXAMPLE (From Book)

⌘ Explain how FOLLOW works....

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LL(1) Grammar

⌘ A grammar G is LL(1) if for each collections of productions

$$A \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$$

for nonterminal A the following holds:

1. $\text{FIRST}(\alpha_i) \cap \text{FIRST}(\alpha_j) = \emptyset$ for all $i \neq j$
2. if $\alpha_i \Rightarrow^* \epsilon$ then
 - 2.a. $\alpha_j \not\Rightarrow^* \epsilon$ for all $i \neq j$
 - 2.b. $\text{FIRST}(\alpha_j) \cap \text{FOLLOW}(A) = \emptyset$
for all $i \neq j$

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Non-LL(1) Examples

Grammar	Not LL(1) because
$S \rightarrow S a \mid a$	Left recursive
$S \rightarrow a S \mid a$	$\text{FIRST}(a S) \cap \text{FIRST}(a) \neq \emptyset$
$S \rightarrow a R \mid \epsilon$ $R \rightarrow S \mid \epsilon$	For R : $S \rightarrow^* \epsilon$ and $\epsilon \rightarrow^* \epsilon$
$S \rightarrow a R a$ $R \rightarrow S \mid \epsilon$	For R : $\text{FIRST}(S) \cap \text{FOLLOW}(R) \neq \emptyset$

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Recursive Descent Parsing

- ⌘ Grammar must be LL(1)
- ⌘ Every nonterminal has one (recursive) procedure responsible for parsing the nonterminal's syntactic category of input tokens
- ⌘ When a nonterminal has multiple productions, each production is implemented in a branch of a selection statement based on input look-ahead information

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Using FIRST and FOLLOW to Write a Rec. Descent Parser

```

expr → term rest
rest → + term rest
        | - term rest
        | ε
term → id

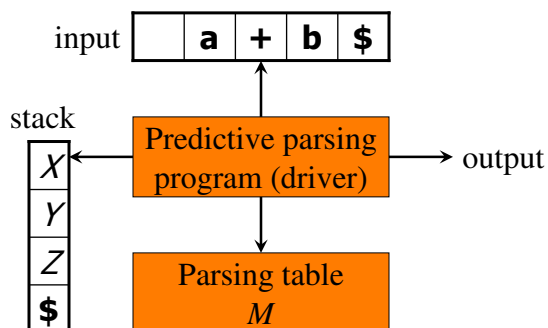
procedure rest();
begin
  if lookahead in FIRST(+ term rest) then
    match('+'); term(); rest()
  else if lookahead in FIRST(- term rest) then
    match('-'); term(); rest()
  else if lookahead in FOLLOW(rest) then
    return
  else error()
end;
    
```

$\text{FIRST}(+ \text{ term rest}) = \{ + \}$
 $\text{FIRST}(- \text{ term rest}) = \{ - \}$
 $\text{FOLLOW}(\text{rest}) = \{ \$ \}$

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Non-Recursive Predictive Parsing

⌘ Given an LL(1) grammar $G=(N, T, P, S)$
 construct a table $M[A, a]$ for $A \in N, a \in T$
 and use a driver program with a stack



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Constructing a Predictive Parsing Table

```

for each production  $A \rightarrow \alpha$  do
    for each  $a \in \text{FIRST}(\alpha)$  do
        add  $A \rightarrow \alpha$  to  $M[A,a]$ 
    enddo
    if  $\epsilon \in \text{FIRST}(\alpha)$  then
        for each  $b \in \text{FOLLOW}(A)$  do
            add  $A \rightarrow \alpha$  to  $M[A,b]$ 
        enddo
    endif
enddo
    Mark each undefined entry in  $M$  error
    
```

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Example Table

$E \rightarrow T E_R$
 $E_R \rightarrow + T E_R \mid \epsilon$
 $T \rightarrow F T_R$
 $T_R \rightarrow * F T_R \mid \epsilon$
 $F \rightarrow (E) \mid \text{id}$



$A \rightarrow \alpha$	$\text{FIRST}(\alpha)$	$\text{FOLLOW}(A)$
$E \rightarrow T E_R$	(id	\$)
$E_R \rightarrow + T E_R$	+	\$)
$E_R \rightarrow \epsilon$	ϵ	
$T \rightarrow F T_R$	(id	+ \$)
$T_R \rightarrow * F T_R$	*	+ \$)
$T_R \rightarrow \epsilon$	ϵ	
$F \rightarrow (E)$	(* + \$)
$F \rightarrow \text{id}$	id	



	id	+	*	()	\$
E	$E \rightarrow T E_R$			$E \rightarrow T E_R$		
E_R		$E_R \rightarrow + T E_R$			$E_R \rightarrow \epsilon$	$E_R \rightarrow \epsilon$
T	$T \rightarrow F T_R$			$T \rightarrow F T_R$		
T_R		$T_R \rightarrow \epsilon$	$T_R \rightarrow * F T_R$		$T_R \rightarrow \epsilon$	$T_R \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

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LL(1) Grammars are Unambiguous

Ambiguous grammar

$S \rightarrow i E t S S_R | a$

$S_R \rightarrow e S | \epsilon$

$E \rightarrow b$



$A \rightarrow \alpha$	FIRST(α)	FOLLOW(A)
$S \rightarrow i E t S$ S_R	i	e \$
$S \rightarrow a$	a	
$S_R \rightarrow e S$	e	e \$
$S_R \rightarrow \epsilon$	ϵ	
$E \rightarrow b$	b	t

Error: duplicate table entry

	a	b	e	i	t	\$
S	$S \rightarrow a$			$S \rightarrow i E t S S_R$		
S_R			<div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;"> $S_R \rightarrow \epsilon$ $S_R \rightarrow e S$ </div>			$S_R \rightarrow \epsilon$
E		$E \rightarrow b$				31

Predictive Parsing Program (Driver)

```

push($)
push(S)
a := lookahead
repeat
    X := pop()
    if X is a terminal or X = $ then
        match(X) // move to next token, a := lookahead
    else if M[X,a] = X → Y1Y2...Yk then
        push(Yk, Yk-1, ..., Y2, Y1) // such that Y1 is on top
        produce output and/or invoke actions
    else error()
endif
until X = $
    
```

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Example Table-Driven Parsing

Stack	Input	Production applied
$\$E$	$id+id*id\$$	
$\$E_R T$	$id+id*id\$$	$E \rightarrow T E_R$
$\$E_R T_R F$	$id+id*id\$$	$T \rightarrow F T_R$
$\$E_R T_R id$	$id+id*id\$$	$F \rightarrow id$
$\$E_R T_R$	$+id*id\$$	
$\$E_R$	$+id*id\$$	$T_R \rightarrow \epsilon$
$\$E_R T+$	$+id*id\$$	$E_R \rightarrow + T E_R$
$\$E_R T$	$id*id\$$	
$\$E_R T_R F$	$id*id\$$	$T \rightarrow F T_R$
$\$E_R T_R id$	$id*id\$$	$F \rightarrow id$
$\$E_R T_R$	$*id\$$	
$\$E_R T_R F*$	$*id\$$	$T_R \rightarrow * F T_R$
$\$E_R T_R F$	$id\$$	
$\$E_R T_R id$	$id\$$	$F \rightarrow id$
$\$E_R T_R$	$\$$	
$\$E_R$	$\$$	$T_R \rightarrow \epsilon$
$\$$	$\$$	$E_R \rightarrow \epsilon$

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Panic Mode Recovery

Add synchronizing actions to undefined entries based on FOLLOW

$FOLLOW(E) = \{ \$ \}$
 $FOLLOW(E_R) = \{ \$ \}$
 $FOLLOW(T) = \{ + \$ \}$
 $FOLLOW(T_R) = \{ + \$ \}$
 $FOLLOW(F) = \{ * + \$ \}$

	id	+	*	()	\$
E	$E \rightarrow T E_R$			$E \rightarrow T E_R$	synch	synch
E_R		$E_R \rightarrow + T E_R$			$E_R \rightarrow \epsilon$	$E_R \rightarrow \epsilon$
T	$T \rightarrow F T_R$	synch		$T \rightarrow F T_R$	synch	synch
T_R		$T_R \rightarrow \epsilon$	$T_R \rightarrow * F T_R$		$T_R \rightarrow \epsilon$	$T_R \rightarrow \epsilon$
F	$F \rightarrow id$	synch	synch	$F \rightarrow (E)$	synch	synch

synch: pop A and skip input till synch token
or skip until $FIRST(A)$ found

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Phrase-Level Recovery

Change input stream by inserting missing *
 For example: **id id** is changed into **id * id**

	id	+	*	()	\$
E	$E \rightarrow T E_R$			$E \rightarrow T E_R$	synch	synch
E_R		$E_R \rightarrow + T E_R$			$E_R \rightarrow \epsilon$	$E_R \rightarrow \epsilon$
T	$T \rightarrow F T_R$	synch		$T \rightarrow F T_R$	synch	synch
T_R	insert *	$T_R \rightarrow \epsilon$	$T_R \rightarrow * F T_R$		$T_R \rightarrow \epsilon$	$T_R \rightarrow \epsilon$
F	$F \rightarrow \text{id}$	synch	synch	$F \rightarrow (E)$	synch	synch

insert *: insert missing * and redo the production

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Error Productions

$E \rightarrow T E_R$
 $E_R \rightarrow + T E_R \mid \epsilon$
 $T \rightarrow F T_R$
 $T_R \rightarrow * F T_R \mid \epsilon$
 $F \rightarrow (E) \mid \text{id}$

Add error production:

$T_R \rightarrow F T_R$
 to ignore missing *, e.g.: **id id**

	id	+	*	()	\$
E	$E \rightarrow T E_R$			$E \rightarrow T E_R$	synch	synch
E_R		$E_R \rightarrow + T E_R$			$E_R \rightarrow \epsilon$	$E_R \rightarrow \epsilon$
T	$T \rightarrow F T_R$	synch		$T \rightarrow F T_R$	synch	synch
T_R	$T_R \rightarrow F T_R$	$T_R \rightarrow \epsilon$	$T_R \rightarrow * F T_R$		$T_R \rightarrow \epsilon$	$T_R \rightarrow \epsilon$
F	$F \rightarrow \text{id}$	synch	synch	$F \rightarrow (E)$	synch	synch

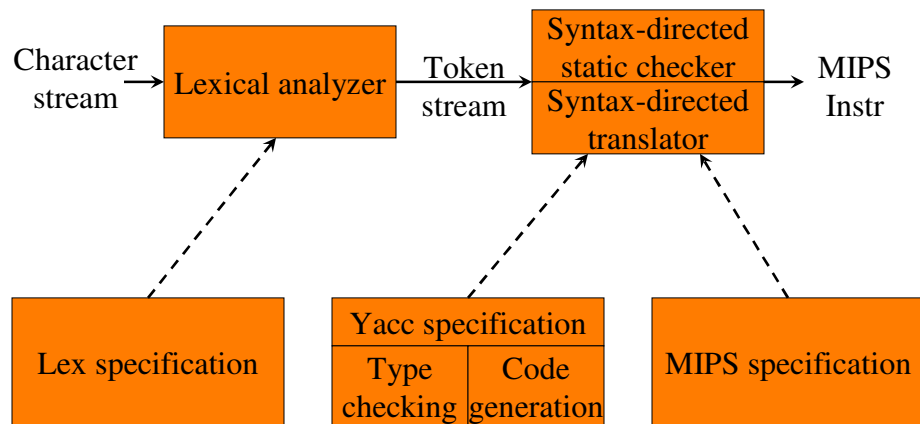
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Static Checking and Type Systems

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1

The Structure of our Compiler Revisited



2

Static versus Dynamic Checking

- ⌘ *Static checking*: the compiler enforces programming language's *static semantics*, which are checked at compile time
- ⌘ *Runtime checking*: *dynamic semantics* are checked at run time by special code generated by the compiler

3

Static Checking

- ⌘ Typical examples of static checking are
 - ☒ Type checks
 - ☒ Flow-of-control checks
 - ☒ Uniqueness checks
 - ☒ Name-related checks

4

Type Checks, Overloading, Coercion, and Polymorphism

```
int op(int), op(float);
int f(float);
int a, c[10], d;

d = c+d;           // FAIL

*d = a;           // FAIL

a = op(d);        // OK: overloading (C++)

a = f(d);         // OK: coercion

vector<int> v;     // OK: template instantiation
```

5

Flow-of-Control Checks

```
myfunc ()
{ ...
  break; // ERROR
}
```

```
myfunc ()
{ ...
  while (n)
  { ...
    if (i>10)
      break; // OK
  }
}
```

```
myfunc ()
{ ...
  switch (a)
  { case 0:
    ...
      break; // OK
    case 1:
    ...
  }
}
```

6

Uniqueness Checks

```
myfunc()
{ int i, j, i; // ERROR
  ...
}
```

```
cnufym(int a, int a) // ERROR
{ ...
}
```

```
struct myrec
{ int name;
};
struct myrec // ERROR
{ int id;
};
```

7

Name-Related Checks

```
LoopA: for (int I = 0; I < n; I++)
{ ...
  if (a[I] == 0)
    break LoopB;
  ...
}
```

8

One-Pass versus Multi-Pass Static Checking

- ⌘ *One-pass compiler*: static checking for C, Pascal, Fortran, and many other languages can be performed in one pass while at the same time intermediate code is generated
- ⌘ *Multi-pass compiler*: static checking for Ada, Java, and C# is performed in a separate phase, sometimes requiring traversing the syntax tree multiple times

9

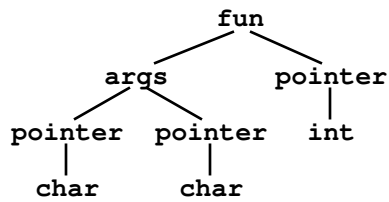
Type Expressions

- ⌘ *Type expressions* are used in declarations and type casts to define or refer to a type
 - ⊠ *Primitive types*, such as `int` and `bool`
 - ⊠ *Type constructors*, such as pointer-to, array-of, records and classes, templates, and functions
 - ⊠ *Type names*, such as typedefs in C and named types in Pascal, refer to type expressions

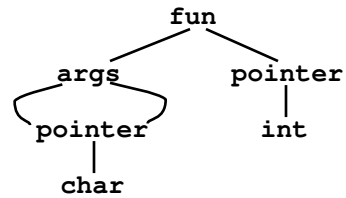
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Graph Representations for Type Expressions

```
int *fun(char*, char*)
```



Tree forms

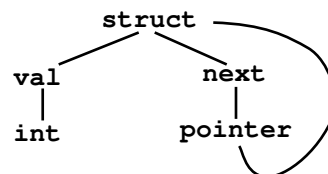


DAGs

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Cyclic Graph Representations

```
struct Node  
{ int val;  
  struct Node *next;  
};
```



Cyclic graph

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Name Equivalence

- ⌘ Each type name is a distinct type, even when the type expressions the names refer to are the same
- ⌘ Types are identical only if names match
- ⌘ Used by Pascal (inconsistently)

```
type link = ^node;  
var next : link;  
    last : link;  
    p : ^node;  
    q, r : ^node;
```

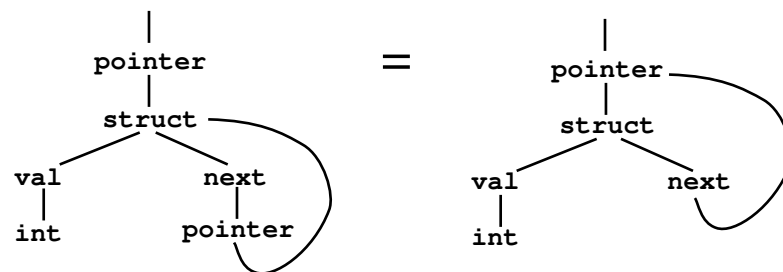
With name equivalence in Pascal:

```
p ≠ next  
p ≠ last  
p = q = r  
next = last
```

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Structural Equivalence of Type Expressions

- ⌘ Two types are the same if they are structurally identical
- ⌘ Used in C, Java, C#



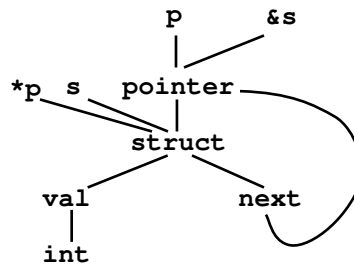
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Structural Equivalence of Type Expressions (cont'd)

- ⌘ Two structurally equivalent type expressions have the same pointer address when constructing graphs by sharing nodes

```
struct Node
{ int val;
  struct Node *next;
};
struct Node s, *p;
```

```
... p = &s; // OK
... *p = s; // OK
```



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Type Systems

- ⌘ A *type system* defines a set of types and rules to assign types to programming language constructs
- ⌘ Informal type system rules, for example
"if both operands of addition are of type integer, then the result is of type integer"
- ⌘ Formal type system rules: Post system

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A Simple Language Example

$P \rightarrow D ; S$	$E \rightarrow \text{true}$
$D \rightarrow D ; D$	false
id : T	literal
$T \rightarrow \text{boolean}$	num
char	id
integer	$E \text{ and } E$
array [num] of T	$E \text{ mod } E$
$^ T$	$E [E]$
$S \rightarrow \text{id} := E$	$E \wedge$
if E then S	
while E do S	
$S ; S$	

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Simple Language Example: Declarations

$D \rightarrow \text{id} : T$	{ $\text{addtype}(\text{id.entry}, T.\text{type})$ }
$T \rightarrow \text{boolean}$	{ $T.\text{type} := \text{boolean}$ }
$T \rightarrow \text{char}$	{ $T.\text{type} := \text{char}$ }
$T \rightarrow \text{integer}$	{ $T.\text{type} := \text{integer}$ }
$T \rightarrow \text{array}$ [num] of T_1	{ $T.\text{type} := \text{array}(1..\text{num.val}, T_1.\text{type})$ }
$T \rightarrow ^ T_1$	{ $T.\text{type} := \text{pointer}(T_1)$ }

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Constructing Type Graphs in Yacc

<code>Type *mkint()</code>	construct int node if not already constructed
<code>Type *mkarr(Type*, int)</code>	construct array-of-type node if not already constructed
<code>Type *mkptr(Type*)</code>	construct pointer-of-type node if not already constructed

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Syntax-Directed Definitions for Constructing Type Graphs in Yacc

```
%union
{ Symbol *sym;
  int num;
  Type *typ;
}
%token INT
%token <sym> ID
%token <int> NUM
%type <typ> type
%%
decl : type ID          { addtype($2, $1); }
     | type ID '[' NUM ']' { addtype($2, mkarr($1, $4)); }
     ;
type : INT              { $$ = mkint(); }
     | type '*'         { $$ = mkptr($1); }
     | /* empty */     { $$ = mkint(); }
     ;
```

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Syntax-Directed Definitions for Type Checking in Yacc

```
%{
enum Types {Tint, Tfloat, Tpointer, Tarray, ... };
typedef struct Type
{ enum Types type;
  struct Type *child;
} Type;
%}
%union
{ Type *typ;
}
%type <typ> expr
%%
expr : expr '+' expr { if ($1.type != Tint
                        || $3.type != Tint)
                        semerror("non-int operands in +");
                        $$ = mkint();
                        emit(iadd);
                    }
```

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Type Conversion and Coercion

- ⌘ Consider $x+i$, where $x:=real$ and $i:=int$
 - ☒ x *intto* *real* $+$
- ⌘ *Type conversion* is explicit, for example using type casts
- ⌘ *Type coercion* is implicitly performed by the compiler
- ⌘ Both require a type system to check and infer types for (sub)expressions

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Syntax-Directed Definitions for Type Coercion in Yacc

```
%{ ... %}
%%
expr : expr '+' expr
    { if ($1.type == Tint && $3.type == Tint)
      { $$ = mkint(); emit(iadd);
      }
      else if ($1.type == Tfloat && $3.type == Tfloat)
      { $$ = mkfloat(); emit(fadd);
      }
      else if ($1.type == Tfloat && $3.type == Tint)
      { $$ = mkfloat(); emit(i2f); emit(fadd);
      }
      else if ($1.type == Tint && $3.type == Tfloat)
      { $$ = mkfloat(); emit(swap); emit(i2f); emit(fadd);
      }
      else semerror("type error in +");
      $$ = mkint();
    }
}
```

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Syntax-Directed Definitions for L-Values and R-Values in Yacc

```
expr : expr '+' expr
    { if ($1.typ->type != Tint
      || $3.typ->type != Tint)
      semerror("non-int operands in +");
      $$ .typ = mkint();
      $$ .islval = FALSE;
      emit(...);
    }
| expr '=' expr
    { if (!$1.islval || $1.typ != $3.typ)
      semerror("invalid assignment");
      $$ .typ = $1.typ; $$ .islval = FALSE;
      emit(...);
    }
| ID
    { $$ .typ = lookup($1);
      $$ .islval = TRUE;
      emit(...);
    }
}
```

```
%{
typedef struct Node
{ Type *typ;
  int islval;
} Node;
%}
%union
{ Node *rec;
}
%type <rec> expr
%%
```

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Syntax Analysis Part 2

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1

Follow Sets

⌘ Rules for Follow Sets

- ⊠ First put \$ (the end of input marker) in Follow(S) (S is the start symbol)
- ⊠ If there is a production $A \rightarrow aBb$, (where a can be a whole string) **then** everything in FIRST(b) except for ϵ is placed in FOLLOW(B).
- ⊠ If there is a production $A \rightarrow aB$, **then** everything in FOLLOW(A) is in FOLLOW(B)
- ⊠ If there is a production $A \rightarrow aBb$, where FIRST(b) contains ϵ , **then** everything in FOLLOW(A) is in FOLLOW(B)

2

Bottom-Up Parsing

- ⌘ LR methods (Left-to-right, Rightmost derivation)
 - ☒ LR(0), SLR, Canonical LR, LALR
- ⌘ Other special cases:
 - ☒ Shift-reduce parsing
 - ☒ Operator-precedence parsing

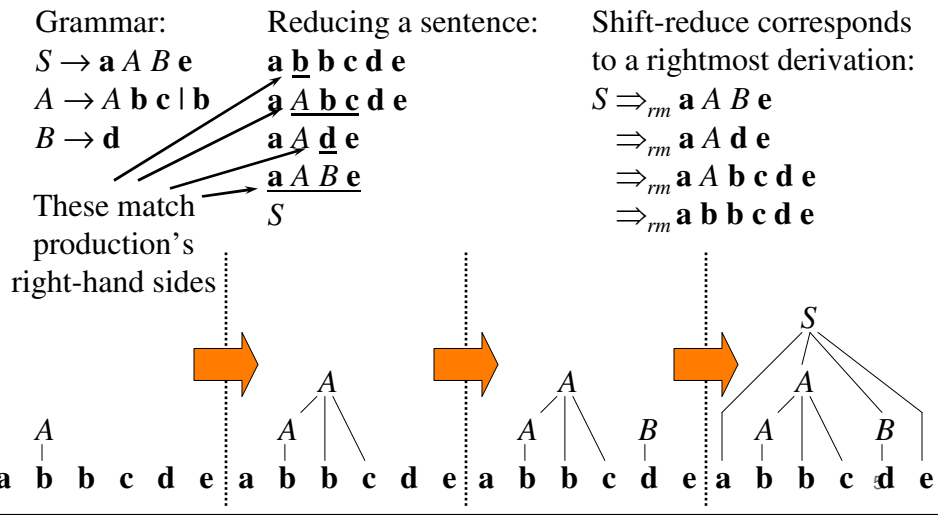
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Operator-Precedence Parsing

- ⌘ Special case of shift-reduce parsing
- ⌘ We will not further discuss (you can skip textbook section 4.6)

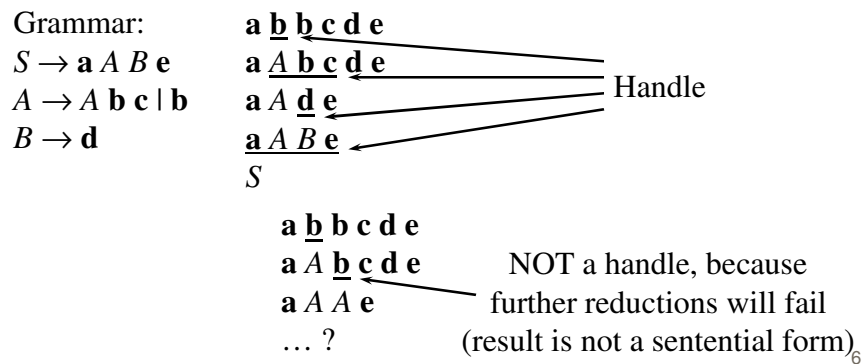
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Shift-Reduce Parsing



Handles

A *handle* is a substring of grammar symbols in a *right-sentential form* that matches a right-hand side of a production



Stack Implementation of Shift-Reduce Parsing

Grammar:
 $E \rightarrow E + E$
 $E \rightarrow E * E$
 $E \rightarrow (E)$
 $E \rightarrow \text{id}$

Stack	Input	Action
\$	id+id*id\$	shift
<u>\$id</u>	+id*id\$	reduce $E \rightarrow \text{id}$
\$E	+id*id\$	shift
\$E+	id*id\$	shift
<u>\$E+id</u>	*id\$	reduce $E \rightarrow \text{id}$
\$E+E	*id\$	shift (or reduce?)
\$E+E*	id\$	shift
<u>\$E+E*id</u>	\$	reduce $E \rightarrow \text{id}$
<u>\$E+E*E</u>	\$	reduce $E \rightarrow E * E$
<u>\$E+E</u>	\$	reduce $E \rightarrow E + E$
\$E	\$	accept

Find handles to reduce

How to resolve conflicts?

7

Conflicts

- ⌘ Shift-reduce and reduce-reduce conflicts are caused by
 - ☒ The limitations of the LR parsing method (even when the grammar is unambiguous)
 - ☒ Ambiguity of the grammar

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Shift-Reduce Parsing: Shift-Reduce Conflicts

Ambiguous grammar:
 $S \rightarrow \text{if } E \text{ then } S$
 $\quad | \text{if } E \text{ then } S \text{ else } S$
 $\quad | \text{other}$

Resolve in favor
of shift, so **else**
matches closest **if**

Stack	Input	Action
\$...	...\$...
\$...if <i>E</i> then <i>S</i>	else ...\$	shift or reduce?

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Shift-Reduce Parsing: Reduce-Reduce Conflicts

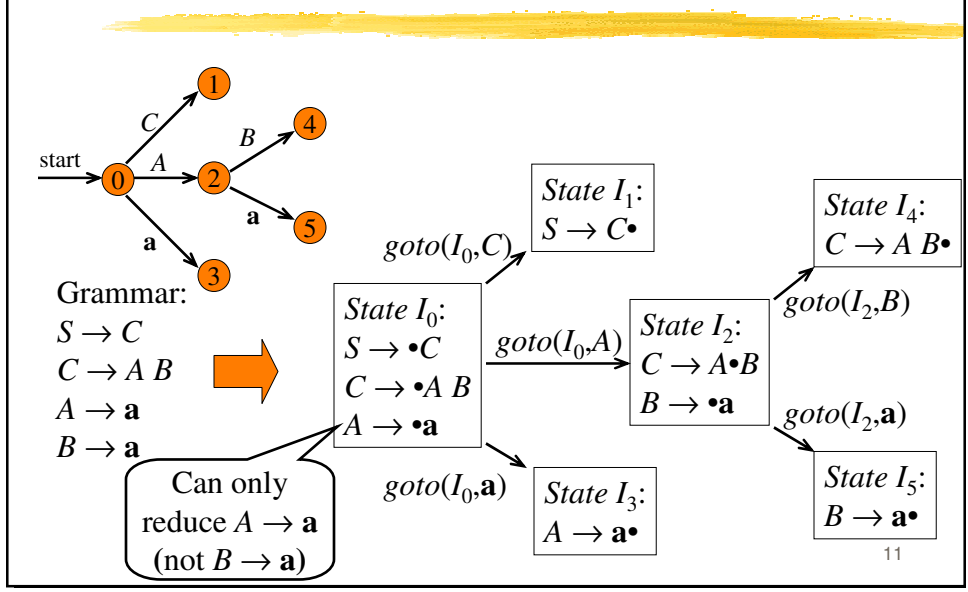
Grammar:
 $C \rightarrow A B$
 $A \rightarrow \mathbf{a}$
 $B \rightarrow \mathbf{a}$

Resolve in favor
of reduce $A \rightarrow \mathbf{a}$,
otherwise we're stuck!

Stack	Input	Action
\$	aa\$	shift
\$ <u>a</u>	a\$	reduce $A \rightarrow \mathbf{a}$ or $B \rightarrow \mathbf{a}$?

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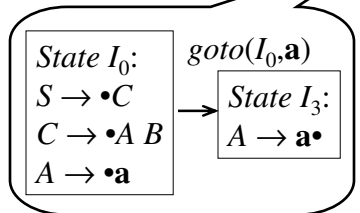
LR(k) Parsers: Use a DFA for Shift/Reduce Decisions



DFA for Shift/Reduce Decisions

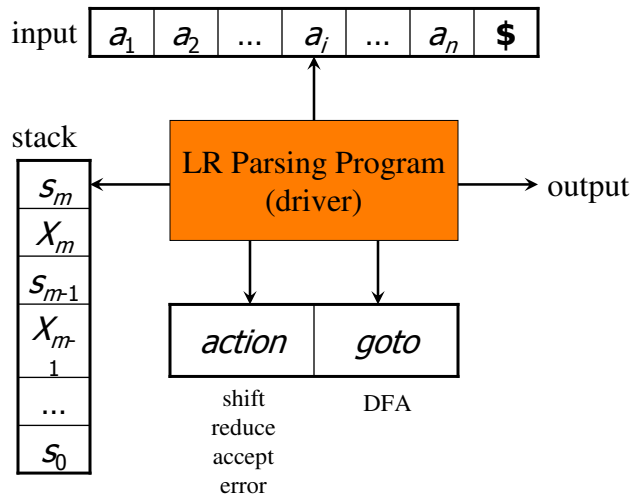
The states of the DFA are used to determine if a handle is on top of the stack

Grammar:
 $S \rightarrow C$
 $C \rightarrow AB$
 $A \rightarrow a$
 $B \rightarrow a$



Stack	Input	Action
\$ 0	aa\$	start in state 0
\$ 0	aa\$	shift (and goto state 3)
\$ 0 a 3	a\$	reduce $A \rightarrow a$ (goto 2)
\$ 0 A 2	a\$	shift (goto 5)
\$ 0 A 2 a 5	\$	reduce $B \rightarrow a$ (goto 4)
\$ 0 A 2 B 4	\$	reduce $C \rightarrow AB$ (goto 1)
\$ 0 C 1	\$	reduce $S \rightarrow C$
\$ 0 S 1	\$	accept

Model of an LR Parser



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LR Parsing

Configuration (= LR parser state):

$$(s_0 X_1 s_1 X_2 s_2 \dots X_m s_m, a_i a_{i+1} \dots a_n \$)$$

⏟
⏟
 stack input

If $action[s_m, a_i] = \text{shift } s$, then push a_i , push s , and advance input:

$$(s_0 X_1 s_1 X_2 s_2 \dots X_m s_m a_i s, a_{i+1} \dots a_n \$)$$

If $action[s_m, a_i] = \text{reduce } A \rightarrow \beta$ and $goto[s_{m-r}, A] = s$ with $r = |\beta|$ then pop $2r$ symbols, push A , and push s :

$$(s_0 X_1 s_1 X_2 s_2 \dots X_{m-r} s_{m-r} A s, a_i a_{i+1} \dots a_n \$)$$

If $action[s_m, a_i] = \text{accept}$, then stop

If $action[s_m, a_i] = \text{error}$, then attempt recovery

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Example LR Parse Table

Grammar:

1. $E \rightarrow E + T$
2. $E \rightarrow T$
3. $T \rightarrow T * F$
4. $T \rightarrow F$
5. $F \rightarrow (E)$
6. $F \rightarrow id$

state	action					goto			
	id	+	*	()	\$	E	T	F
0	s5			s4			1	2	3
1		s6				acc			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3
7	s5			s4					10
8		s6			s1				
9			s7		r1	r1			
10		r3	r3		r3	r3			
11		r5	r5		r5	r5			

Shift & goto 5

Reduce by production #1

Example LR Parsing

Grammar:

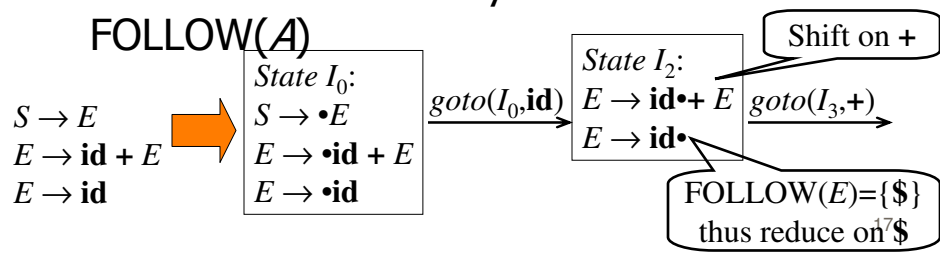
1. $E \rightarrow E + T$
2. $E \rightarrow T$
3. $T \rightarrow T * F$
4. $T \rightarrow F$
5. $F \rightarrow (E)$
6. $F \rightarrow id$

Stack	Input	Action
\$ 0	id*id+id\$	shift 5
\$ 0 id 5	*id+id\$	reduce 6 goto 3
\$ 0 F 3	*id+id\$	reduce 4 goto 2
\$ 0 T 2	*id+id\$	shift 7
\$ 0 T 2 * 7	id+id\$	shift 5
\$ 0 T 2 * 7 id 5	+id\$	reduce 6 goto 10
\$ 0 T 2 * 7 F 10	+id\$	reduce 3 goto 2
\$ 0 T 2	+id\$	reduce 2 goto 1
\$ 0 E 1	+id\$	shift 6
\$ 0 E 1 + 6	id\$	shift 5
\$ 0 E 1 + 6 id 5	\$	reduce 6 goto 3
\$ 0 E 1 + 6 F 3	\$	reduce 4 goto 9
\$ 0 E 1 + 6 T 9	\$	reduce 1 goto 1
\$ 0 E 1	\$	accept

SLR Grammars

⌘ SLR (Simple LR): a simple extension of LR(0) shift-reduce parsing

⌘ SLR eliminates some conflicts by populating the parsing table with reductions $A \rightarrow \alpha$ on symbols in $\text{FOLLOW}(A)$



SLR Parsing Table

⌘ Reductions do not fill entire rows

⌘ Otherwise the same as LR(0)

1. $S \rightarrow E$
2. $E \rightarrow \text{id} + E$
3. $E \rightarrow \text{id}$

	id	+	\$	E
0	s2			1
1		acc		
2		s3	r3	
3	s2			4
4			r2	

Shift on +
 $\text{FOLLOW}(E) = \{ \$ \}$
 thus reduce on \$

SLR Parsing

- ⌘ An LR(0) state is a set of LR(0) items
- ⌘ An LR(0) item is a production with a • (dot) in the right-hand side
- ⌘ Build the LR(0) DFA by
 - ☒ *Closure operation* to construct LR(0) items
 - ☒ *Goto operation* to determine transitions
- ⌘ Construct the SLR parsing table from the DFA
- ⌘ LR parser program uses the SLR parsing table to determine shift/reduce operations

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LR(0) Items of a Grammar

- ⌘ An *LR(0) item* of a grammar G is a production of G with a • at some position of the right-hand side
- ⌘ Thus, a production
 $A \rightarrow XYZ$
has four items:
 - $[A \rightarrow \bullet XYZ]$
 - $[A \rightarrow X \bullet YZ]$
 - $[A \rightarrow XY \bullet Z]$
 - $[A \rightarrow XYZ \bullet]$
- ⌘ Note that production $A \rightarrow \epsilon$ has one item $[A \rightarrow \bullet]$

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Constructing the set of LR(0) Items of a Grammar

1. The grammar is augmented with a new start symbol S' and production $S' \rightarrow S$
2. Initially, set $C = \text{closure}(\{[S' \rightarrow \bullet S]\})$
(this is the start state of the DFA)
3. For each set of items $I \in C$ and each grammar symbol $X \in (N \cup T)$ such that $\text{goto}(I, X) \notin C$ and $\text{goto}(I, X) \neq \emptyset$, add the set of items $\text{goto}(I, X)$ to C
4. Repeat 3 until no more sets can be added to C

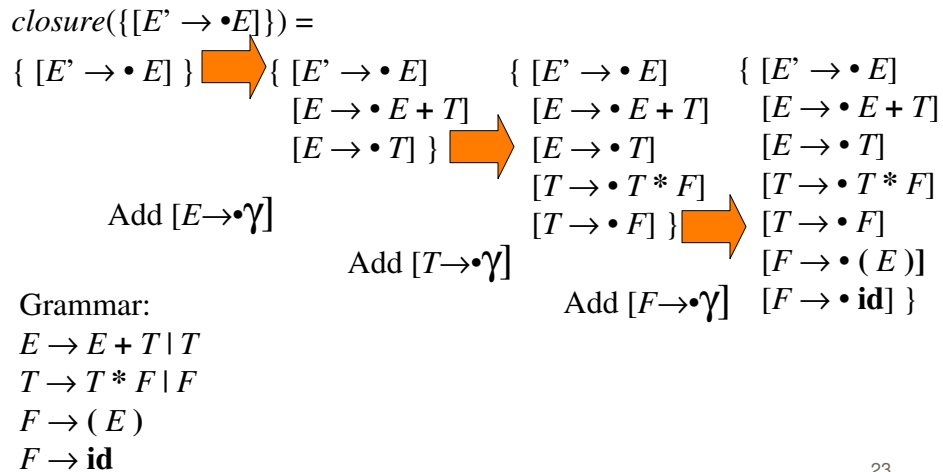
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The Closure Operation for LR(0) Items

1. Start with $\text{closure}(I) = I$
2. If $[A \rightarrow \alpha \bullet B \beta] \in \text{closure}(I)$ then for each production $B \rightarrow \gamma$ in the grammar, add the item $[B \rightarrow \bullet \gamma]$ to I if not already in I
3. Repeat 2 until no new items can be added

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The Closure Operation (Example)



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The Goto Operation for LR(0) Items

1. For each item $[A \rightarrow \alpha \bullet X \beta] \in I$, add the set of items $closure(\{[A \rightarrow \alpha X \bullet \beta]\})$ to $goto(I, X)$ if not already there
2. Repeat step 1 until no more items can be added to $goto(I, X)$
3. Intuitively, $goto(I, X)$ is the set of items that are valid for the viable prefix γX when I is the set of items that are valid for γ

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The Goto Operation (Example 1)

Suppose $I = \{ [E' \rightarrow \bullet E]$
 $[E \rightarrow \bullet E + T]$
 $[E \rightarrow \bullet T]$
 $[T \rightarrow \bullet T * F]$
 $[T \rightarrow \bullet F]$
 $[F \rightarrow \bullet (E)]$
 $[F \rightarrow \bullet \text{id}] \}$

Then $\text{goto}(I, E) = \text{closure}(\{ [E' \rightarrow E \bullet, E \rightarrow E \bullet + T] \})$
 $= \{ [E' \rightarrow E \bullet]$
 $[E \rightarrow E \bullet + T] \}$

Grammar:
 $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E)$
 $F \rightarrow \text{id}$

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The Goto Operation (Example 2)

Suppose $I = \{ [E' \rightarrow E \bullet], [E \rightarrow E \bullet + T] \}$

Then $\text{goto}(I, +) = \text{closure}(\{ [E \rightarrow E + \bullet T] \}) = \{ [E \rightarrow E + \bullet T]$
 $[T \rightarrow \bullet T * F]$
 $[T \rightarrow \bullet F]$
 $[F \rightarrow \bullet (E)]$
 $[F \rightarrow \bullet \text{id}] \}$

Grammar:
 $E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E)$
 $F \rightarrow \text{id}$

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Constructing SLR Parsing Tables

1. Augment the grammar with $S \rightarrow S$
2. Construct the set $C = \{I_0, I_1, \dots, I_n\}$ of LR(0) items
3. If $[A \rightarrow \alpha \bullet a \beta] \in I_i$ and $goto(I_i, a) = I_j$ then set $action[i, a] = \text{shift } j$
4. If $[A \rightarrow \alpha \bullet] \in I_i$ then set $action[i, a] = \text{reduce } A \rightarrow \alpha$ for all $a \in \text{FOLLOW}(A)$ (apply only if $A \neq S$)
5. If $[S \rightarrow S \bullet]$ is in I_i then set $action[i, \$] = \text{accept}$
6. If $goto(I_i, A) = I_j$ then set $goto[i, A] = j$
7. Repeat 3-6 until no more entries added
8. The initial state i is the I_i holding item $[S \rightarrow \bullet S]$ ²⁷

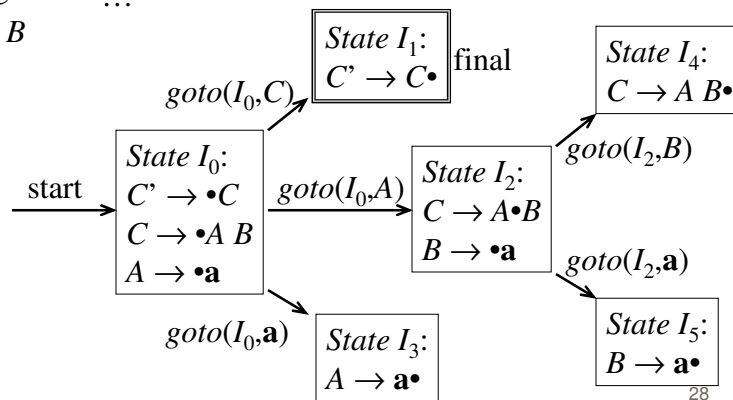
Example SLR Grammar and LR(0) Items

Augmented grammar:

1. $C' \rightarrow C$
2. $C \rightarrow A B$
3. $A \rightarrow a$
4. $B \rightarrow a$

$$I_0 = \text{closure}(\{[C' \rightarrow \bullet C]\})$$

$$I_1 = \text{goto}(I_0, C) = \text{closure}(\{[C' \rightarrow C \bullet]\})$$



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Example SLR Parsing Table

State I_0 :

$C' \rightarrow \bullet C$

$C \rightarrow \bullet A B$

$A \rightarrow \bullet a$

State I_1 :

$C' \rightarrow C \bullet$

State I_2 :

$C \rightarrow A \bullet B$

$B \rightarrow \bullet a$

State I_3 :

$A \rightarrow a \bullet$

State I_4 :

$C \rightarrow A B \bullet$

State I_5 :

$B \rightarrow a \bullet$

	a	\$	C	A	B
0	s3		1	2	
1		acc			
2	s5				4
3	r3				
4		r2			
5		r4			

Grammar:

1. $C' \rightarrow C$
2. $C \rightarrow A B$
3. $A \rightarrow a$
4. $B \rightarrow a$

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SLR and Ambiguity

- ⌘ Every SLR grammar is unambiguous, but **not** every unambiguous grammar is SLR
- ⌘ Consider for example the unambiguous grammar

$$S \rightarrow L = R \mid R$$

$$L \rightarrow * R \mid \text{id}$$

I_0 :

$S' \rightarrow \bullet S$

$S \rightarrow \bullet L = R$

$S \rightarrow \bullet * R$

$L \rightarrow \bullet * R$

$L \rightarrow \bullet \text{id}$

$R \rightarrow \bullet L$

I_1 :

$S' \rightarrow S \bullet$

I_2 :

$S \rightarrow L \bullet = R$

$R \rightarrow L \bullet$

I_3 :

$S \rightarrow R \bullet$

I_4 :

$L \rightarrow * \bullet R$

$R \rightarrow \bullet L$

$L \rightarrow \bullet * R$

$L \rightarrow \bullet \text{id}$

I_5 :

$L \rightarrow \text{id} \bullet$

I_6 :

$S \rightarrow L = \bullet R$

$R \rightarrow \bullet L$

$L \rightarrow \bullet * R$

$L \rightarrow \bullet \text{id}$

I_7 :

$L \rightarrow * R \bullet$

I_8 :

$R \rightarrow L \bullet$

I_9 :

$S \rightarrow L = R \bullet$

action[2,]=s6

action[2,]=r5

Has no SLR parsing table

LR(1) Grammars

- ⌘ SLR too simple
- ⌘ LR(1) parsing uses lookahead to avoid unnecessary conflicts in parsing table
- ⌘ LR(1) item = LR(0) item + lookahead

LR(0) item:
 $[A \rightarrow \alpha \cdot \beta]$

LR(1) item:
 $[A \rightarrow \alpha \cdot \beta, a]$

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LALR(1) Grammars

- ⌘ LR(1) parsing tables have many states
- ⌘ LALR(1) parsing (Look-Ahead LR) combines LR(1) states to reduce table size
- ⌘ Less powerful than LR(1)
 - ☒ Will not introduce shift-reduce conflicts, because shifts do not use lookaheads
 - ☒ May introduce reduce-reduce conflicts, but seldom do so for grammars of programming languages

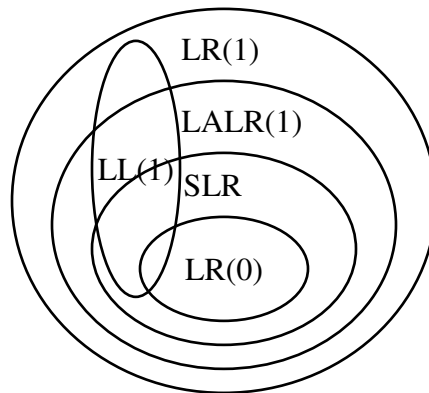
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LL, SLR, LR, LALR Summary

- ⌘ LL parse tables computed using FIRST/FOLLOW
 - ☒ Nonterminals \times terminals \rightarrow productions
 - ☒ Computed using FIRST/FOLLOW
- ⌘ LR parsing tables computed using closure/goto
 - ☒ LR states \times terminals \rightarrow shift/reduce actions
 - ☒ LR states \times terminals \rightarrow goto state transitions
- ⌘ A grammar is
 - ☒ LL(1) if its LL(1) parse table has no conflicts
 - ☒ SLR if its SLR parse table has no conflicts
 - ☒ LALR(1) if its LALR(1) parse table has no conflicts
 - ☒ LR(1) if its LR(1) parse table has no conflicts

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LL, SLR, LR, LALR Grammars



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Error Detection in LR Parsing

- ⌘ Canonical LR parser uses full LR(1) parse tables and will never make a single reduction before recognizing the error when a syntax error occurs on the input
- ⌘ SLR and LALR may still reduce when a syntax error occurs on the input, but will never shift the erroneous input symbol

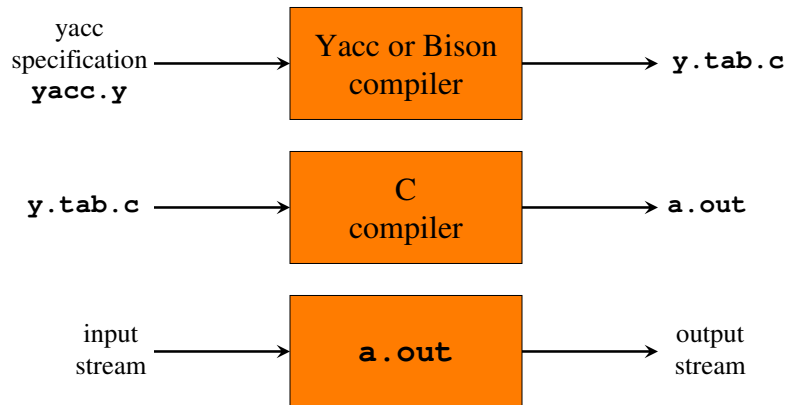
50

ANTLR, Yacc, and Bison

- ⌘ *ANTLR* tool generates LL(k) parsers
- ⌘ *Yacc* (Yet Another Compiler Compiler) generates LALR(1) parsers
- ⌘ *Bison* (*Yacc* improved)

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Creating an LALR(1) Parser with Yacc/Bison



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Yacc Specification

- ⌘ A *yacc specification* consists of three parts:
 - yacc declarations*, and *C declarations* in `%{ %}`
 - `%%`
 - translation rules*
 - `%%`
 - user-defined auxiliary procedures*
- ⌘ *Translation rules* are grammar productions and actions:
 - production*₁ { *semantic action*₁ }
 - production*₂ { *semantic action*₂ }
 - ...
 - production*_n { *semantic action*_n }

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Writing a Grammar in Yacc

- ⌘ Productions in Yacc are of the form

$$\begin{aligned} \textit{Nonterminal} & : \textit{tokens/nonterminals} \{ \\ \textit{action} & \} \\ & | \textit{tokens/nonterminals} \{ \textit{action} \} \\ & \dots \\ & ; \end{aligned}$$
- ⌘ Tokens that are single characters can be used directly within productions, e.g. '+'
- ⌘ Named tokens must be declared first in the declaration part using

$$\%token \textit{TokenName}$$

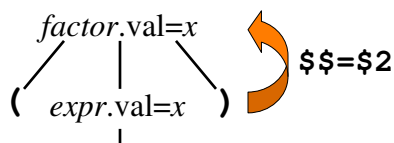
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Synthesized Attributes

- ⌘ Semantic actions may refer to values of the *synthesized attributes* of terminals and nonterminals in a production:

$$X : Y_1 Y_2 Y_3 \dots Y_n \{ \textit{action} \}$$
 - ☒ \$\$ refers to the value of the attribute of X
 - ☒ \$i refers to the value of the attribute of Y_i
- ⌘ For example

$$\textit{factor} : \textit{'(' expr ')' } \{ \textit{\$\$=\$2; } \}$$



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Example 1

```

%{ #include <ctype.h> %}
%token DIGIT
%%
line : expr '\n'      { printf("%d\n", $1); }
;
expr : expr '+' term  { $$ = $1 + $3; }
    | term            { $$ = $1; }
;
term : term '*' factor { $$ = $1 * $3; }
    | factor          { $$ = $1; }
;
factor : '(' expr ')' { $$ = $2; }
      | DIGIT        { $$ = $1; }
;
%%
int yylex()
{ int c = getchar();
  if (isdigit(c))
  { yylval = c-'0';
    return DIGIT;
  }
  return c;
}

```

Also results in definition of `#define DIGIT xxx`

Attribute of **term** (parent)

Attribute of **factor** (child)

Attribute of token (stored in **yylval**)

Example of a very crude lexical analyzer invoked by the parser

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Dealing With Ambiguous Grammars

- ⌘ By defining operator precedence levels and left/right associativity of the operators, we can specify ambiguous grammars in Yacc, such as $E \rightarrow E+E \mid E-E \mid E^*E \mid E/E \mid (E) \mid -E \mid \text{num}$
- ⌘ To define precedence levels and associativity in Yacc's declaration part:


```

%left '+' '-'
%left '*' '/'
%right UMINUS

```

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Example 2

```
%{
#include <ctype.h>
#include <stdio.h>
#define YYSTYPE double
%}
%token NUMBER
%left '+' '-'
%left '*' '/'
%right UMINUS
%%
lines : lines expr '\n'      { printf("%g\n", $2); }
      | lines '\n'
      | /* empty */
      ;
expr  : expr '+' expr      { $$ = $1 + $3; }
      | expr '-' expr      { $$ = $1 - $3; }
      | expr '*' expr      { $$ = $1 * $3; }
      | expr '/' expr      { $$ = $1 / $3; }
      | '(' expr ')'       { $$ = $2; }
      | '-' expr %prec UMINUS { $$ = -$2; }
      | NUMBER
      ;
%%
```

Double type for attributes
and `yylval`

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Example 2 (cont'd)

```
%%
int yylex()
{ int c;
  while ((c = getchar()) == '\n')
    ;
  if ((c == '.') || isdigit(c))
  { ungetc(c, stdin);
    scanf("%lf", &yylval);
    return NUMBER;
  }
  return c;
}
int main()
{ if (yyparse() != 0)
  { fprintf(stderr, "Abnormal exit\n");
    return 0;
  }
}
int yyerror(char *s)
{ fprintf(stderr, "Error: %s\n", s);
}
}
```

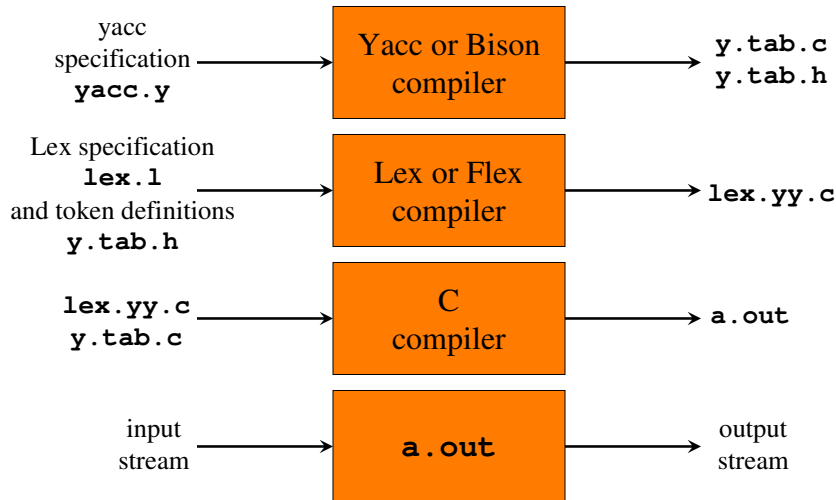
Crude lexical analyzer for
fp doubles and arithmetic
operators

Run the parser

Invoked by parser
to report parse errors

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Combining Lex/Flex with Yacc/Bison



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Lex Specification for Example 2

```

%option noyywrap
%{
#include "y.tab.h"
extern double yylval;
%}
number [0-9]+\.[0-9]*|[0-9]*\.[0-9]+
%%
[ ]          { /* skip blanks */ }
{number}    { sscanf(yytext, "%lf", &yylval);
              return NUMBER;
            }
\n|.        { return yytext[0]; }
  
```

Generated by Yacc, contains #define NUMBER xxx

Defined in y.tab.c

```

yacc -d example2.y
lex example2.l
gcc y.tab.c lex.yy.c
./a.out
  
```

```

bison -d -y example2.y
flex example2.l
gcc y.tab.c lex.yy.c
./a.out
  
```

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Error Recovery in Yacc

```
%{
...
}%
...
%%
lines : lines expr '\n'      { printf("%g\n", $2; }
      | lines '\n'
      | /* empty */
      | error '\n'
...
;

```

Error production:
set error mode and
skip input until newline

```
{ yyerror("reenter last line: ");
  yyerrok;
}
```

Reset parser to normal mode

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Intermediate Code Generation



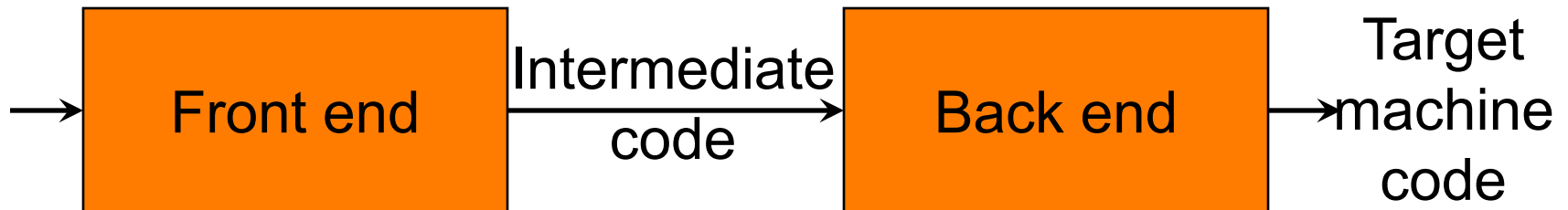
Bart Kienhuis
Computer Systems Group
University Leiden (LIACS)

The Phases of a Compiler

Phase	Output	Sample
<i>Programmer</i>	Source string	<code>A=B+C;</code>
<i>Scanner</i> (performs <i>lexical analysis</i>)	Token string	<code>'A', '=', 'B', '+', 'C', ';'</code> And <i>symbol table</i> for identifiers
<i>Parser</i> (performs <i>syntax analysis</i> based on the grammar of the programming language)	Parse tree or abstract syntax tree	<pre> ; = / \ A + / \ B C </pre>
<i>Semantic analyzer</i> (type checking, etc)	Parse tree or abstract syntax tree	
<i>Intermediate code generator</i>	Three-address code, quads, or RTL	<pre> int2fp B t1 + t1 C t2 := t2 A </pre>
<i>Optimizer</i>	Three-address code, quads, or RTL	<pre> int2fp B t1 + t1 #2.3 A </pre>
<i>Code generator</i>	Assembly code	<pre> MOVE #2.3, r1 ADDF2 r1, r2 MOVE r2, A </pre>
<i>Peephole optimizer</i>	Assembly code	<pre> ADDF2 #2.3, r2 MOVE r2, A </pre>

Intermediate Code Generation

- ⌘ Facilitates *retargeting*: enables attaching a back end for the new machine to an existing front end



- ⌘ Enables machine-independent code optimization

Intermediate Representations

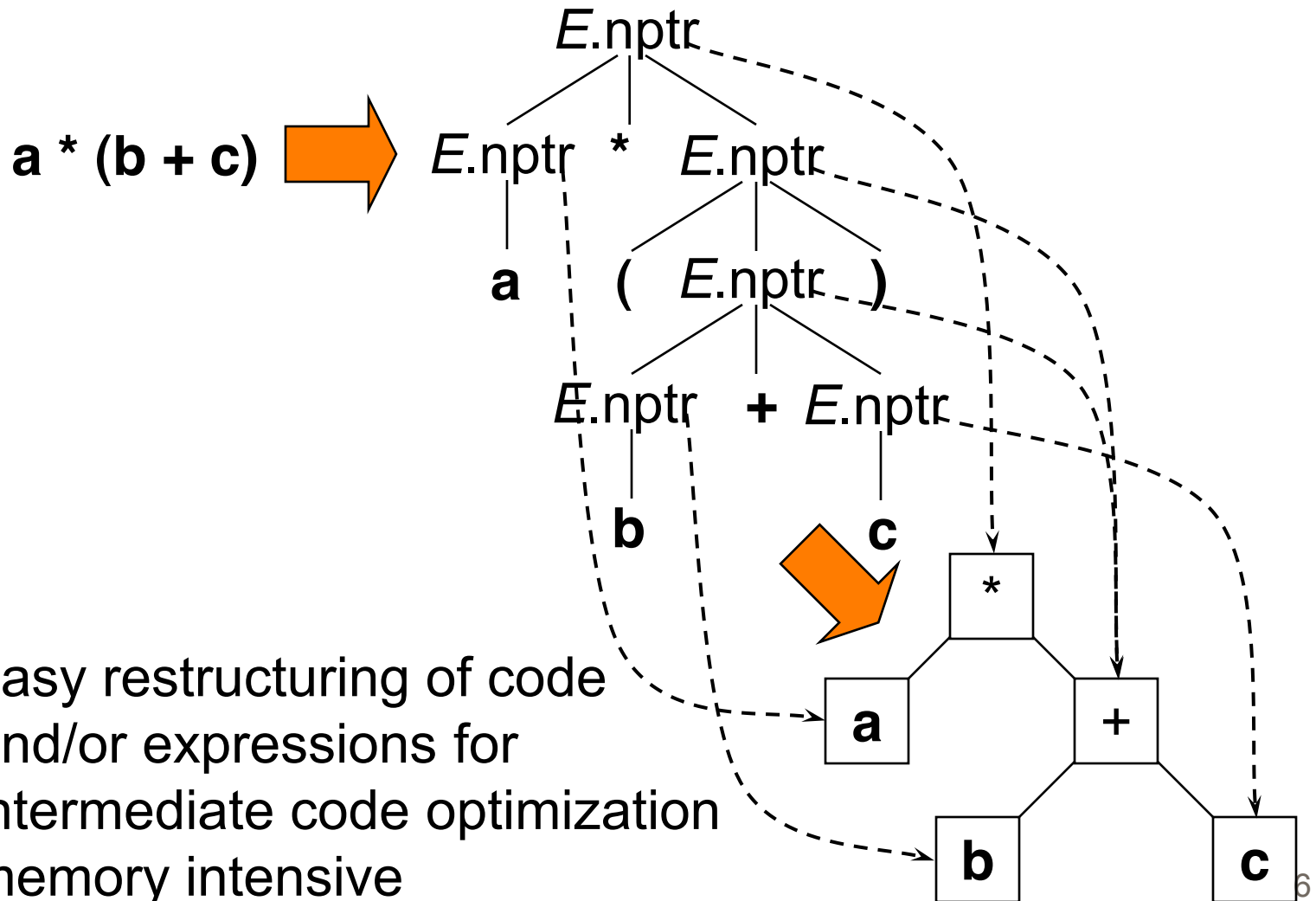
- ⌘ *Graphical representations* (e.g. AST)
- ⌘ *Postfix notation*: operations on values stored on operand stack (similar to JVM bytecode)
- ⌘ *Three-address code*: (e.g. *triples* and *quads*)
$$x := y \text{ op } z$$
- ⌘ *Two-address code*:
$$x := \text{op } y$$

which is the same as $x := x \text{ op } y$

Syntax-Directed Translation of Abstract Syntax Trees

Production	Semantic Rule
$S \rightarrow \mathbf{id} := E$	$S.nptr := mknnode(':=', mkleaf(\mathbf{id}, \mathbf{id}.entry), E.nptr)$
$E \rightarrow E_1 + E_2$	$E.nptr := mknnode('+', E_1.nptr, E_2.nptr)$
$E \rightarrow E_1 * E_2$	$E.nptr := mknnode('*', E_1.nptr, E_2.nptr)$
$E \rightarrow - E_1$	$E.nptr := mknnode('uminus', E_1.nptr)$
$E \rightarrow (E_1)$	$E.nptr := E_1.nptr$
$E \rightarrow \mathbf{id}$	$E.nptr := mkleaf(\mathbf{id}, \mathbf{id}.entry)$

Abstract Syntax Trees

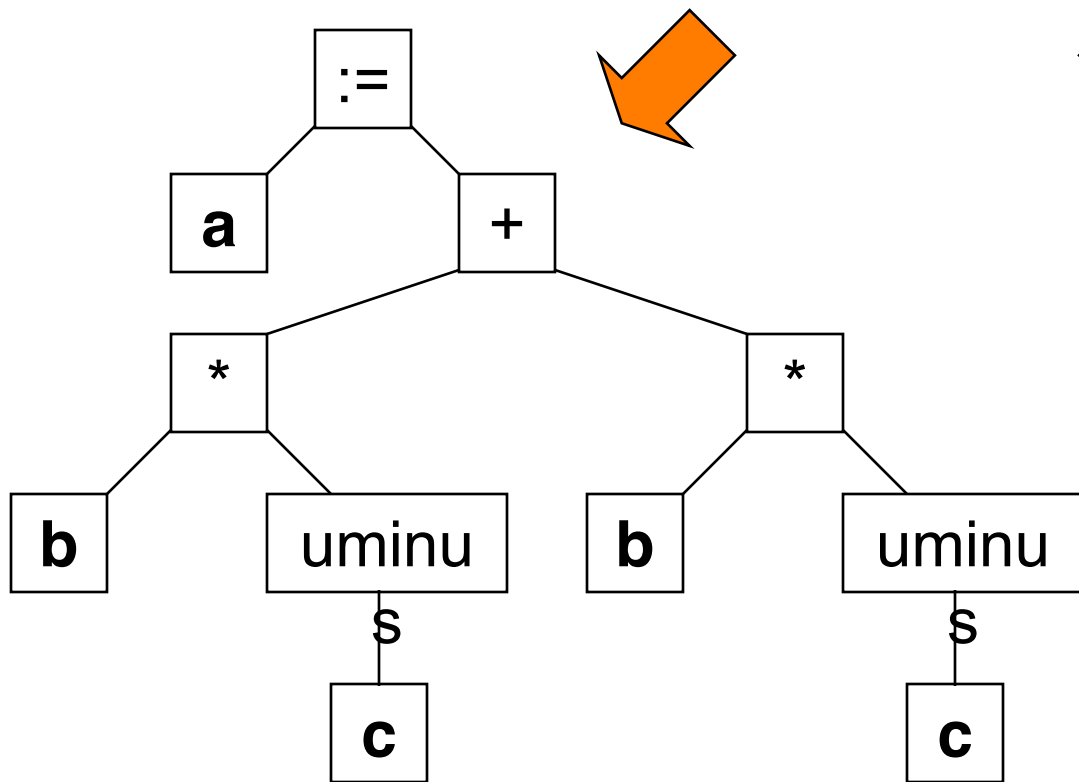


Pro: easy restructuring of code
and/or expressions for
intermediate code optimization

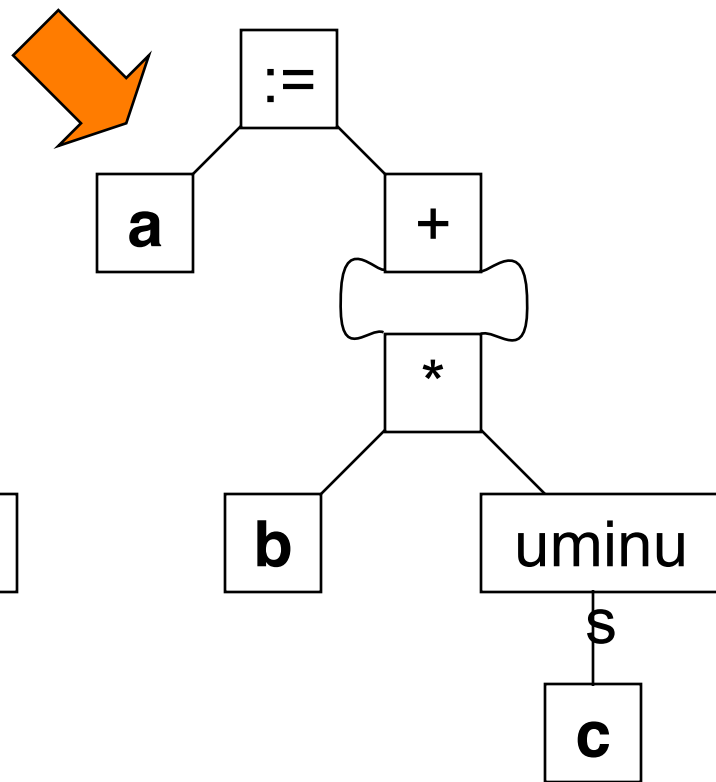
Cons: memory intensive

Abstract Syntax Trees versus DAGs

$a := b * -c + b * -c$



Tree



DAG

Postfix Notation

$a := b * -c + b * -c$



a b c uminus * b c uminus * + assign Bytecode (for example)

Postfix notation represents operations on a stack

- Pro: easy to generate
- Cons: stack operations are more difficult to optimize

```
iload 2      // push b
iload 3      // push c
ineg        // uminus
imul        // *
iload 2      // push b
iload 3      // push c
ineg        // uminus
imul        // *
iadd        // +
istore 1     // store a
```

Three-Address Code

$a := b * -c + b * -c$



```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Linearized representation
of a syntax tree

```
t1 := - c
t2 := b * t1
t5 := t2 + t2
a := t5
```

Linearized representation
of a syntax DAG

Three-Address Statements

- ⌘ Assignment statements: $x := y \text{ op } z, x := \text{op } y$
- ⌘ Indexed assignments: $x := y[i], x[i] := y$
- ⌘ Pointer assignments: $x := \&y, x := *y, *x := y$
- ⌘ Copy statements: $x := y$
- ⌘ Unconditional jumps: **goto** *lab*
- ⌘ Conditional jumps: **if** $x \text{ relop } y$ **goto** *lab*
- ⌘ Function calls: **param** $x\dots$ **call** p, n
return y

Syntax-Directed Translation into Three-Address Code

Productions

$S \rightarrow \text{id} := E$
| **while** E **do** S
 $E \rightarrow E + E$
| $E * E$
| $- E$
| (E)
| **id**
| **num**

Synthesized attributes:

$S.code$ three-address code for
 $S.begin$ label to start of S or nil
 $S.after$ label to end of S or nil
 $E.code$ three-address code for
 $E.place$ a name holding the value

$gen(E.place \text{ ':=' } E_1.place \text{ '+' } E_2.place)$

Code generation \rightarrow $t3 := t1 + t2$

Syntax-Directed Translation into Three-Address Code (cont'd)

Productions	Semantic rules
$S \rightarrow \mathbf{id} := E$	$S.code := E.code \parallel gen(\mathbf{id.place} := E.place); S.begin := S.after$
$S \rightarrow \mathbf{while} E$ $\mathbf{do} S_1$	(see next slide)
$E \rightarrow E_1 + E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place := E_1.place + E_2.place)$
$E \rightarrow E_1 * E_2$	$E.place := newtemp();$ $E.code := E_1.code \parallel E_2.code \parallel gen(E.place := E_1.place * E_2.place)$
$E \rightarrow - E_1$	$E.place := newtemp();$ $E.code := E_1.code \parallel gen(E.place := 'uminus' E_1.place)$
$E \rightarrow (E_1)$	$E.place := E_1.place$ $E.code := E_1.code$
$E \rightarrow \mathbf{id}$	$E.place := \mathbf{id.name}$ $E.code := ''$
$E \rightarrow \mathbf{num}$	$E.place := newtemp();$ $E.code := gen(E.place := \mathbf{num.value})$

Syntax-Directed Translation into Three-Address Code (cont'd)

Production

$S \rightarrow \text{while } E \text{ do } S_1$

Semantic rule

$S.\text{begin} := \text{newlabel}()$

$S.\text{after} := \text{newlabel}()$

$S.\text{code} := \text{gen}(S.\text{begin} ':') \parallel$

$E.\text{code} \parallel$

$\text{gen}(\text{'if' } E.\text{place} \text{'=' '0' 'goto' } S.\text{after}) \parallel$

$S_1.\text{code} \parallel$

$\text{gen}(\text{'goto' } S.\text{begin}) \parallel$

$\text{gen}(S.\text{after} ':')$

$S.\text{begin}:$

$E.\text{code}$

$\text{if } E.\text{place} = 0 \text{ goto}$

$S.\text{after}$
 $S.\text{code}$

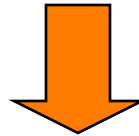
$\text{goto } S.\text{begin}$

$S.\text{after}:$

...

Example

```
i := 2 * n + k
while i do
  i := i - k
```



```
t1 := 2
t2 := t1 * n
t3 := t2 + k
i := t3
L1: if i = 0 goto L2
    t4 := i - k
    i := t4
    goto L1
L2:
```

Implementation of Three-Address Statements: Quads

<i>#</i>	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>	<i>Res</i>
(0)	uminus	c		t1
(1)	*	b	t1	t2
(2)	uminus	c		t3
(3)	*	b	t3	t4
(4)	+	t2	t4	t5
(5)	Quads (quadruples)			a

Pro: easy to rearrange code for global optimization

Cons: lots of temporaries

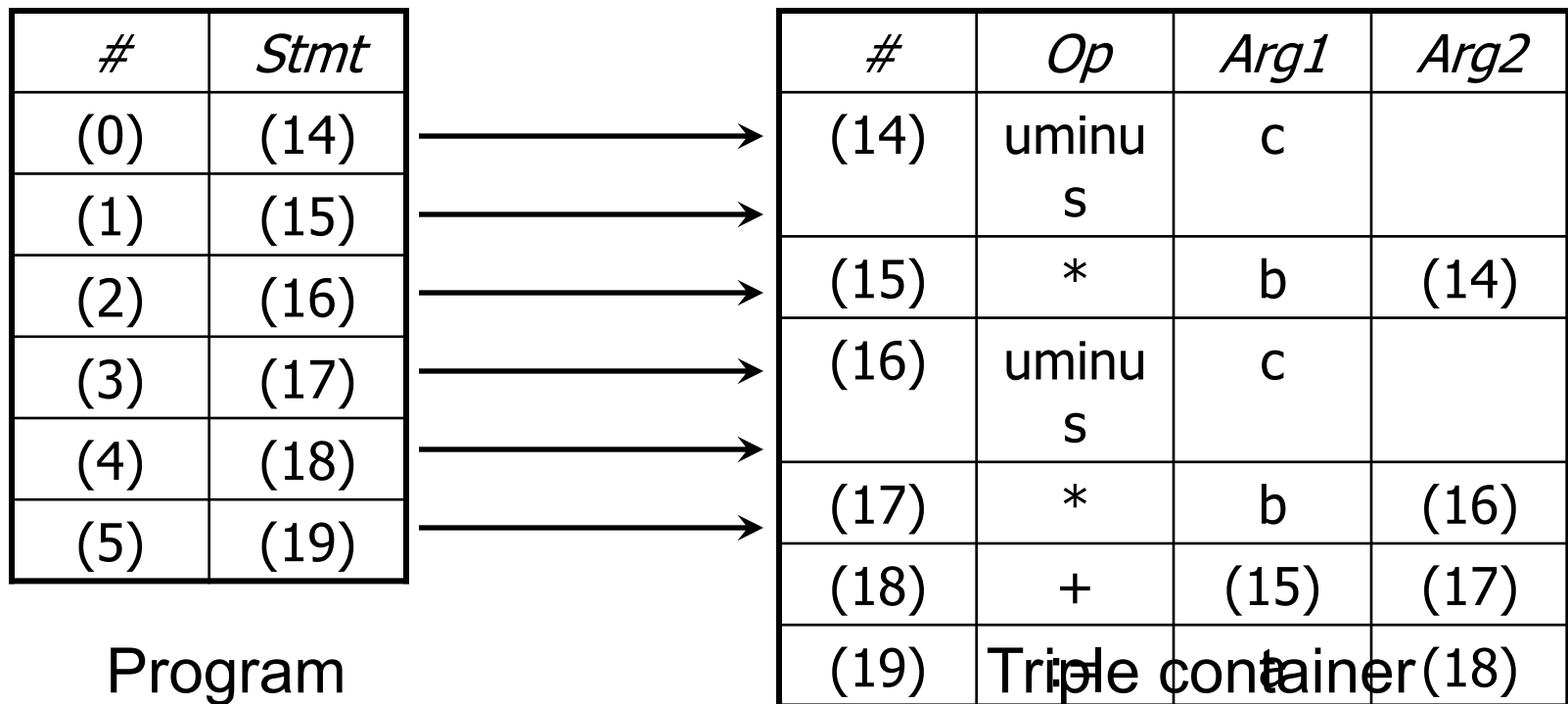
Implementation of Three-Address Statements: Triples

<i>#</i>	<i>Op</i>	<i>Arg1</i>	<i>Arg2</i>
(0)	uminu s	c	
(1)	*	b	(0)
(2)	uminu s	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	:=	Tripl _a	(4)

Pro: temporaries are implicit

Cons: difficult to rearrange code

Implementation of Three-Address Stmts: Indirect Triples



Pro: temporaries are implicit & easier to rearrange code

Names and Scopes



- ⌘ The three-address code generated by the syntax-directed definitions shown on the previous slides is somewhat simplistic, because it assumes that the names of variables can be easily resolved by the back end in global or local variables
- ⌘ We need local symbol tables to record global declarations as well as local declarations in procedures, blocks, and structs to resolve names

Symbol Tables for Scoping

```
struct S  
{ int a;  
  int b;  
} s;
```

We need a symbol table
for the *fields* of struct S

```
void swap(int& a, int& b)  
{ int t;  
  t = a;  
  a = b;  
  b = t;  
}
```

Need symbol table
for *global* variables
and functions

```
void somefunc()  
{ ...  
  swap(s.a, s.b);  
  ...  
}
```

Need symbol table for *arguments*
and *locals* for each function

Check: **s** is global and has fields **a** and **b**
Using symbol tables we can generate
code to access **s** and its fields

Offset and Width for Runtime Allocation

```
struct S
{ int a;
  int b;
} s;
```

The fields `a` and `b` of struct `S` are located at *offsets* 0 and 4 from the start of `S`

```
void swap(int& a, int& b)
{ int t;
  t = a;
  a = b;
  b = t;
}
```

The *width* of `S` is 8

<code>a</code>	(0)
<code>b</code>	(4)

Subroutine frame holds arguments `a` and `b` and local `t` at *offsets* 0, 4, and 8

```
void somefunc ()
{ ...
  swap(s.a, s.b);
  ...
}
```

The *width* of the frame is 12

Subroutine frame

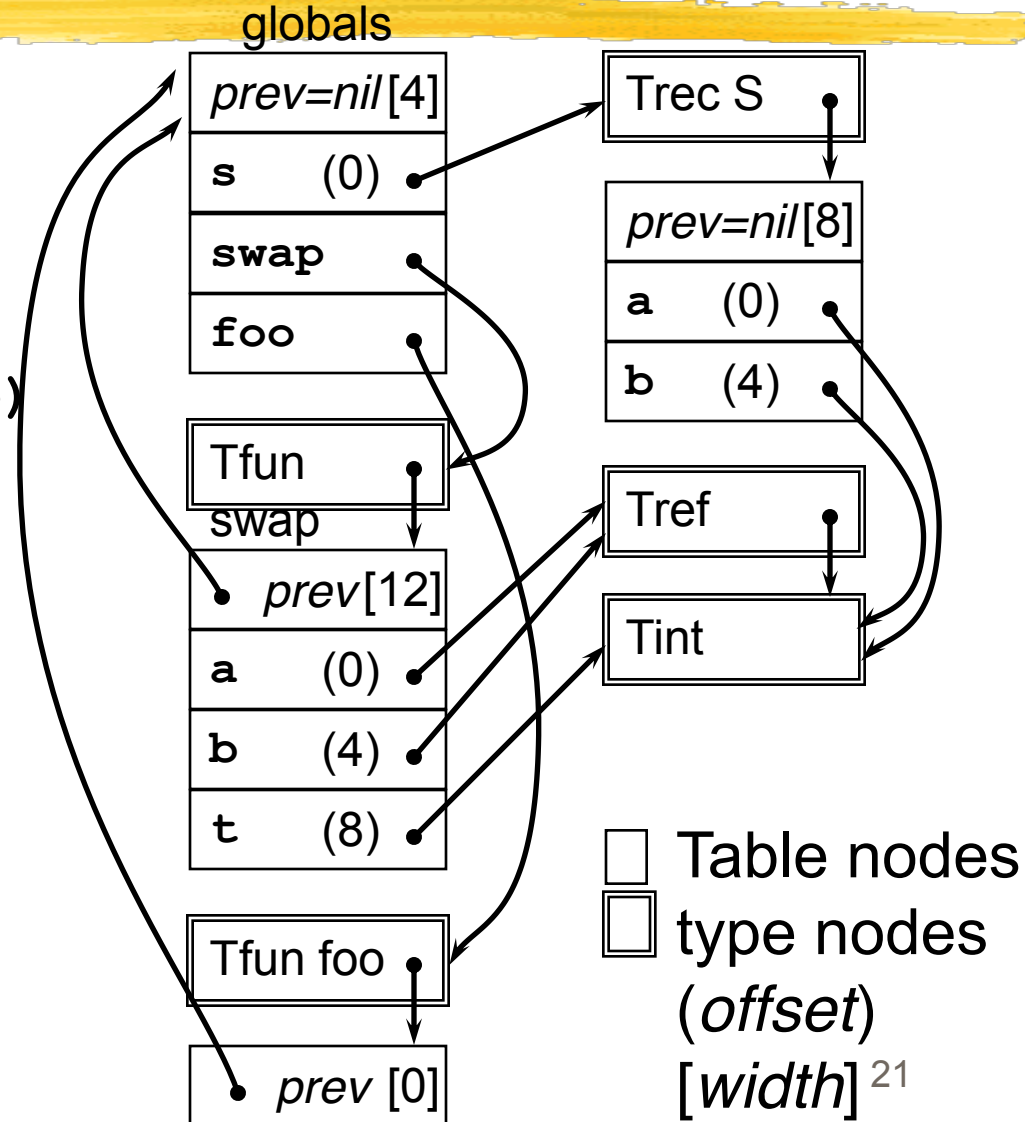
<code>fp[0]=</code>	<code>a</code>	(0)
<code>fp[4]=</code>	<code>b</code>	(4)
<code>fp[8]=</code>	<code>t</code>	(8)

Example

```
struct S
{ int a;
  int b;
} s;
```

```
void swap(int& a, int& b)
{ int t;
  t = a;
  a = b;
  b = t;
}
```

```
void foo()
{ ...
  swap(s.a, s.b);
  ...
}
```



Hierarchical Symbol Table Operations



- ⌘ *mktable(previous)* returns a pointer to a new table that is linked to a previous table in the outer scope
- ⌘ *enter(table, name, type, offset)* creates a new entry in *table*
- ⌘ *addwidth(table, width)* accumulates the total width of all entries in *table*
- ⌘ *enterproc(table, name, newtable)* creates a new entry in *table* for procedure with local scope *newtable*
- ⌘ *lookup(table, name)* returns a pointer to the entry in the table for *name* by following linked tables

Syntax-Directed Translation of Declarations in Scope

Productions

$P \rightarrow D ; S$

$D \rightarrow D ; D$

| **id** : T

| **proc id** ; D ; S

$T \rightarrow$ **integer**

| **real**

| **array** [**num**] **of** T

| $^ T$

| **record** D **end**

$S \rightarrow S ; S$

| **id** := E

| **call id** (A)

Productions (*cont'd*)

$E \rightarrow E + E$

| $E * E$

| $- E$

| (E)

| **id**

| $E ^$

| **&** E

| $E . \mathbf{id}$

$A \rightarrow A , E$

| E

Synthesized attributes:

$T.type$ pointer to type

$T.width$ storage width of type (bytes)

$E.place$ name of temp holding value of

Global data to implement scoping:

$tblptr$ stack of pointers to tables

$offset$ stack of offset values

Syntax-Directed Translation of Declarations in Scope (cont'd)

$P \rightarrow \{ t := mktable(nil); push(t, tblptr); push(0, offset) \}$
 $D ; S$

$D \rightarrow \mathbf{id} : T$
 $\{ enter(top(tblptr), \mathbf{id.name}, T.type, top(offset));$
 $top(offset) := top(offset) + T.width \}$

$D \rightarrow \mathbf{proc id} ;$
 $\{ t := mktable(top(tblptr)); push(t, tblptr); push(0, offset);$
 $D_1 ; S$
 $\{ t := top(tblptr); addwidth(t, top(offset));$
 $pop(tblptr); pop(offset);$
 $enterproc(top(tblptr), \mathbf{id.name}, t) \}$

$D \rightarrow D_1 ; D_2$

Syntax-Directed Translation of Declarations in Scope (cont'd)

$T \rightarrow \text{integer} \{ T.type := 'integer'; T.width := 4 \}$

$T \rightarrow \text{real} \{ T.type := 'real'; T.width := 8 \}$

$T \rightarrow \text{array [num] of } T_1$
 $\{ T.type := \text{array}(\text{num.val}, T_1.type);$
 $T.width := \text{num.val} * T_1.width \}$

$T \rightarrow \wedge T_1$
 $\{ T.type := \text{pointer}(T_1.type); T.width := 4 \}$

$T \rightarrow \text{record}$
 $\{ t := \text{mktable}(\text{nil}); \text{push}(t, \text{tblptr}); \text{push}(0, \text{offset}) \}$

D end

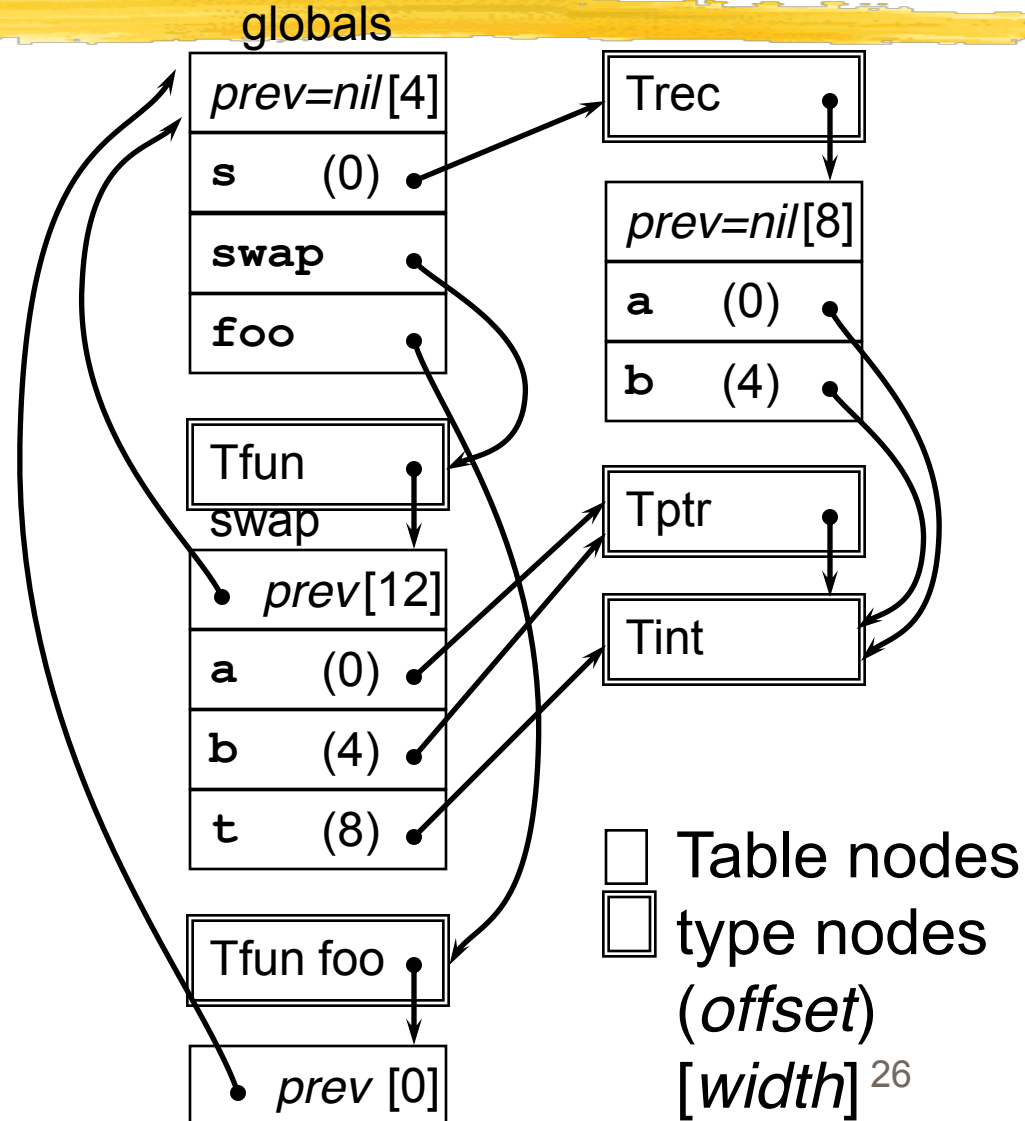
$\{ T.type := \text{record}(\text{top}(\text{tblptr})); T.width := \text{top}(\text{offset});$
 $\text{addwidth}(\text{top}(\text{tblptr}), \text{top}(\text{offset})); \text{pop}(\text{tblptr}); \text{pop}(\text{offset}) \}$

Example

```
s: record
  a: integer;
  b: integer;
end;
```

```
proc swap;
  a: ^integer;
  b: ^integer;
  t: integer;
  t := a^;
  a^ := b^;
  b^ := t;
```

```
proc foo;
  call swap(&s.a, &s.b);
```



Syntax-Directed Translation of Statements in Scope

$S \rightarrow S ; S$

$S \rightarrow \text{id} := E$

{ $p := \text{lookup}(\text{top}(\text{tblptr}), \text{id.name});$

if $p = \text{nil}$ **then**

error()

else if $p.\text{level} = 0$ **then** // *global variable*

emit(id.place ':=' E.place)

else // *local variable in subroutine frame*

emit(fp[p.offset] ':=' E.place) }

Globals

s	(0)
x	(8)
y	(12)

Subroutine
frame

fp[0]=	a	(0)
fp[4]=	b	(4)
fp[8]=	t	(8)

...

Syntax-Directed Translation of Expressions in Scope

$E \rightarrow E_1 + E_2$ { $E.place := newtemp();$
 $emit(E.place := E_1.place + E_2.place)$ }

$E \rightarrow E_1 * E_2$ { $E.place := newtemp();$
 $emit(E.place := E_1.place * E_2.place)$ }

$E \rightarrow - E_1$ { $E.place := newtemp();$
 $emit(E.place := 'uminus' E_1.place)$ }

$E \rightarrow (E_1)$ { $E.place := E_1.place$ }

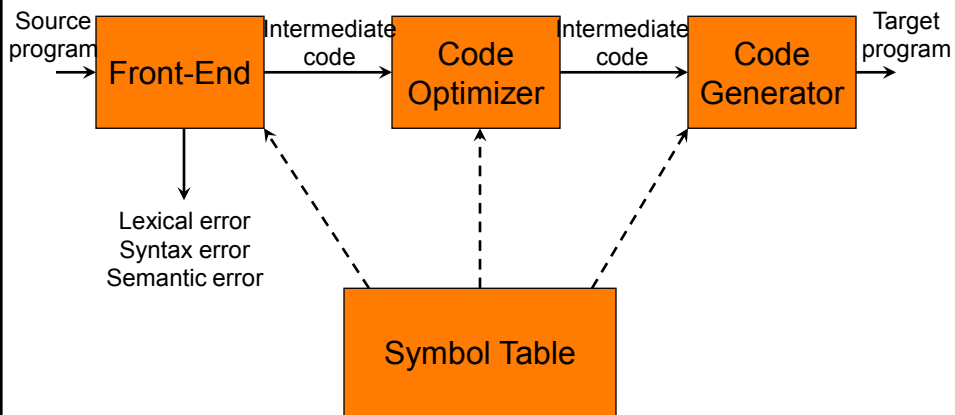
$E \rightarrow id$ { $p := lookup(top(tblptr), id.name);$
if $p = nil$ **then** $error()$
else if $p.level = 0$ **then** // global variable
 $E.place := id.place$
else // local variable in frame
 $E.place := fp[p.offset]$ }

Code Generation

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1

Position of a Code Generator in the Compiler Model



2

Code Generation

- ⌘ Code produced by compiler must be correct
 - ☒ Source to target program transformation is *semantics preserving*
- ⌘ Code produced by compiler should be of high quality
 - ☒ Effective use of target machine resources
 - ☒ Heuristic techniques can generate good but suboptimal code, because generating optimal code is undecidable

3

Target Program Code

- ⌘ The back-end code generator of a compiler may generate different forms of code, depending on the requirements:
 - ☒ Absolute machine code (executable code)
 - ☒ Relocatable machine code (object files for linker)
 - ☒ Assembly language (facilitates debugging)
 - ☒ Byte code forms for interpreters (e.g. JVM)

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The Target Machine

- ⌘ Implementing code generation requires thorough understanding of the target machine architecture and its instruction set
- ⌘ Our (hypothetical) machine:
 - ☒ Byte-addressable (word = 4 bytes)
 - ☒ Has n general purpose registers R_0, R_1, \dots, R_{n-1}
 - ☒ Two-address instructions of the form

op source, destination

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The Target Machine: Op-codes and Address Modes

- ⌘ Op-codes (op), for example
 - MOV** (move content of *source* to *destination*)
 - ADD** (add content of *source* to *destination*)
 - SUB** (subtract content of *source* from *dest.*)
- ⌘ Address modes

Mode	Form	Address	Added Cost
Absolute	M	M	1
Register	R	R	0
Indexed	$c(\mathbf{R})$	$c + \text{contents}(\mathbf{R})$	1
Indirect register	$*\mathbf{R}$	$\text{contents}(\mathbf{R})$	0
Indirect indexed	$*c(\mathbf{R})$	$\text{contents}(c + \text{contents}(\mathbf{R}))$	1
Literal	#C	N/A	1

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Instruction Costs

- ⌘ Machine is a simple, non-super-scalar processor with fixed instruction costs
- ⌘ Realistic machines have deep pipelines, I-cache, D-cache, etc.
- ⌘ Define the cost of instruction
 $= 1 + \text{cost}(\textit{source-mode}) + \text{cost}(\textit{destination-mode})$

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Examples

Instruction	Operation	Cost
MOV R0 , R1	Store <i>content</i> (R0) into register R1	
MOV R0 , M	Store <i>content</i> (R0) into memory location M	
MOV M , R0	Store <i>content</i> (M) into register R0	2
MOV 4 (R0) , M	Store <i>contents</i> (4+ <i>contents</i> (R0)) into M	3
MOV *4 (R0) , M	Store <i>contents</i> (<i>contents</i> (4+ <i>contents</i> (R0))) into M	3
MOV #1 , R0	Store 1 into R0	2
ADD 4 (R0) , *12 (R1)	Add <i>contents</i> (4+ <i>contents</i> (R0)) to <i>contents</i> (12+ <i>contents</i> (R1))	3

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Instruction Selection

⌘ Instruction selection is important to obtain efficient code

⌘ Suppose we translate three-address code

$X := Y + Z$

to: `MOV Y, R0`
`ADD Z, R0`
`MOV R0, X`

$a := a + 1$  `MOV a, R0`
`ADD #1, R0`
`MOV R0, a`
Cost = 6

Better



`ADD #1, a`
Cost = 3

Better



`INC a`
Cost = 2

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Instruction Selection: Utilizing Addressing Modes

⌘ Suppose we translate $a := b + c$ into

`MOV b, R0`
`ADD c, R0`
`MOV R0, a`

⌘ Assuming addresses of a , b , and c are stored in $R0$, $R1$, and $R2$

`MOV *R1, *R0`
`ADD *R2, *R0`

⌘ Assuming $R1$ and $R2$ contain values of b and c

`ADD R2, R1`
`MOV R1, a`

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Need for Global Machine-Specific Code Optimizations

⌘ Suppose we translate three-address code

$x := y + z$

to: `MOV y, R0`
`ADD Z, R0`
`MOV R0, X`

⌘ Then, we translate

$a := b + c$

$d := a + e$

to: `MOV a, R0`
`ADD b, R0`
`MOV R0, a`
`MOV a, R0`
`ADD e, R0`
`MOV R0, d`

Redundant



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Register Allocation and Assignment

⌘ Efficient utilization of the limited set of registers is important to generate good code

⌘ Registers are assigned by

☒ *Register allocation* to select the set of variables that will reside in registers at a point in the code

☒ *Register assignment* to pick the specific register that a variable will reside in

⌘ Finding an optimal register assignment in general is NP-complete

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Example

```
t:=a+b
t:=t*c
t:=t/d
```

↓ { R1=t }

```
MOV a,R1
ADD b,R1
MUL c,R1
DIV d,R1
MOV R1,t
```

```
t:=a*b
t:=t+a
t:=t/d
```

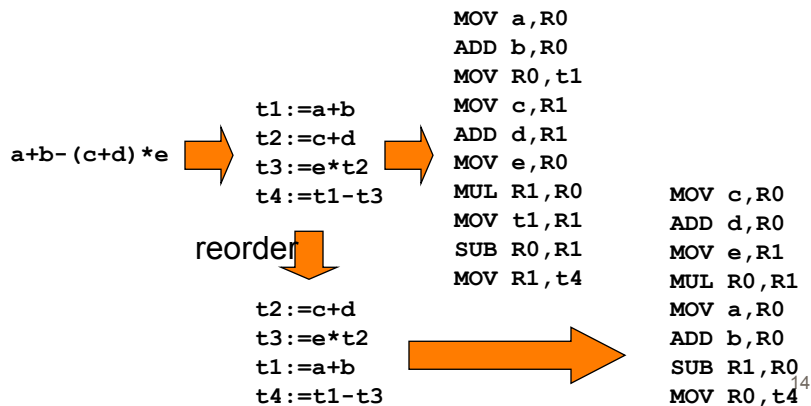
↓ { R0=a, R1=t }

```
MOV a,R0
MOV R0,R1
MUL b,R1
ADD R0,R1
DIV d,R1
MOV R1,t
```

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Choice of Evaluation Order

⌘ When instructions are independent, their evaluation order can be changed



Generating Code for Stack Allocation of Activation Records

<code>t1 := a + b</code>	<code>100: ADD #16,SP</code>	Push frame
<code>param t1</code>	<code>108: MOV a,R0</code>	
<code>param c</code>	<code>116: ADD b,R0</code>	
<code>t2 := call foo,2</code>	<code>124: MOV R0,4(SP)</code>	Store a+b
<code>...</code>	<code>132: MOV c,8(SP)</code>	Store c
	<code>140: MOV #156,*SP</code>	Store return address
	<code>148: GOTO 500</code>	Jump to foo
<code>func foo</code>	<code>156: MOV 12(SP),R0</code>	Get return value
<code>...</code>	<code>164: SUB #16,SP</code>	Remove frame
<code>return t1</code>	<code>172: ...</code>	
	<code>500: ...</code>	
	<code>564: MOV R0,12(SP)</code>	Store return value
	<code>572: GOTO *SP</code>	Return to caller

Note: Language and machine dependent
Here we assume C-like implementation with SP and no FP

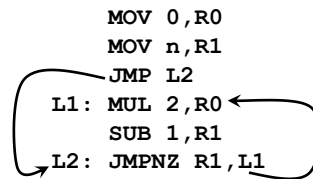
Code Generation Part 2

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Flow Graphs

- ⌘ A *flow graph* is a graphical depiction of a sequence of instructions with control flow edges
- ⌘ A flow graph can be defined at the intermediate code level or target code level

```
MOV 1,R0
MOV n,R1
JMP L2
L1: MUL 2,R0
SUB 1,R1
L2: JMPNZ R1,L1
```



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Basic Blocks

- ⌘ A *basic block* is a sequence of consecutive instructions with exactly one entry point and one exit point (with natural flow or a branch instruction)

```
MOV 1,R0
MOV n,R1
JMP L2
L1: MUL 2,R0
SUB 1,R1
L2: JMPNZ R1,L1
```



```
MOV 1,R0
MOV n,R1
JMP L2
```

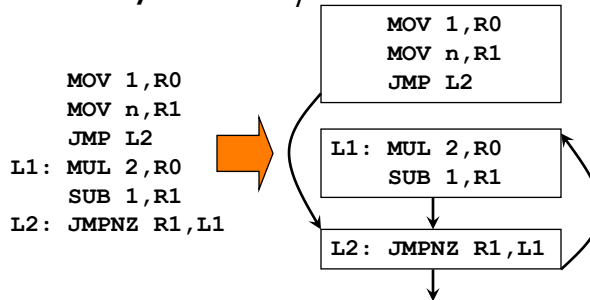
```
L1: MUL 2,R0
SUB 1,R1
```

```
L2: JMPNZ R1,L1
```

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Basic Blocks and Control Flow Graphs

⌘ A *control flow graph* (CFG) is a directed graph with basic blocks B_i as vertices and with edges $B_i \rightarrow B_j$ iff B_j can be executed immediately after B_i .

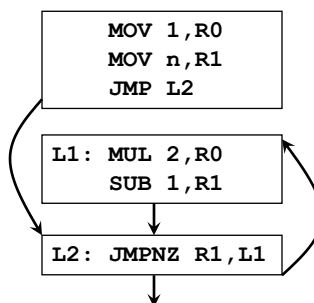


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Successor and Predecessor Blocks

⌘ Suppose the CFG has an edge $B_1 \rightarrow B_2$

- ⊞ Basic block B_1 is a *predecessor* of B_2
- ⊞ Basic block B_2 is a *successor* of B_1



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Partition Algorithm for Basic Blocks

Input: A sequence of three-address statements

Output: A list of basic blocks with each three-address statement in exactly one block

1. Determine the set of *leaders*, the first statements of basic blocks
 - a) The first statement is the leader
 - b) Any statement that is the target of a goto is a leader
 - c) Any statement that immediately follows a goto is a leader
2. For each leader, its basic block consists of the leader and all statements up to but not including the next leader or the end of the program

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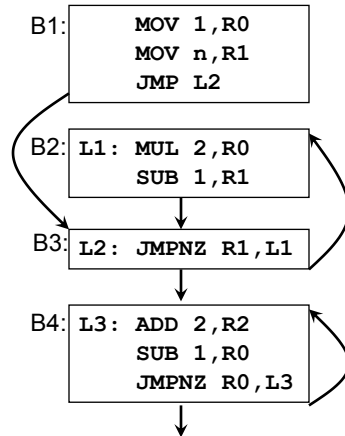
Loops

⌘ A *loop* is a collection of basic blocks, such that

- ☒ All blocks in the collection are *strongly connected*
- ☒ The collection has a unique *entry*, and the only way to reach a block in the loop is through the entry

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Loops (Example)



Strongly connected components:

SCC={ {B2,B3},
{B4} }

Entries:
B3, B4

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Equivalence of Basic Blocks

⌘ Two basic blocks are (semantically) *equivalent* if they compute the same set of expressions

```

b := 0
t1 := a + b
t2 := c * t1
a := t2
  
```

↓

```

a := c*a
b := 0
  
```

```

a := c * a
b := 0
  
```

↓

```

a := c*a
b := 0
  
```

Blocks are equivalent, assuming $t1$ and $t2$ are *dead*: no longer used (no longer live)

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Transformations on Basic Blocks

- ⌘ A *code-improving transformation* is a code optimization to improve speed or reduce code size
- ⌘ *Global transformations* are performed across basic blocks
- ⌘ *Local transformations* are only performed on single basic blocks
- ⌘ Transformations must be safe and preserve the meaning of the code
 - ☒ A local transformation is safe if the transformed basic block is guaranteed to be equivalent to its original form

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Common-Subexpression Elimination

- ⌘ Remove redundant computations

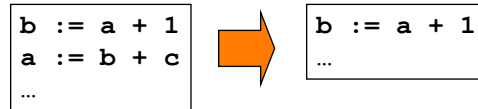
a := b + c	→	a := b + c
b := a - d		b := a - d
c := b + c		c := b + c
d := a - d		d := b

t1 := b * c	→	t1 := b * c
t2 := a - t1		t2 := a - t1
t3 := b * c		t4 := t2 + t1
t4 := t2 + t3		

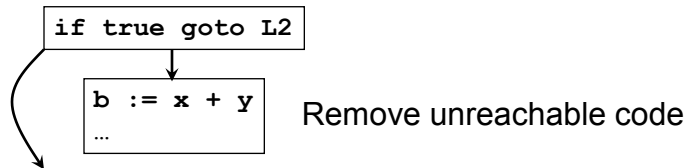
26

Dead Code Elimination

⌘ Remove unused statements



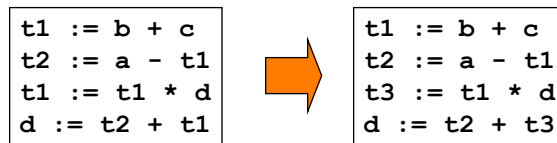
Assuming *a* is *dead* (not used)



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Renaming Temporary Variables

⌘ Temporary variables that are dead at the end of a block can be safely renamed

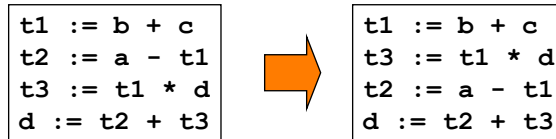


Normal-form block

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Interchange of Statements

⌘ Independent statements can be reordered



Note that normal-form blocks permit all statement interchanges that are possible

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Algebraic Transformations

⌘ Change arithmetic operations to transform blocks to algebraic equivalent forms



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Next-Use

- ⌘ Next-use information is needed for dead-code elimination and register assignment
- ⌘ Next-use is computed by a backward scan of a basic block and performing the following actions on statement

$i: x := y \text{ op } z$

- ☒ Add liveness/next-use info on x , y , and z to statement i
- ☒ Set x to "not live" and "no next use"
- ☒ Set y and z to "live" and the next uses of y and z to i

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Next-Use (Step 1)

$i: a := b + c$

$j: t := a + b$ [$live(a) = true, live(b) = true, live(t) = true,$
 $nextuse(a) = none, nextuse(b) = none, nextuse(t) = none$]

Attach current live/next-use information
Because info is empty, assume variables are live
(Data flow analysis Ch.10 can provide accurate information)

Next-Use (Step 2)

$i: a := b + c$

$live(a) = true$	$nextuse(a) = j$
$live(b) = true$	$nextuse(b) = j$
$live(t) = false$	$nextuse(t) = none$

$j: t := a + b$ [$live(a) = true, live(b) = true, live(t) = true,$
 $nextuse(a) = none, nextuse(b) = none, nextuse(t) = none$]

Compute live/next-use information at j

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Next-Use (Step 3)

$i: a := b + c$ [$live(a) = true, live(b) = true, live(c) = false,$
 $nextuse(a) = j, nextuse(b) = j, nextuse(c) = none$]

$j: t := a + b$ [$live(a) = true, live(b) = true, live(t) = true,$
 $nextuse(a) = none, nextuse(b) = none, nextuse(t) = none$]

Attach current live/next-use information to i

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Next-Use (Step 4)

$live(a) = false$	$nextuse(a) = none$
$live(b) = true$	$nextuse(b) = i$
$live(c) = true$	$nextuse(c) = i$
$live(t) = false$	$nextuse(t) = none$

$i: a := b + c$ [$live(a) = true, live(b) = true, live(c) = false,$
 $nextuse(a) = j, nextuse(b) = j, nextuse(c) = none$]

$j: t := a + b$ [$live(a) = false, live(b) = false, live(t) = false,$
 $nextuse(a) = none, nextuse(b) = none, nextuse(t) = none$]

Compute live/next-use information i

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A Code Generator

- ⌘ Generates target code for a sequence of three-address statements using next-use information
- ⌘ Uses new function *getreg* to assign registers to variables
- ⌘ Computed results are kept in registers as long as possible, which means:
 - ☑ Result is needed in another computation
 - ☑ Register is kept up to a procedure call or end of block
- ⌘ Checks if operands to three-address code are available in registers

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The Code Generation Algorithm

- ⌘ For each statement $x := y \text{ op } z$
 1. Set location $L = \text{getreg}(y, z)$
 2. If $y \notin L$ then generate
`MOV y', L`
where y' denotes one of the locations where the value of y is available (choose register if possible)
 3. Generate
`OP z', L`
where z' is one of the locations of z ,
Update register/address descriptor of x to include L
 4. If y and/or z has no next use and is stored in register, update register descriptors to remove y and/or z

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Register and Address Descriptors

- ⌘ A *register descriptor* keeps track of what is currently stored in a register at a particular point in the code, e.g. a local variable, argument, global variable, etc.
`MOV a, R0` "`R0` contains `a`"
- ⌘ An *address descriptor* keeps track of the location where the current value of the name can be found at run time, e.g. a register, stack location, memory address, etc.
`MOV a, R0`
`MOV R0, R1` "`a` in `R0` and `R1`"

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The *getreg* Algorithm

- ⌘ To compute *getreg*(*y*,*z*)
1. If *y* is stored in a register *R* and *R* only holds the value *y*, and *y* has no next use, then return *R*;
Update address descriptor: value *y* no longer in *R*
 2. Else, return a new empty register if available
 3. Else, find an occupied register *R*;
Store contents (register spill) by generating
`MOV R, M`
for every *M* in address descriptor of *y*;
Return register *R*
 4. Return a memory location

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Code Generation Example

<i>Statements</i>	<i>Code Generated</i>	<i>Register Descriptor</i>	<i>Address Descriptor</i>
<code>t := a - b</code>	<code>MOV a, R0 SUB b, R0</code>	Registers empty R0 contains t	t in R0
<code>u := a - c</code>	<code>MOV a, R1 SUB c, R1</code>	R0 contains t R1 contains u	t in R0 u in R1
<code>v := t + u</code>	<code>ADD R1, R0</code>	R0 contains v R1 contains u	u in R1 v in R0
<code>d := v + u</code>	<code>ADD R1, R0 MOV R0, d</code>	R0 contains d	d in R0 d in R0 and memory

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Register Allocation and Assignment

- ⌘ The *getreg* algorithm is simple but sub-optimal
 - ☒ All live variables in registers are stored (flushed) at the end of a block
- ⌘ *Global register allocation* assigns variables to limited number of available registers and attempts to keep these registers consistent across basic block boundaries
 - ☒ Keeping variables in registers in looping code can result in big savings

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Allocating Registers in Loops

- ⌘ Suppose loading a variable x has a cost of 2
- ⌘ Suppose storing a variable x has a cost of 2
- ⌘ Benefit of allocating a register to a variable x within a loop L is
$$\sum_{B \in L} (use(x, B) + 2 live(x, B))$$
where $use(x, B)$ is the number of times x is used in B and $live(x, B) = \text{true}$ if x is live on exit from B

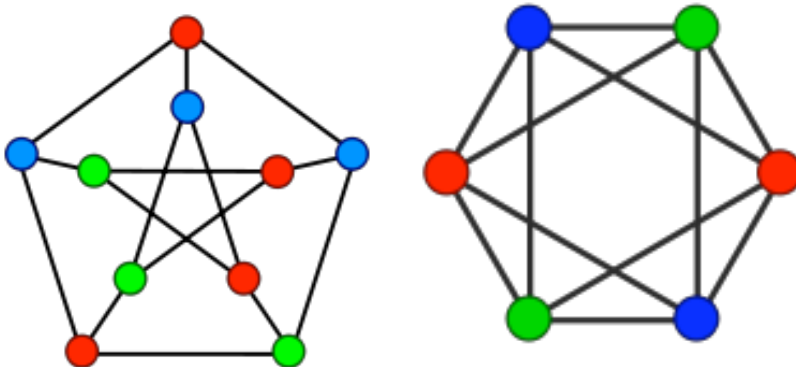
42

Global Register Allocation Using Graph Coloring

- ⌘ When a register is needed but all available registers are in use, the content of one of the used registers must be stored (spilled) to free a register
- ⌘ Graph coloring allocates registers and attempts to minimize the cost of spills
- ⌘ Build a *conflict graph* (*interference graph*)
- ⌘ Find a k -coloring for the graph, with k the number of registers

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Graph Coloring Example



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Peephole Optimization

- ⌘ Examines a short sequence of target instructions in a window (peephole) and replaces the instructions by a faster and/or shorter sequence when possible
- ⌘ Applied to intermediate code or target code
- ⌘ Typical optimizations:
 - ☒ Redundant instruction elimination
 - ☒ Flow-of-control optimizations
 - ☒ Algebraic simplifications
 - ☒ Use of machine idioms

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Peephole Opt: Eliminating Redundant Loads and Stores

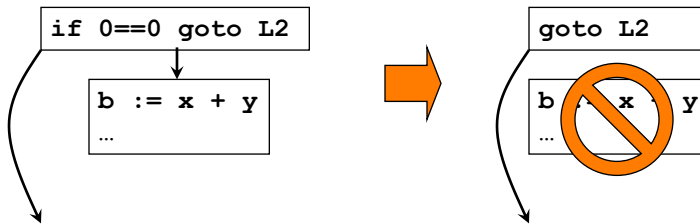
- ⌘ Consider

```
MOV R0 , a
MOV a , R0
```
- ⌘ The second instruction can be deleted, but only if it is not labeled with a target label
 - ☒ Peephole represents sequence of instructions with at most one entry point
- ⌘ The first instruction can also be deleted if $live(a) = false$

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Peephole Optimization: Deleting Unreachable Code

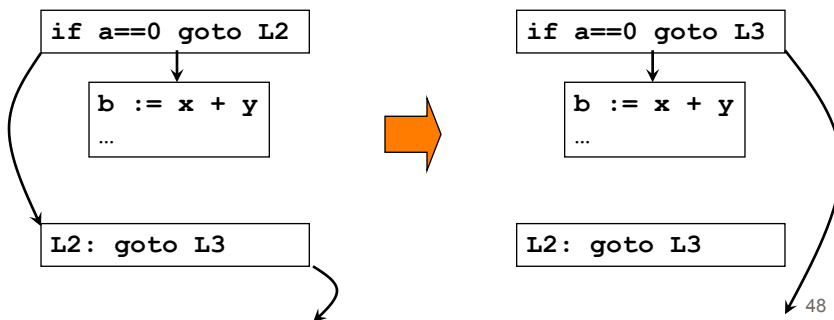
⌘ Unlabeled blocks can be removed



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Peephole Optimization: Branch Chaining

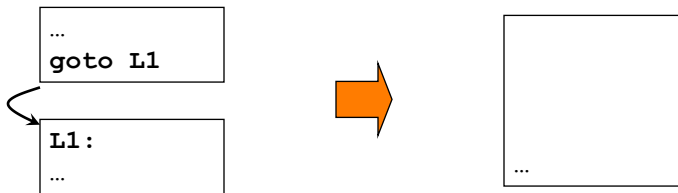
⌘ Shorten chain of branches by modifying target labels



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Peephole Optimization: Other Flow-of-Control Optimizations

⌘ Remove redundant jumps



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Other Peephole Optimizations

⌘ *Reduction in strength*: replace expensive arithmetic operations with cheaper ones



⌘ Utilize machine idioms



⌘ Algebraic simplifications



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Code Optimization



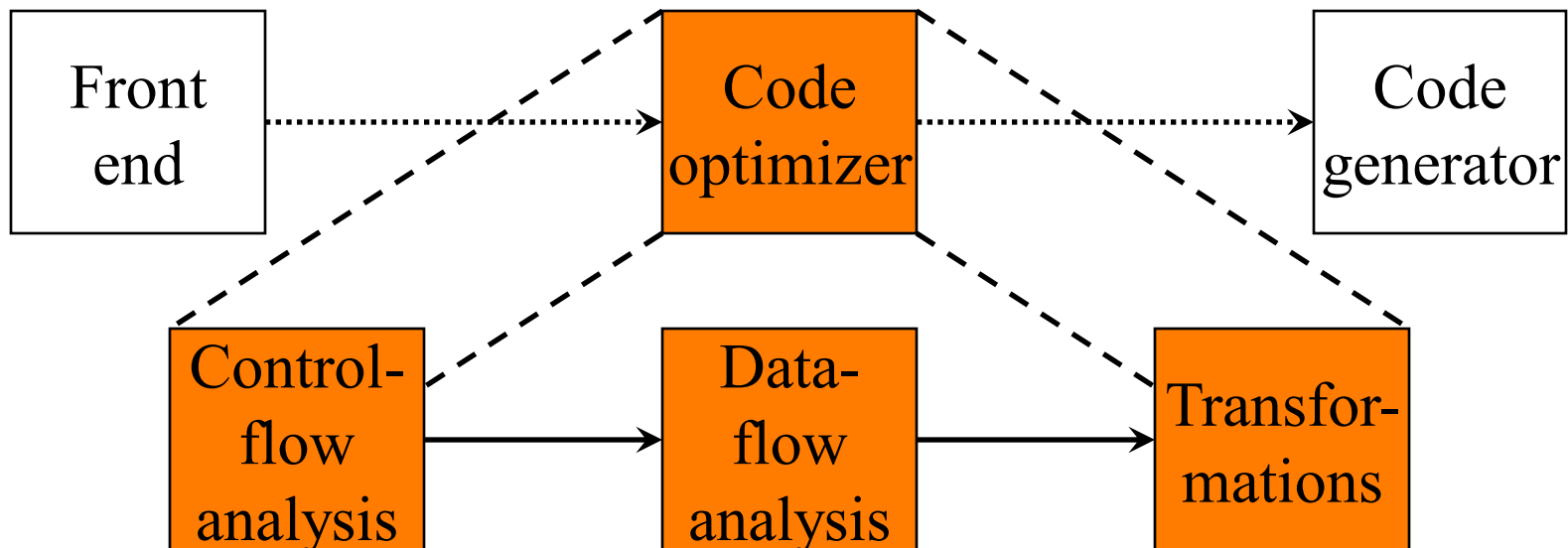
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The Code Optimizer

- ⌘ Control flow analysis: CFG (Ch. 9)
- ⌘ Data-flow analysis
- ⌘ Transformations



Code Optimizations



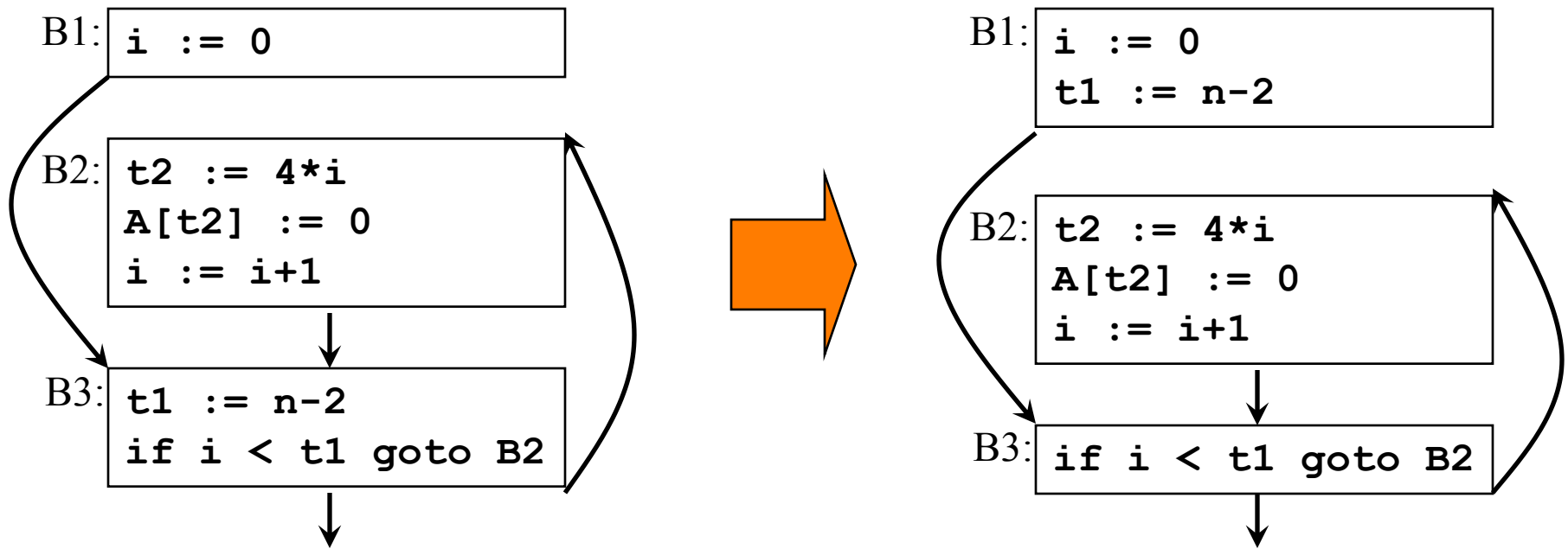
- ⌘ Local/global common subexpression elimination
- ⌘ Dead-code elimination
- ⌘ Instruction reordering
- ⌘ Constant folding
- ⌘ Algebraic transformations
- ⌘ Copy propagation
- ⌘ *Loop optimizations*

Loop Optimizations



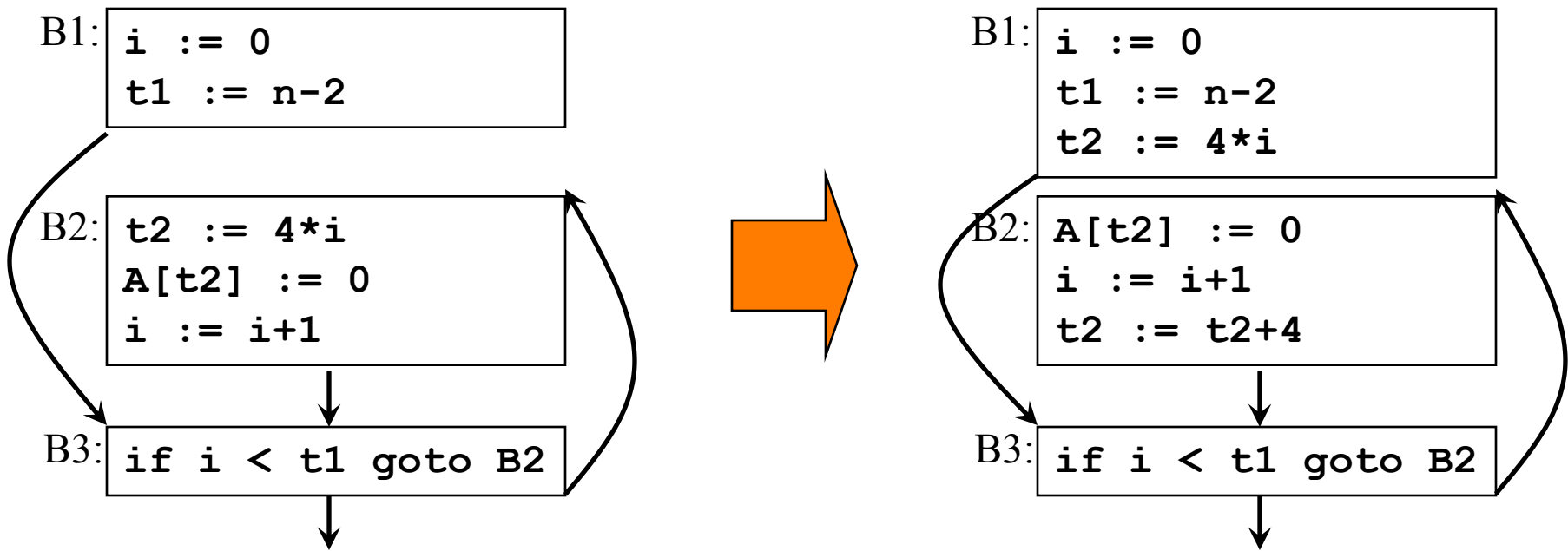
- ⌘ Code motion
- ⌘ Induction variable elimination
- ⌘ Reduction in strength
- ⌘ ... lots more

Code Motion



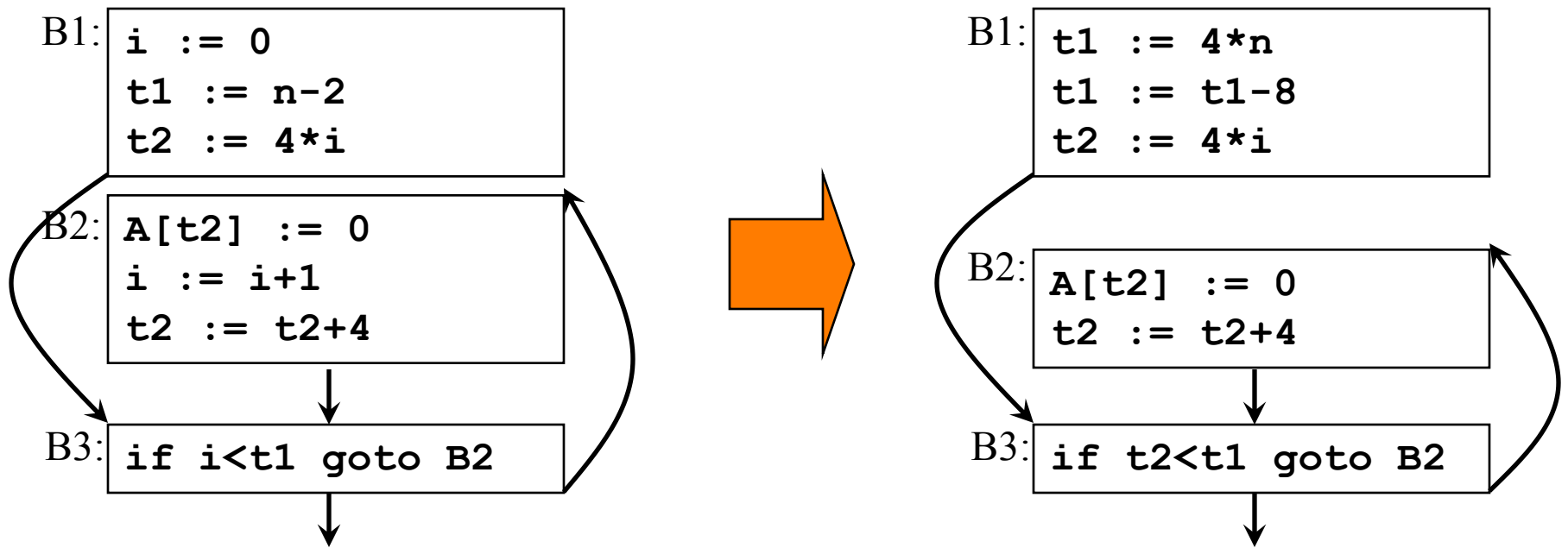
Move *loop-invariant computations* before the loop

Strength Reduction



Replace expensive computations with *induction variables*

Reduction Variable Elimination



Replace induction variable in expressions with another

Determining Loops in Flow Graphs: Dominators

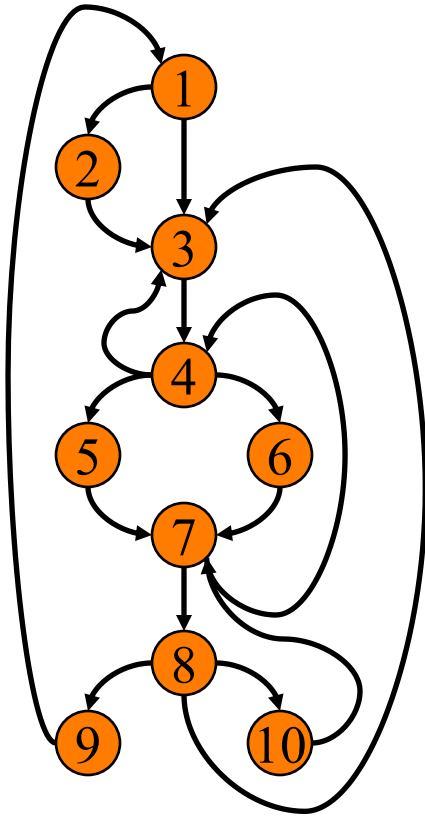
⌘ Dominators: $d \text{ dom } n$

- ☑ Node d of a CFG *dominates* node n if *every* path from the initial node of the CFG to n goes through d
- ☑ The loop entry dominates all nodes in the loop

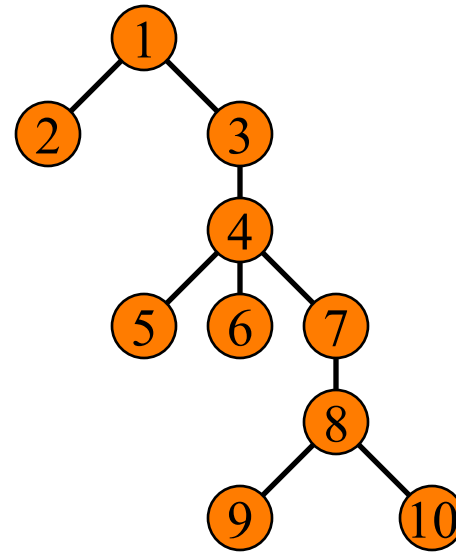
⌘ The *immediate dominator* m of a node n is the last dominator on the path from the initial node to n

- ☑ If $d \neq n$ and $d \text{ dom } n$ then $d \text{ dom } m$

Dominator Trees



CFG



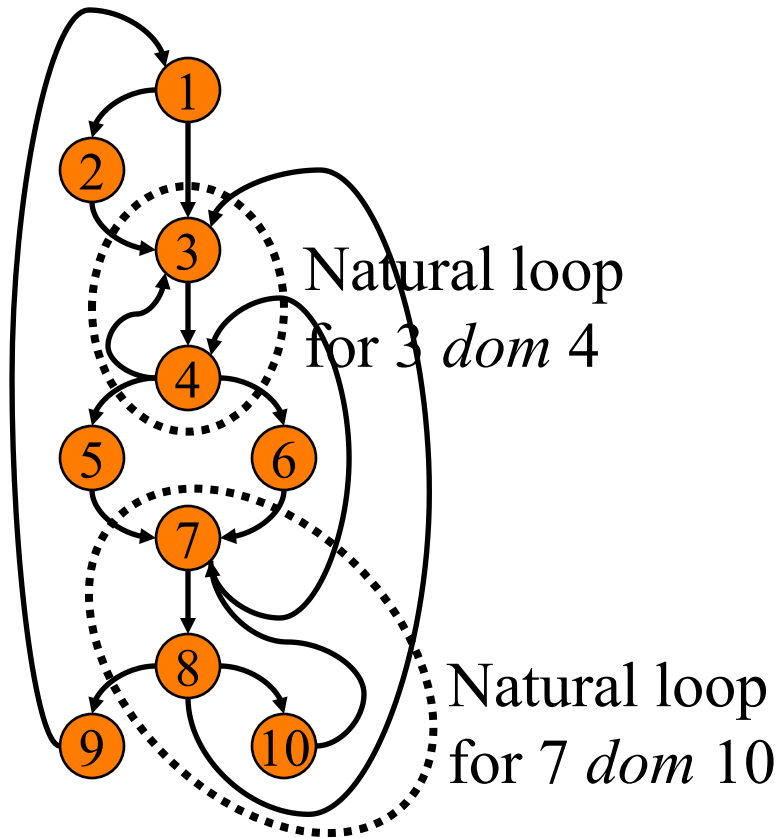
Dominator tree

Natural Loops

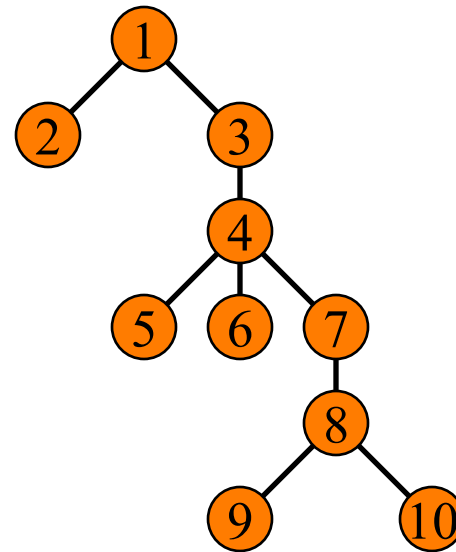


- ⌘ A *back edge* is an edge $a \rightarrow b$ whose head b dominates its tail a
- ⌘ Given a back edge $n \rightarrow d$
 - ☑ The *natural loop* consists of d plus the nodes that can reach n without going through d
 - ☑ The *loop header* is node d
- ⌘ Unless two loops have the same header, they are disjoint or one is nested within the other
 - ☑ A nested loop is an *inner loop* if it contains no other loops

Natural (Inner) Loops Example



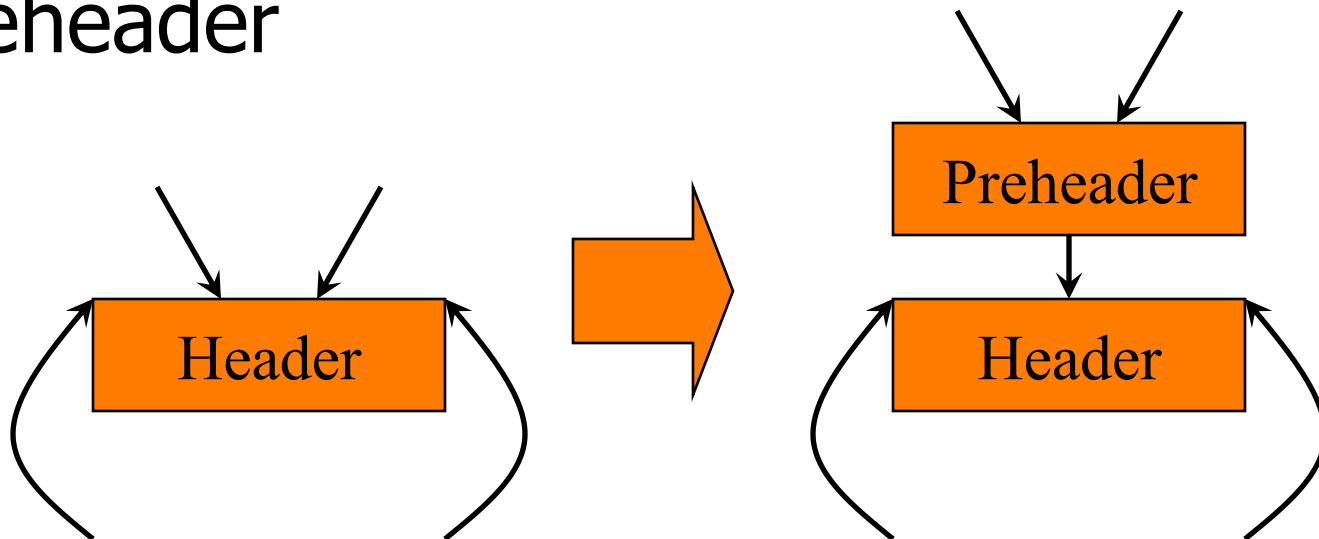
CFG



Dominator tree

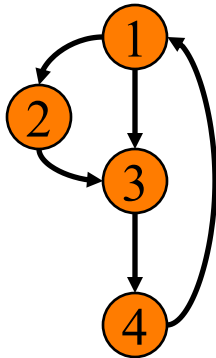
Pre-Headers

- ⌘ To facilitate loop transformations, a compiler often adds a *preheader* to a loop
- ⌘ Code motion, strength reduction, and other loop transformations populate the preheader

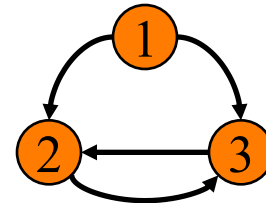


Reducible Flow Graphs

⌘ *Reducible graph* = disjoint partition in forward and back edges such that the forward edges form an acyclic (sub)graph



Example of a
reducible CFG



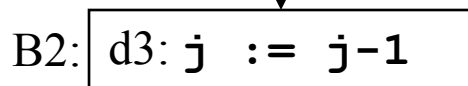
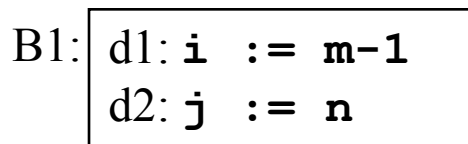
Example of a
nonreducible CFG

Global Data-Flow Analysis

⌘ To apply global optimizations on basic blocks, *data-flow information* is collected by solving systems of *data-flow equations*

⌘ Suppose we need to determine the *reaching definitions* for a sequence of statements S

$$out[S] = gen[S] \cup (in[S] - kill[S])$$

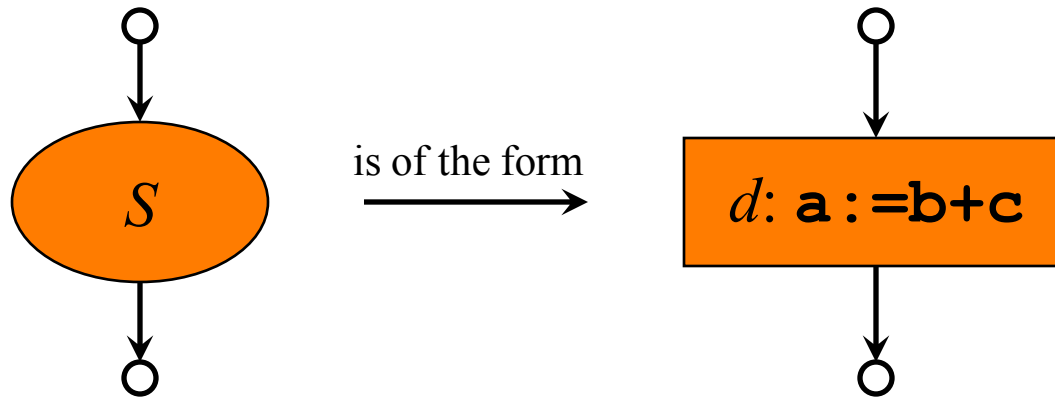


$$out[B1] = gen[B1] = \{d1, d2\}$$

$$out[B2] = gen[B2] \cup \{d1\} = \{d1, d3\}$$

d1 reaches B2 and B3 and
d2 reaches B2, but not B3
because d2 is killed in B2

Reaching Definitions

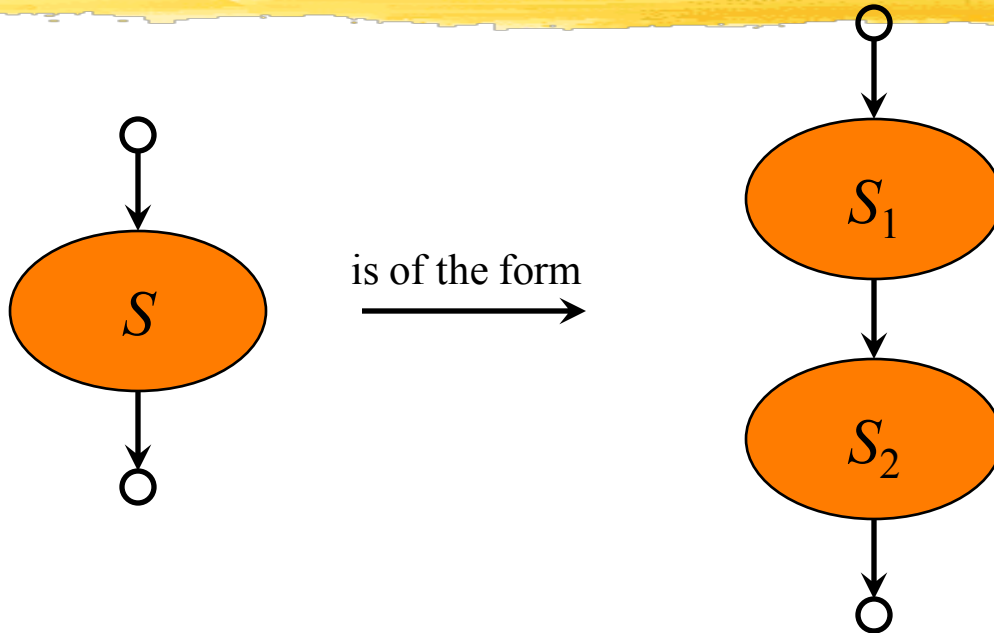


Then, the data-flow equations for S are:

$$\begin{aligned} gen[S] &= \{d\} \\ kill[S] &= D_a - \{d\} \\ out[S] &= gen[S] \cup (in[S] - kill[S]) \end{aligned}$$

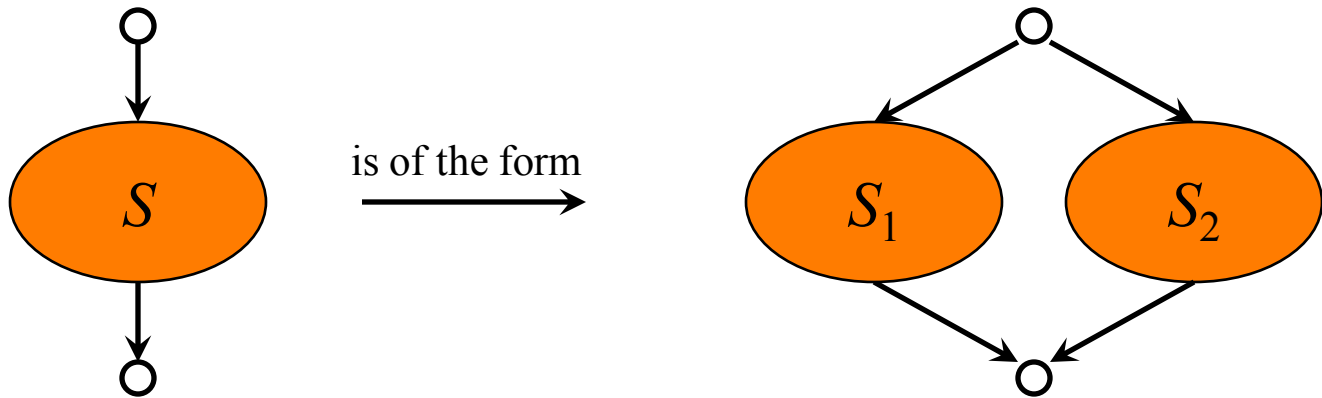
where D_a = all definitions of \mathbf{a} in the region of code

Reaching Definitions



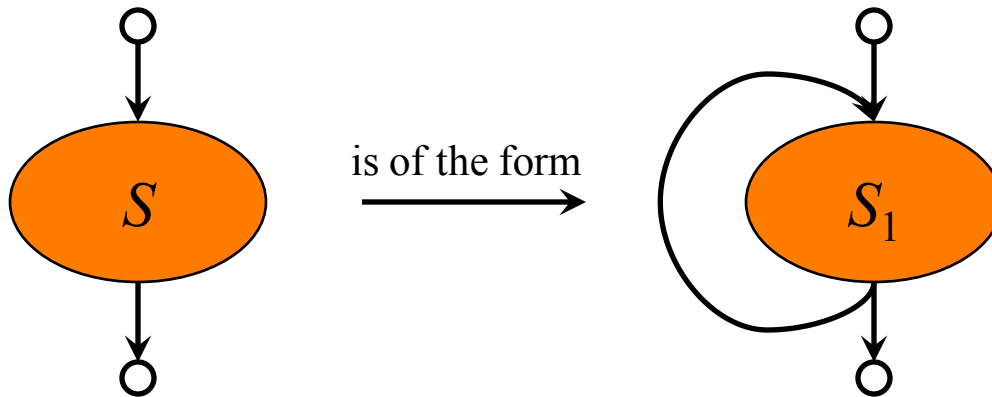
$$\begin{aligned} gen[S] &= gen[S_2] \cup (gen[S_1] - kill[S_2]) \\ kill[S] &= kill[S_2] \cup (kill[S_1] - gen[S_2]) \\ in[S_1] &= in[S] \\ in[S_2] &= out[S_1] \\ out[S] &= out[S_2] \end{aligned}$$

Reaching Definitions



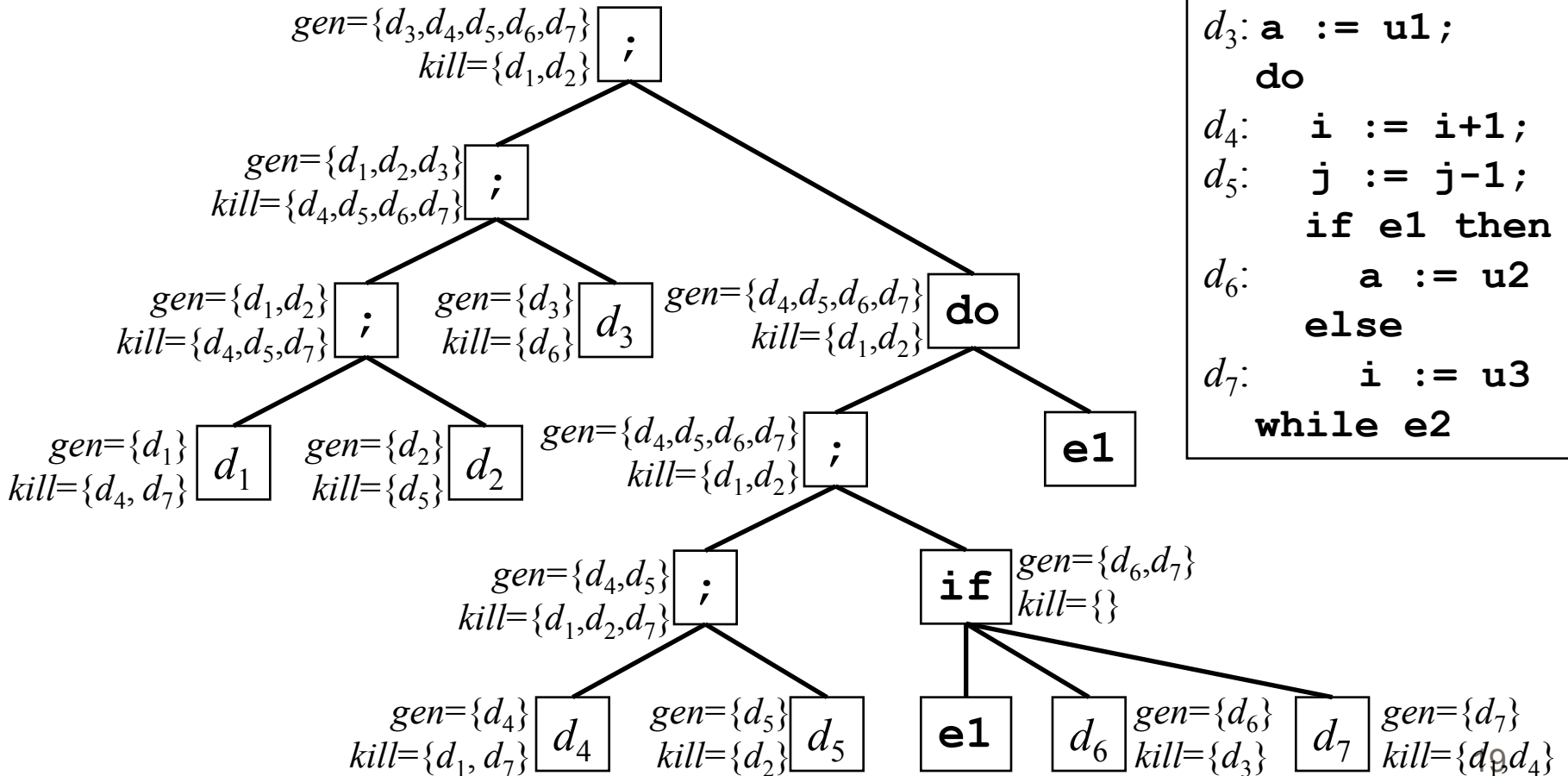
$$\begin{aligned} gen[S] &= gen[S_1] \cup gen[S_2] \\ kill[S] &= kill[S_1] \cap kill[S_2] \\ in[S_1] &= in[S] \\ in[S_2] &= in[S] \\ out[S] &= out[S_1] \cup out[S_2] \end{aligned}$$

Reaching Definitions

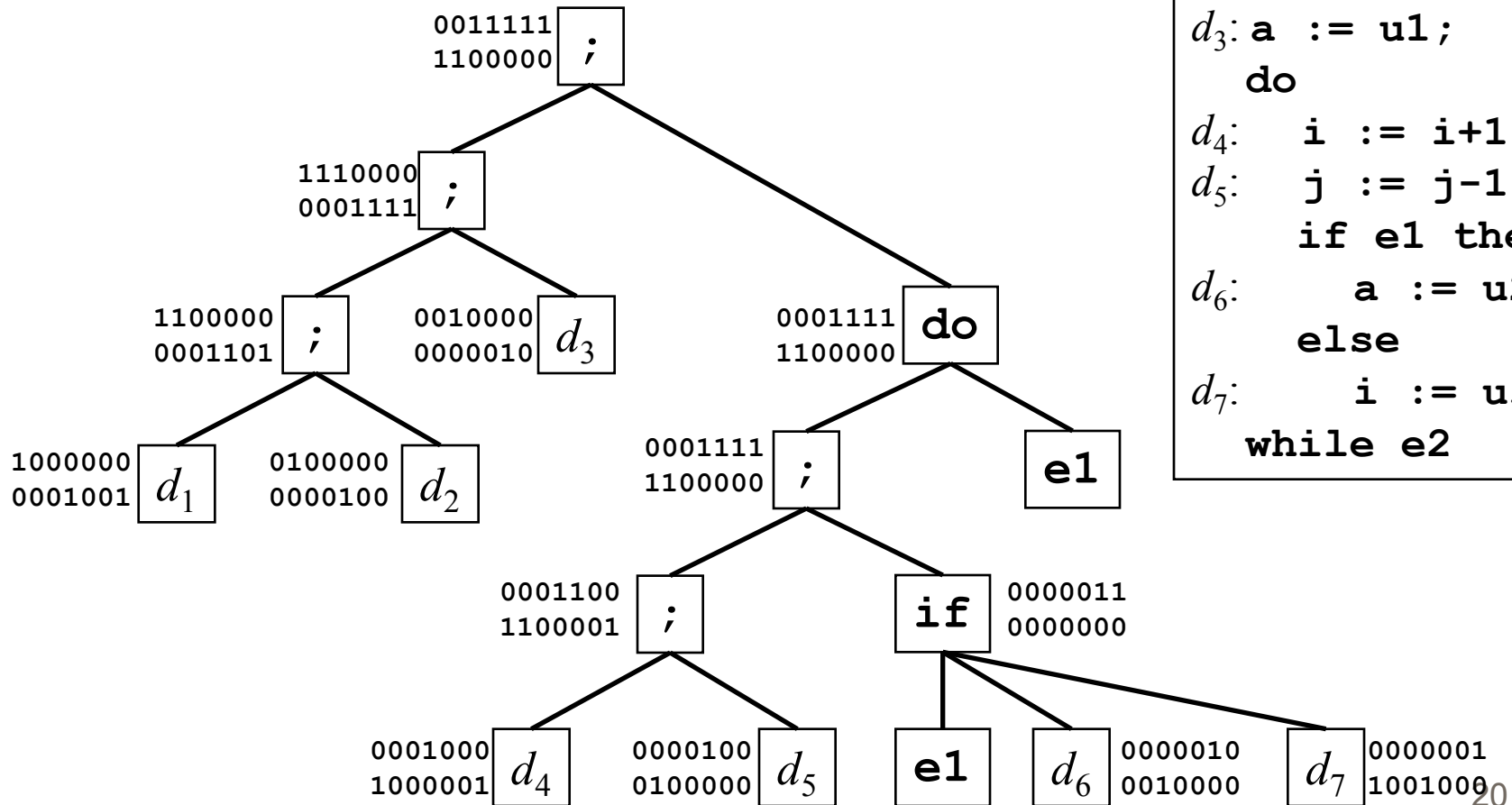


$$\begin{aligned} gen[S] &= gen[S_1] \\ kill[S] &= kill[S_1] \\ in[S_1] &= in[S] \cup gen[S_1] \\ out[S] &= out[S_1] \end{aligned}$$

Example Reaching Definitions



Using Bit-Vectors to Compute Reaching Definitions



```

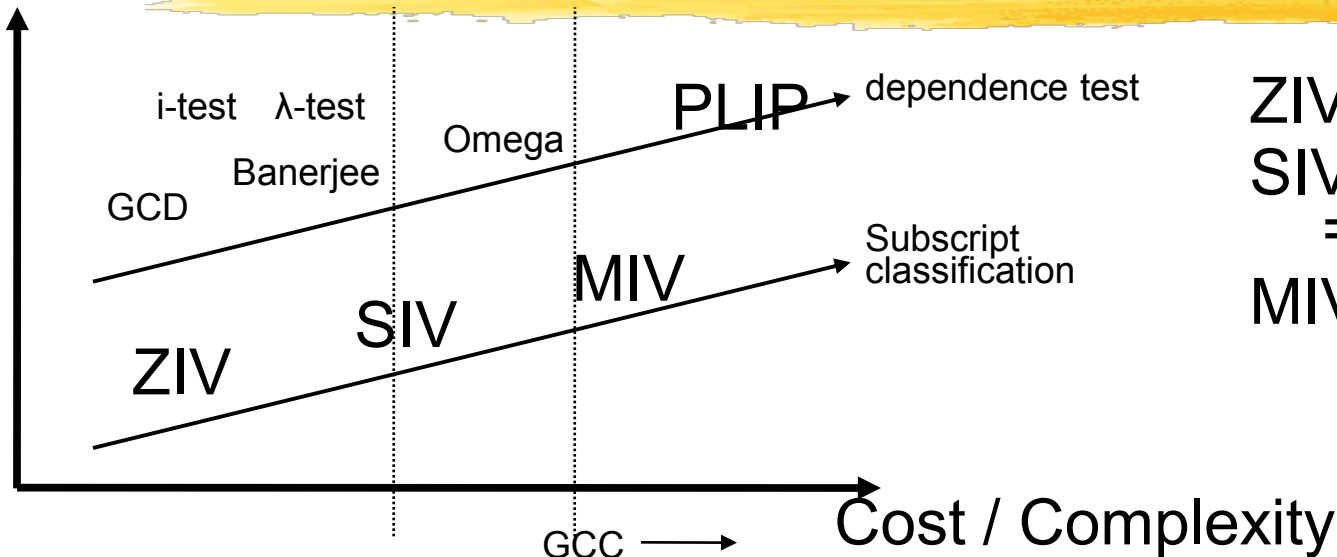
d1: i := m-1;
d2: j := n;
d3: a := u1;
do
d4: i := i+1;
d5: j := j-1;
if e1 then
d6: a := u2
else
d7: i := u3
while e2
  
```

QR Algorithm – Smart Antenna

Matlab Code (QR Algorithm)

```
%parameter N 8 16;  
%parameter K 100 1000;  
  
for k = 1:1:K,  
    for j = 1:1:N,  
        [ r(j,j), x(k,j), t ]=Vectorize( r(j,j), x(k,j) );  
        for i = j+1:1:N,  
            [ r(j,i), x(k,i), t]=Rotate( r(j,i), x(k,i), t );  
        end  
    end  
end
```

Data Dependence Tests



$$\text{ZIV: } a[3] = a[5]$$

$$\text{SIV: } a[i] = a[2], \quad a[i] = a[i]$$

$$\text{MIV: } a[i][j] = a[j][i+j]$$

GCD, Banerjee, i-test, λ-test, cannot handle:

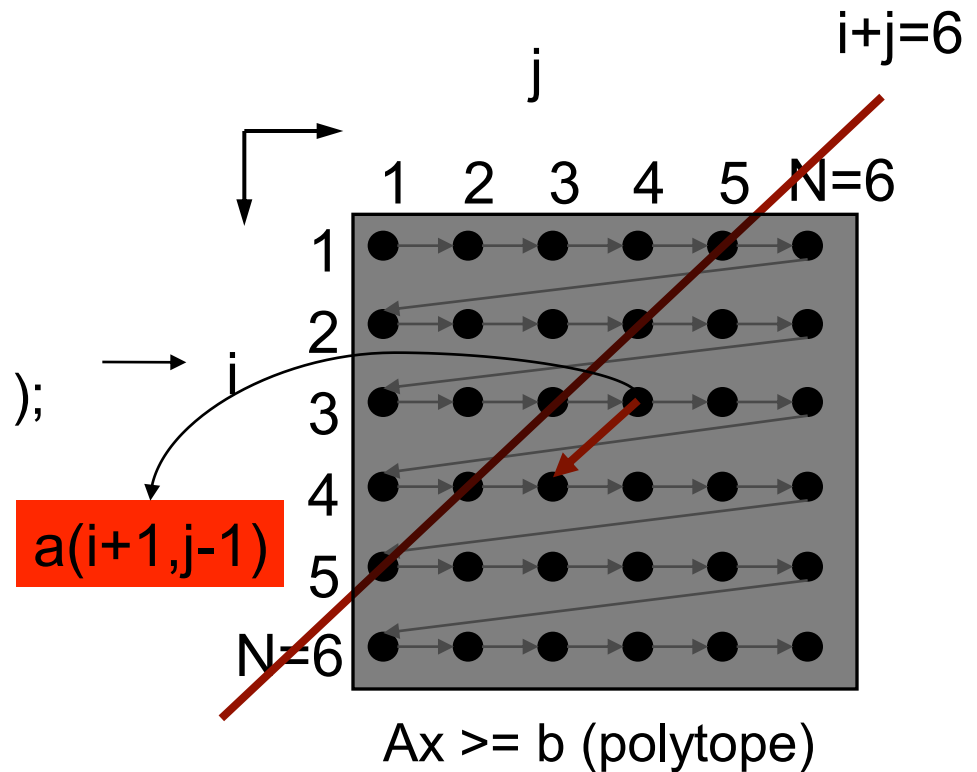
- ⌘ if conditionals
- ⌘ parametric loop bounds
- ⌘ coupled subscripts
- ⌘ parametric subscripts

Omega, PLIP:

- ⌘ Exact data dependencies
- ⌘ Omega: Fourier-Motzkin
- ⌘ PLIP: dual-simplex method, more precise with parametric codes

Exact Dependency Analysis

```
for i= 1 : 1 : N,  
  for j= 1 : 1 : N,  
    [ a(i+j) ] = funcA( a(i+j) );  
  end  
end
```



The for-next loops define an Iteration Domain

Many more optimizations



⌘ Aliases analysis (pointers)

- ☑ if two or more expressions denote the same memory address, the expressions are aliases of one another.

Compiler Frameworks



⌘ Open Source

- ☒ GCC
- ☒ LLVM
- ☒ Open64
- ☒ SUIF

⌘ Commercial

- ☒ Target
- ☒ Altrium
- ☒ ACE

⌘ In-house

- ☒ Many

Compilers

